

Solving Trigonometric Equations - Lesson 3

Solving Trigonometric Equations (Rearranging : 0° to 360°)

LI

- Solve trigonometric equations after rearranging into the form :

$$\sin x^\circ = a$$

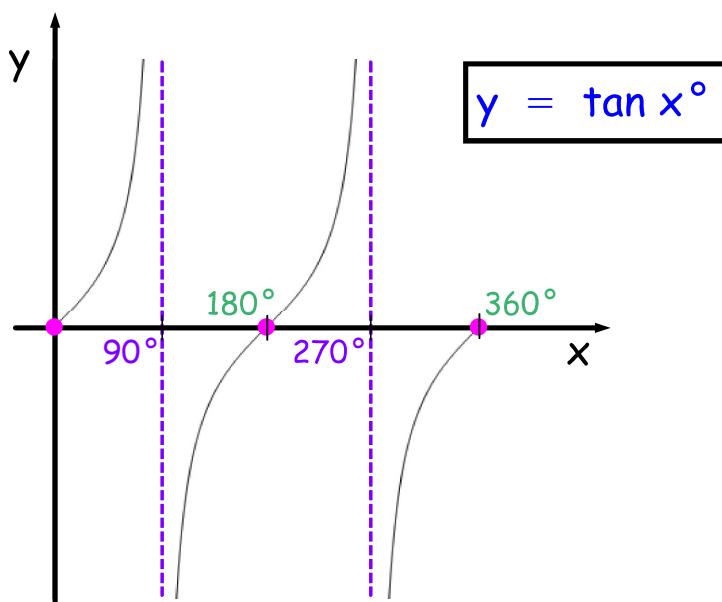
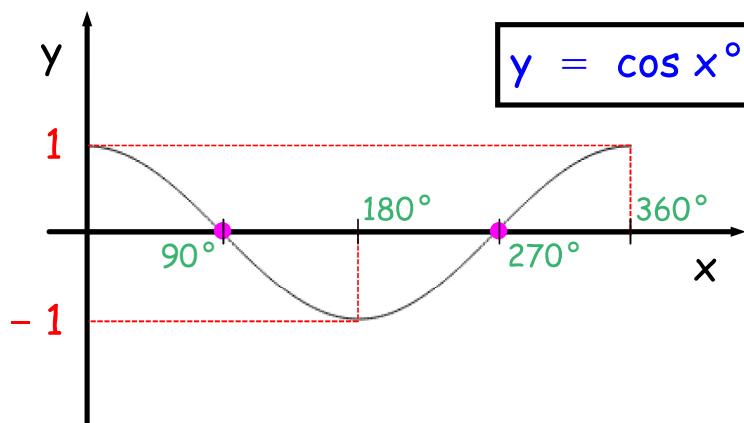
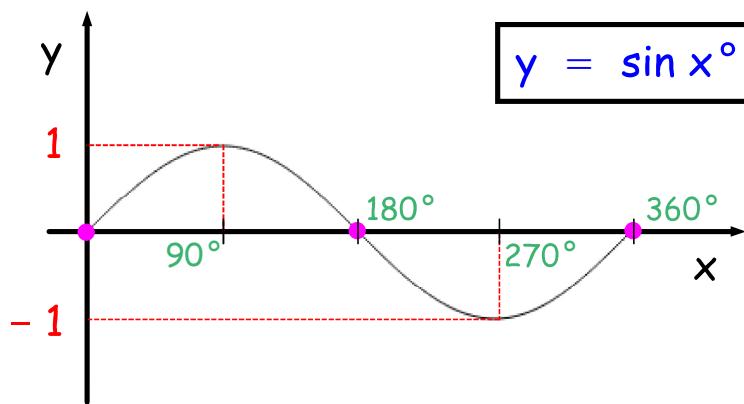
$$\cos x^\circ = a \quad \text{between } 0^\circ \text{ and } 360^\circ$$

$$\tan x^\circ = a$$

SC

- Graphs of $y = \sin x^\circ$, $y = \cos x^\circ$ and $y = \tan x^\circ$ between 0° and 360° .
- Use the ASTC Diagram.

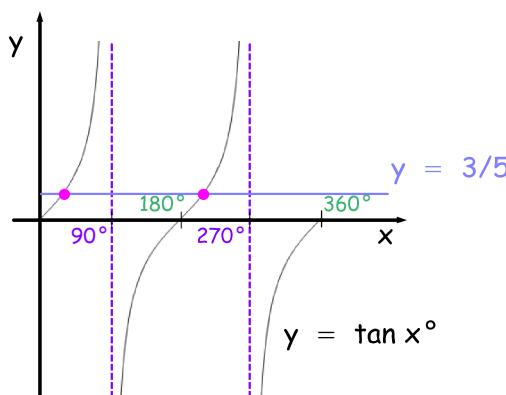
Trigonometric Graphs Between 0° and 360°



Example 1

Solve $5 \tan x^\circ - 3 = 0$ for $0^\circ \leq x^\circ \leq 360^\circ$ (1 d.p.).

$$\begin{aligned} 5 \tan x^\circ - 3 &= 0 \\ \Rightarrow 5 \tan x^\circ &= 3 \\ \Rightarrow \underline{\tan x^\circ} &= 3/5 \end{aligned}$$

