Advanced Trigonometry - Lesson 3

# Sine Rule (Length)

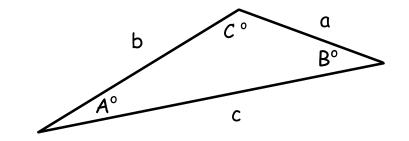
## LI

• Use the Sine Rule to find a missing length in any triangle.

## <u>SC</u>

• Use a calculator properly.

# Sine Rule



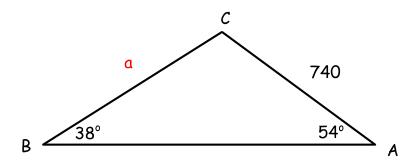
$$\frac{a}{\sin A^{\circ}} = \frac{b}{\sin B^{\circ}} = \frac{c}{\sin C^{\circ}}$$

# Strategy for Finding Missing Length

- Sketch triangle and label all sides and angles
- Write down Sine Rule
- Tick the things you know
- Solve for missing length (set calculator to degrees)

### Example 1

Calculate a to 1 d.p..



$$\frac{a}{\sin A^{\circ}} = \frac{b}{\sin B^{\circ}} = \frac{c}{\sin C^{\circ}}$$

$$A^{\circ} = 54^{\circ}$$
 ,  $a =$ 
 $B^{\circ} = 38^{\circ}$  ,  $b = 740$ 
 $C^{\circ} =$  .  $c =$ 

$$\frac{d}{\sin A^{\circ}} = \frac{D}{\sin B^{\circ}}$$

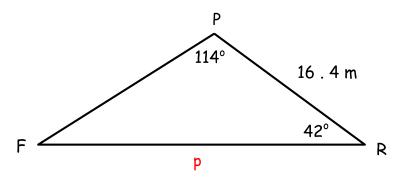
$$\frac{a}{\sin 54^{\circ}} = \frac{740}{\sin 38^{\circ}}$$

$$a = \frac{(740 \times \sin 54^{\circ})}{\sin 38^{\circ}}$$

$$a = 972.4$$

### Example 2

Calculate p to the nearest centimetre.



$$\frac{p}{\sin P^{\circ}} = \frac{f}{\sin F^{\circ}} = \frac{r}{\sin R^{\circ}}$$

$$P^{\circ} = 114^{\circ}$$
 ,  $p =$ 
 $F^{\circ} = 24^{\circ}$  ,  $f = 16.4 \text{ m}$ 
 $P^{\circ} = 42^{\circ}$   $r =$ 

$$\frac{p}{\sin P^{\circ}} = \frac{f}{\sin F^{\circ}}$$

$$\frac{p}{\sin 114^{\circ}} = \frac{16.4}{\sin 24^{\circ}}$$

$$p = \frac{(16.4 \times \sin 114^{\circ})}{\sin 24^{\circ}}$$

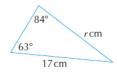
$$p = 36.835...$$

$$p = 36.84 \, m$$

#### Questions

1 Find the size of the missing side in each triangle. Give your answers to 3 significant figures.

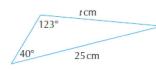
a



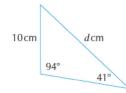
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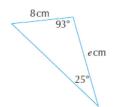
C



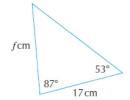
d



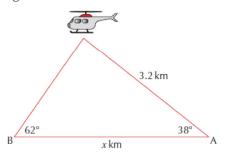
e



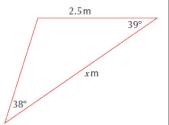
f



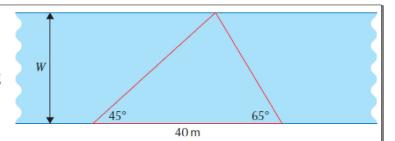
4 A helicopter flies from Helipad A. It then needs to land at Helipad B. How far apart are the two helipads? Give your answer to 3 significant figures.



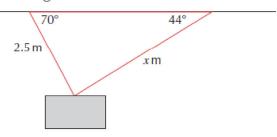
6 A metal support for a roof at a stadium is shown. Calculate the size of the beam labelled *x* to 2 significant figures.



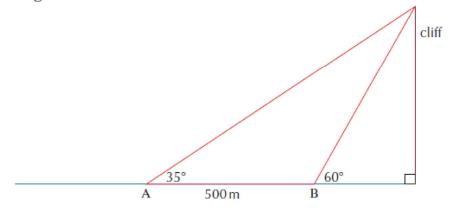
7 Two surveyors measure the distance across a river in order to build a bridge. They measure the information shown. Calculate the width W of the river giving your answer to 3 significant figures.



- 8 Jane uses a pulley system to lift a weight. The pulley is mounted to the ceiling as shown.
  - a Calculate the length of rope marked x giving your answer to 2 significant figures.
  - b The weight has to be attached to the ceiling. What distance must the weight be lifted?



10 Two ships A and B are 500 m apart. Their navigators measure the angles from the sea level to the top of the cliff. Find the height of the cliff. Give your answer to 3 significant figures.



### **Answers**

**1 a** 15.2 cm **4** 3.57 km **b** 4.85 cm **6** 4 m

c 19.2 cm 7 27.3 m

**d** 15.2 cm **8 a** 3.4 m

**e** 16.7 cm **b** 2.4 m

**f** 21.1 cm **10** 588 m