

Volumes - Lesson 5

Volume of a Sphere - Non-Calculator

LI

- Calculate the Volume of a Sphere without using a calculator.

SC

- Sphere formula.

Volume of a Sphere

$$V = \frac{4}{3} \pi r^3$$

(r is radius of sphere)

Remember, r^3 means $r \times r \times r$

$$V = 4 \times \pi \times r \times r \times r \div 3$$

For this lesson, we will approximate

π as 3.141

Useful calculation for this lesson ($\pi \div 3$):

$$\begin{array}{r} 1 \cdot 0 \ 4 \ 7 \\ 3 \overline{)3 \cdot 1 \ 4 \ 1}^{\text{1}} \\ \end{array}$$

Example 1

Calculate the volume of a sphere of radius 2 cm.

Take $\pi = 3.141$.

$$V = 4 \times \pi \times r^3 \div 3$$

$$V = 4 \times 3.141 \times 2^3 \div 3$$

$$V = 4 \times 1.047 \times 8$$

$$V = 4.188 \times 8$$

$$V = 33.504 \text{ cm}^3$$

Example 2

Calculate the volume of a sphere of radius 10 cm.

Take $\pi = 3.141$.

$$V = 4 \times \pi \times r^3 \div 3$$

$$V = 4 \times 3.141 \times 10^3 \div 3$$

$$V = 4 \times 1.047 \times 1000$$

$$V = 4.188 \times 1000$$

$$V = 4188 \text{ cm}^3$$

Example 3

Calculate the exact volume (meaning leave your answer in terms of π) of a sphere of radius 3 cm.

$$V = 4 \times \pi \times r^3 \div 3$$

$$V = 4 \times \pi \times 3^3 \div 3$$

$$V = 4 \times \pi \times 27 \div 3$$

$$V = 4 \times \pi \times 9$$

$$V = 36\pi \text{ cm}^3$$

Example 4

Calculate the exact volume (meaning leave your answer in terms of π) of a sphere of radius 6 cm.

$$V = 4 \times \pi \times r^3 \div 3$$

$$V = 4 \times \pi \times 6^3 \div 3$$

$$V = 4 \times \pi \times 216 \div 3$$

$$V = 4 \times \pi \times 72$$

$$V = 288\pi \text{ cm}^3$$

Calculate the **volumes** of these spheres :

Take $\pi = 3.141$

Exact volume (answer in terms of π)

1) $r = 1 \text{ cm}$

5) $r = 2 \text{ cm}$

2) $r = 100 \text{ cm}$

6) $r = 9 \text{ cm}$

3) $r = 1/2 \text{ cm}$

7) $r = 4 \text{ cm}$

4) $r = 1/10 \text{ cm}$

8) $r = 5 \text{ cm}$

Calculate the **volumes** of these spheres :

Take $\pi = 3.141$

Exact volume (answer in terms of π)

1) 4.188 cm^3

5) $32\pi/3 \text{ cm}^3$

2) 4188000 cm^3

6) $972\pi \text{ cm}^3$

3) 0.5235 cm^3

7) $256\pi/3 \text{ cm}^3$

4) 0.004188 cm^3

8) $500\pi/3 \text{ cm}^3$