

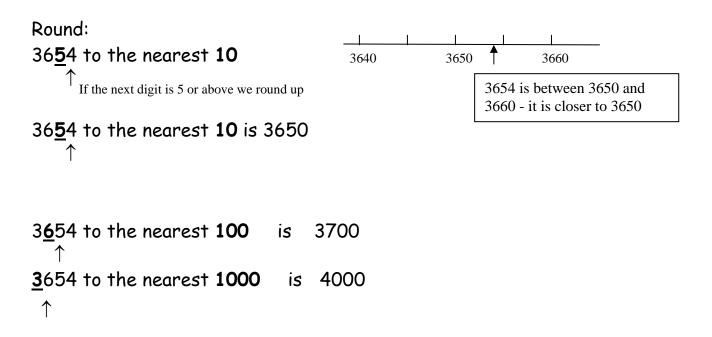
North Berwick High School August 2011

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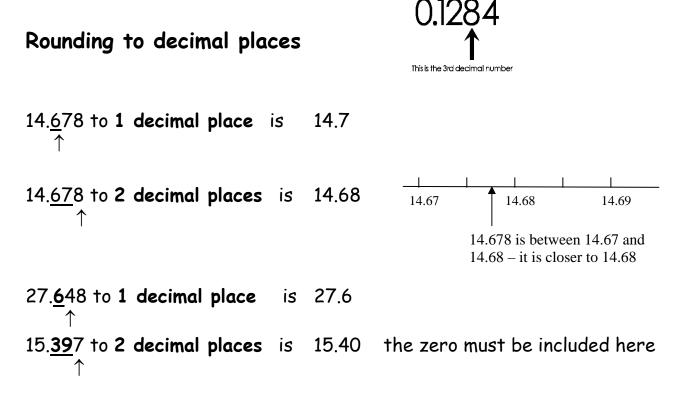
ROUNDING

Rounding whole numbers - level 2



This is the 2nd decimal number

Rounding decimals



Rounding using significant figures Level 3

2456 to 2 significant figures i	S	2500
<u>3</u> 4 600 to 1 significant figure	is	30 000
0.00 <u>26</u> 8 to 2 significant figures	is	0.0027
0.000 <u>9</u> 7 to 1 significant figure	is	0.001
0.000 <u>9</u> 7 to 2 significant figures	s is	0.0010

ADDITION Level 2 onwards

Related words : Sum, total, plus

Mental methods

To find 36 + 45

Method 1 add the tens and add the units

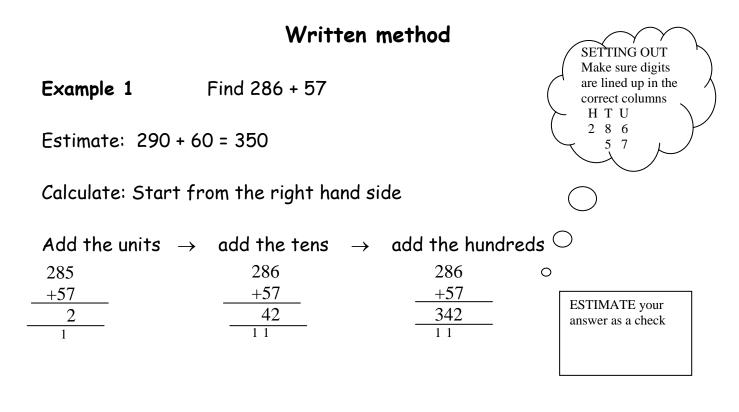
30 + 40 = 70 $6 + 5 = 11 \rightarrow 70 + 11 = 81$ so 36 + 45 = 81

Method 2 add the tens then add the units

36 + 40 = 76 76 + 5 = 81 so 36 + 45 = 81

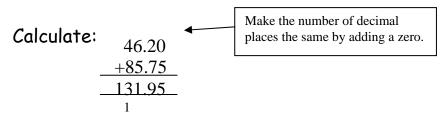
Method 3 add the next ten then subtract (in this case add 50 then subtract 5)

