## Advanced Trigonometry - Lesson 3

## Sine Rule (Length)

## LI

- Use the Sine Rule to find a missing length in any triangle.

SC

- Use a calculator properly.

Sine Rule


## Strategy for Finding Missing Length

- Sketch triangle and label all sides and angles
- Write down Sine Rule
- Tick the things you know
- Solve for missing length (set calculator to degrees)

Example 1
Calculate a to $1 \mathrm{~d} . \mathrm{p}$.


$$
\frac{a}{\sin A^{\circ}}=\frac{b}{\sin B^{\circ}}=\frac{c}{\sin C^{\circ}}
$$

$$
\begin{aligned}
& \\
& A^{\circ}=54^{\circ}, \quad a= \\
& B^{\circ}=38^{\circ}, \quad b=740 \\
& C^{\circ}=c= \\
& \frac{a}{\sin A^{\circ}}=\frac{b}{\sin B^{\circ}} \\
& \frac{a}{\sin 54^{\circ}}=\frac{740}{\sin 38^{\circ}} \\
& a=\frac{\left(740 \times \sin 54^{\circ}\right)}{\sin 38^{\circ}}
\end{aligned}
$$

$$
a=972.4
$$

## Example 2

Calculate $p$ to the nearest centimetre.

$$
\frac{P}{\sin P^{\circ}}=\frac{f}{\sin F^{\circ}}=\frac{r}{\sin R^{\circ}}
$$

$$
p^{0}=114^{\circ}, p=
$$

$$
F^{\circ}=24^{\circ}, f=16.4 \mathrm{~m}
$$

$$
R^{\circ}=42^{\circ}, r=
$$

$$
\frac{P}{\sin P^{o}}=\frac{f}{\sin F^{\circ}}
$$

$$
\frac{p}{\sin 114^{\circ}}=\frac{16.4}{\sin 24^{\circ}}
$$

$$
p=\frac{\left(16.4 \times \sin 114^{\circ}\right)}{\sin 24^{\circ}}
$$

$$
p=36.835 \ldots
$$

$$
p=36.84 \mathrm{~m}
$$

## Questions

1 Find the size of the missing side in each triangle. Give your answers to 3 significant figures.
a

b

C

d

e

f


4 A helicopter flies from Helipad A.
It then needs to land at Helipad B.
How far apart are the two helipads?
Give your answer to 3 significant
figures.


6 A metal support for a roof at a stadium is shown. Calculate the size of the beam labelled $x$ to 2 significant figures.


7 Two surveyors measure the distance across a river in order to build a bridge. They measure the information shown.
Calculate the width $W$ of the river giving your answer to 3 significant figures.


8 Jane uses a pulley system to lift a weight. The pulley is mounted to the ceiling as shown.
a Calculate the length of rope marked $x$ giving your answer to 2 significant figures.
b The weight has to be attached to the ceiling. What distance must the weight be lifted?


10 Two ships $A$ and $B$ are 500 m apart. Their navigators measure the angles from the sea level to the top of the cliff. Find the height of the cliff. Give your answer to 3 significant figures.


## Answers

| $\mathbf{1}$ | $\mathbf{a}$ | 15.2 cm | $\mathbf{4}$ | 3.57 km |
| :--- | :--- | :--- | :--- | :--- |
|  | $\mathbf{b}$ | 4.85 cm | $\mathbf{6}$ | 4 m |
|  | c | 19.2 cm | $\mathbf{7}$ | 27.3 m |
|  | d | 15.2 cm | $\mathbf{8}$ | a |
|  |  | 3.4 m |  |  |
|  | e | 16.7 cm |  | $\mathbf{b}$ |
|  | f | 21.1 cm | $\mathbf{1 0}$ | 588 m |

