## Outcome 1

1. A line passes through the points $(1,-4)$ and $(3,-6)$.

Find the equation of this line.
2. A line makes an angle of $112^{\circ}$ with the positive direction of the x -axis, as shown in Diagram 1.

The scales on the axes are equal.
Find the gradient of the line giving your answer correct to 3 significant figures.


Diagram 1
3. A line L has equation $y=3 x-1$.

Write down the gradient of a line which is:
(a) parallel to L $\mathbf{1}$
(b) perpendicular to L .

## Outcome 2

4. The graph of a cubic $y=f(x)$ is shown in Diagram 2.

On separate diagrams sketch the graphs of:
(a) $y=-f(x)$
(b) $y=f(x-3)$


Diagram 2
5. The graphs with equations $y=4^{x}$ and $y=a^{x}$ are shown in Diagram 3.

If the graph with equation $y=a^{x}$ passes through the point $(3,27)$, find the value of $a$.


Diagram 3
6. The graphs of $y=6^{x}$ and its inverse function are shown in Diagram 4.

Write down the equation of the inverse function.


Diagram 4
7. Functions $f$ and $g$ are defined on suitable domains by $f(x)=3 x-4$ and $g(x)=x^{2}$.

Obtain an expression for $f(g(x))$.

## Outcome 3

8. Given $y=\frac{7}{x^{4}} \quad x \neq 0$, find $\frac{d y}{d x}$

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9. A sketch of the curve with equation $y=x^{2}+6 x-3$ is shown in Diagram 5.

A tangent has been drawn at $\mathrm{P}(1,4)$
Find the gradient of the tangent at $P$.

10. A curve has equation $y=\frac{1}{3} x^{3}-x^{2}-8 x+2$

Using differentiation, find the coordinates of the stationary points on this curve and determine their nature.

## Higher Mathematics

## Outcome 4

11. Every morning four fifths of the mushrooms in a bed are picked.

By the next morning another 300 are ready for picking.
There are $u_{n}$ mushrooms at the start of a particular day.
(a) Write down a recurrence relation for $u_{n+1}$ the number of mushrooms at the start of the next day.
(b) In order to be successful the grower needs at least 400 mushrooms a day.
(i) Find the limit of the sequence generated by this recurrence relation as $n \rightarrow \infty$.
(ii) In the long term, can the grower sustain the number of mushrooms needed?