STEP 1

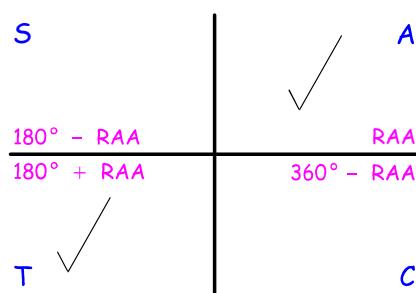
(Expecting 2 answers)

STEP 2

$$\begin{aligned} RAA &= \tan^{-1}(3/5) \\ \Rightarrow \underline{RAA} &= 30.96\ldots^\circ \end{aligned}$$

STEP 3

$$\begin{array}{c} \tan x^\circ = 3/5 \\ \text{main equation} \\ \boxed{\tan \text{ is +ve}} \end{array}$$

STEP 4

$$x^\circ = RAA, 180^\circ + RAA$$

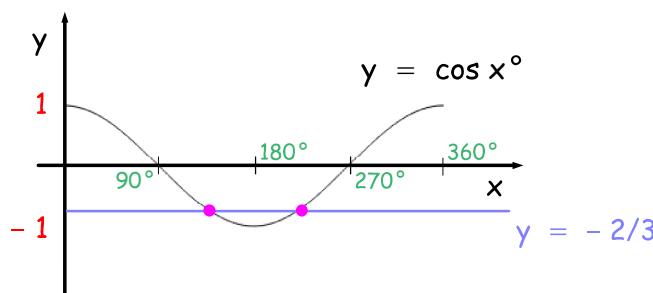
$$\therefore x^\circ = 31.0^\circ, 180^\circ + 31.0^\circ$$

$$\Rightarrow \boxed{x^\circ = 31.0^\circ, 211.0^\circ}$$

Example 2

Solve $3 \cos x^\circ + 4 = 2$ for $0^\circ \leq x^\circ \leq 360^\circ$. (1 d.p.).

$$\begin{aligned} 3 \cos x^\circ + 4 &= 2 \\ \Rightarrow 3 \cos x^\circ &= -2 \\ \Rightarrow \underline{\cos x^\circ} &= -2/3 \end{aligned}$$

STEP 1

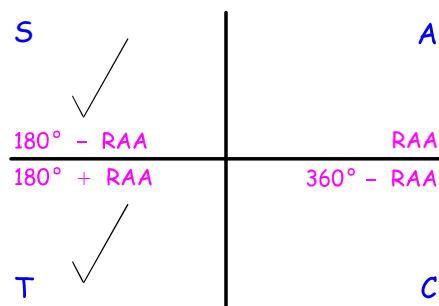
(Expecting 2 answers)

STEP 2

$$\begin{aligned} RAA &= \cos^{-1}(2/3) \\ \Rightarrow \underline{RAA} &= 48.18\dots^\circ \end{aligned}$$

STEP 3

$$\begin{array}{c} \text{main equation} \\ \cos x^\circ = -2/3 \end{array} \quad \boxed{\cos \text{ is } -\text{ve}}$$

STEP 4

$$x^\circ = 180^\circ - RAA, 180^\circ + RAA$$

$$\therefore x^\circ = 180^\circ - 48.2^\circ, 180^\circ + 48.2^\circ$$

$$\Rightarrow \boxed{x^\circ = 131.8^\circ, 228.2^\circ}$$

CfE N5 Maths

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Questions

- 1 Solve for $0 \leq x \leq 360$, giving your answers to 1 decimal place.
- a $3\sin x^\circ - 2 = 0$ b $4\cos x^\circ + 1 = 2$ c $5\tan x^\circ - 4 = 3$
d $4\cos x^\circ + 3 = 0$ e $8 + 3\tan x^\circ = 4$ f $7 - 3\cos x^\circ = 6$
g $4\sin x^\circ - 5 = -1$ h $6\cos x^\circ + 2 = 7$ i $3 + 5\sin x^\circ = 7$
j $2\tan x^\circ - 3 = 5$ k $2\cos x^\circ + 3 = 1$ l $5 - 4\sin x^\circ = 8$
- 2 The height, h metres, of a carriage on a Ferris wheel is given by the equation
$$h = 35 + 30\sin t^\circ$$
where t is the time in seconds after starting.
- a Calculate the height after 45 seconds.
b i After how many seconds is the carriage first at a height of 50 m?
ii When does it next reach this height?

Answers

- 1 a $x = 41.8^\circ, x = 138.2^\circ$
b $x = 75.5^\circ, x = 284.5^\circ$
c $x = 54.5^\circ, x = 234.5^\circ$
d $x = 138.6^\circ, x = 221.4^\circ$
e $x = 126.9^\circ, x = 306.9^\circ$
f $x = 70.5^\circ, x = 289.5^\circ$
g $x = 90.0^\circ$
h $x = 33.6^\circ, x = 326.4^\circ$
i $x = 53.1^\circ, x = 126.9^\circ$
j $x = 76.0^\circ, x = 256.0^\circ$
k $x = 180.0^\circ$
l $x = 228.6^\circ, x = 311.4^\circ$

- 2 a $h = 56.2\text{m}$
b i $x = 30.0\text{s}$
ii $x = 150.0\text{s}$