36 + 50 = 86 86 -5 = 81 so 36 + 45 = 81



Example 2 Find 46.2 + 85.75

Estimate: 50 + 90 = 140

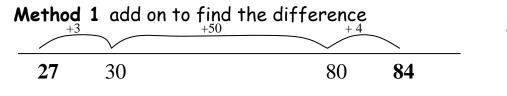


Level 2 onwards SUBTRACTION

Related words: difference, take away, minus

Mental methods

Find 84 - 27



3 + 50 + 4 = 57

so 84 - 27 = 57

Method 2 Method 3 subtract tens subtract units subtract tens then add units

84 - 20 = 64	84 - 30 = 54
64 - 7 = 57	54 + 3 = 57

Written method

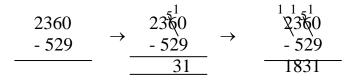
We use the decomposition method **<u>never</u>** 'borrow and pay back'!

Example 1 Find 2360 - 529

Estimate: 2400 - 500 = 1900

Calculate: Start from the right hand side

Subtract the units \rightarrow Subtract the tens \rightarrow Subtract the hundreds



9 cannot be subtracted from zero so we must change a ten for ten units.

5 cannot be subtracted from 3 so we must change a thousand for ten hundreds.

Example 2 Find 752.0 - 87.9

Estimate: 750 - 90 = 660

Calculate:

MULTIPLICATION Level 2 onwards

Mental methods

Knowledge of tables is very important, these need to be learned.

$ 1 \times 1 = 1 $	2 x 1 = 2	3 x 1 = 3	$ 4 \times 1 = 4 $	5 x 1 = 5
$ 1 \times 2 = 2 $	$2 \times 2 = 4$	$3 \times 2 = 6$	$ 4 \times 2 = 8 $	5 x 2 = 10
$ 1 \times 3 = 3 $	$2 \times 3 = 6$	$3 \times 3 = 9$	4 x 3 = 12	5 x 3 = 15
$ 1 \times 4 = 4 $	$2 \times 4 = 8$	$3 \times 4 = 12$	$4 \times 4 = 16$	5 x 4 = 20
$ 1 \times 5 = 5 $	$2 \times 5 = 10$	$3 \times 5 = 15$	$4 \times 5 = 20$	5 x 5 = 25
$ 1 \times 6 = 6 $	$2 \times 6 = 12$	$3 \times 6 = 18$	$4 \times 6 = 24$	$5 \times 6 = 30$
$ 1 \times 7 = 7 $	$2 \times 7 = 14$	3 x 7 = 21	$4 \times 7 = 28$	5 x 7 = 35
$1 \times 8 = 8$	2 x 8 = 16	$3 \times 8 = 24$	$4 \times 8 = 32$	5 x 8 = 40
$1 \times 9 = 9$	$2 \times 9 = 18$	$3 \times 9 = 27$	$4 \times 9 = 36$	5 x 9 = 45
$1 \times 10 = 10$	$2 \times 10 = 20$	$3 \times 10 = 30$	$4 \times 10 = 40$	$5 \times 10 = 50$
<u>ev 1 – e</u>	$7 \times 1 = 7$	$\left[0 \times 1 - 0\right]$	$\begin{bmatrix} 0 \\ y \\ 1 \\ z \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$	$10 \times 1 = 10$
$6 \times 1 = 6$		8 x 1 = 8	9 x 1 = 9	10 x 1 = 10
6 x 2 = 12	7 x 2 = 14	8 x 2 = 16	9 x 2 = 18	$ 10 \times 2 = 20 $
6 x 3 = 18	7 x 3 = 21	8 x 3 = 24	9 x 3 = 27	$10 \times 3 = 30$
$6 \times 4 = 24$	7 x 4 = 28	8 x 4 = 32	9 x 4 = 36	$10 \times 4 = 40$
$6 \times 5 = 30$	7 x 5 = 35	8 x 5 = 40	9 x 5 = 45	$10 \times 5 = 50$
$6 \times 6 = 36$	$7 \times 6 = 42$	8 x 6 = 48	$9 \times 6 = 54$	$10 \times 6 = 60$
$6 \times 7 = 42$	$7 \times 7 = 49$	8 x 7 = 56	$9 \times 7 = 63$	$10 \times 7 = 70$
$6 \times 8 = 48$	7 x 8 = 56	8 x 8 = 64	9 x 8 = 72	$10 \times 8 = 80$
	1	$8 \times 9 = 72$	$9 \times 9 = 81$	$10 \times 9 = 90$
	$7 \times 9 = 63$ $7 \times 10 = 70$	8 x 9 = 72 8 x 10 = 80	9 x 9 = 81 9 x 10 = 90	10 x 9 = 90 10 x 10 = 100

Find 58×3

adding gives

Method 1 multiply tens, multiply units.

