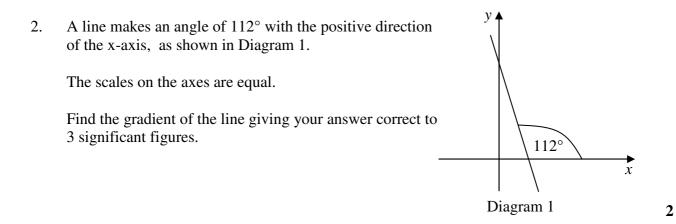
# Higher Mathematics

2

#### Outcome 1

1. A line passes through the points (1, -4) and (3, -6).

Find the equation of this line.



3. A line L has equation y = 3x - 1. Write down the gradient of a line which is:

(a)	parallel to L	1
(b)	perpendicular to L.	1

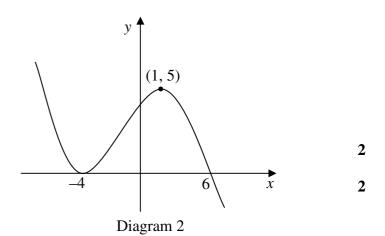
#### **Higher Mathematics**

# Outcome 2

4. The graph of a cubic y = f(x) is shown in Diagram 2.

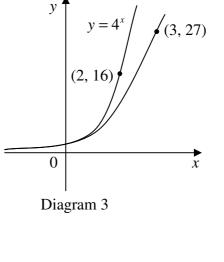
On separate diagrams sketch the graphs of:

- (a) y = -f(x)
- (b) y = f(x 3)



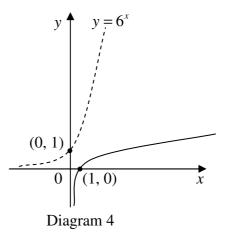
5. The graphs with equations  $y = 4^x$  and  $y = a^x$  are shown in Diagram 3.

If the graph with equation  $y = a^x$  passes through the point (3, 27), find the value of *a*.



6. The graphs of  $y = 6^x$  and its inverse function are shown in Diagram 4.

Write down the equation of the inverse function.



7. Functions *f* and *g* are defined on suitable domains by f(x) = 3x - 4 and  $g(x) = x^2$ . Obtain an expression for f(g(x)).

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1

1

# Higher Mathematics

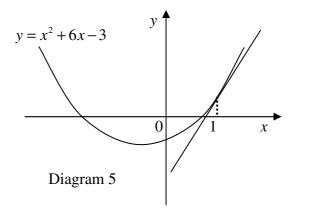
# Outcome 3

8. Given 
$$y = \frac{7}{x^4}$$
  $x \neq 0$ , find  $\frac{dy}{dx}$ 

9. A sketch of the curve with equation  $y = x^2 + 6x - 3$  is shown in Diagram 5.

A tangent has been drawn at P(1, 4)

Find the gradient of the tangent at P.



10. A curve has equation  $y = \frac{1}{3}x^3 - x^2 - 8x + 2$ 

Using differentiation, find the coordinates of the stationary points on this curve and determine their nature.

6

3

2

#### Outcome 4

11. Every morning four fifths of the mushrooms in a bed are picked. By the next morning another 300 are ready for picking.

There are  $u_n$  mushrooms at the start of a particular day.

- (a) Write down a recurrence relation for  $u_{n+1}$  the number of mushrooms at the start of the next day.
- (b) In order to be successful the grower needs at least 400 mushrooms a day.
  - (*i*) Find the limit of the sequence generated by this recurrence relation as  $n \rightarrow \infty$ .
  - (*ii*) In the long term, can the grower sustain the number of mushrooms needed?

3

1

#### End of assessment