50 × 3 = 150

8 × 3 = 24

58 × 3 = 174

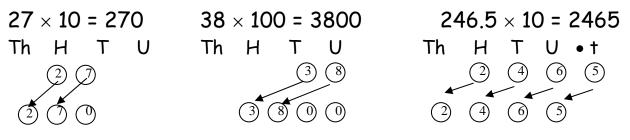
Method 2 multiply next ten then subtract

	60 × 3 = 180
	2 × 3 = 6
subtract	58 × 3 = 174



Multiplying by 10,100...

When multiplying by 10 each **digit** is moved up one place to the left When multiplying by 100 each **digit** is moved up two place to the left...



The decimal point does not move!

Written method

Example 1

Find 742 \times 8

Estimate: 742 × 10 = 7420

Calculate: Work from the right hand side Multiply units \rightarrow multiply tens \rightarrow multiply hundreds

742	742	742
x 8	_×_8_	× 8
6	36	5936
1	3 1	3 1

Multiplying by multiples of 10, 100...

To multiply by 40 multiply by 4 then multiply by 10 and so on To multiply by 400 multiply by 4 then multiply by 100 and so on

Example 1	Fir	nd 37×40	Example 2	Find	d 45.7 × 300
		37 × 4 = 148			45.7 × 3 = 137.1
		148 × 10 = 1 48	80		137.1 × 100 = 13 710
	S 0	37 × 40 = 1 48	0	S 0	45.7 × 300 = 13 710

Example 3	37 × 28				
Method 1		Me	ethod 2 Gri	d meth	od
37			20	-	
× 28		Г	_30		
296 (8×37)		20	600	140	
740 (20×37)					
1036		8	240	56	
	6	•00 +	140 + 240	+ 56 =	= 1036

Multiplying decimals level 2/3

Example Estimate Calculate	Find 32.5 × 2.8 33 × 3 = 99	
	325 × 28	Both numbers have been multiplied by 10. $10 \times 10 = 100$ so we divide
	2600	the answer by 100.
	6500	
	9100	9100 ÷ 100 = 91

0

The number of decimal places in the answer will be the same as the total number of decimal places in the question.

DIVISION

Related words : split, share, quotient

Level 1

 $65 \div 5$

Repeated subtraction from small numbers introducing division more used as a mental method.

65 - <u>50</u> ÷ 5 = **10** 15 <u>-15</u> ÷ 5 = **3** so 65 ÷ 5 = 13 0

Level 2 onwards Example 1 Find 126 ÷ 7



Example 2 Find 62.1 ÷ 3



Start dividing from the left hand side

Example 3

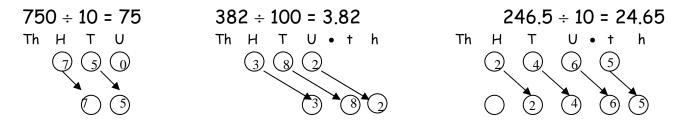
Find $86 \div 5$

$$\begin{array}{c}
 17.2 \\
 5 86.0 \\
 86.0 \\
 0$$

If there is a remainder at the end of the calculation add a decimal point and zeroes after the decimal point.

Dividing by 10, 100...

When dividing by 10 each digit is moved up one place to the left When dividing by 100 each digit is moved up two places to the left...



The decimal point does not move!

Dividing by multiples of 10, 100...

To divide by 40 divide by 4 then by 10 or by 10 then 4 and so on To divide by 400 divide by 4 then by 100 or by 100 then 4 and so on

Example 1Find $320 \div 40$ Example 2Find $60 \div 300$ $320 \div 10 = 32$ $60 \div 3 = 20$ $32 \div 4 = 8$ $20 \div 100 = 0.2$ so $320 \div 40 = 8$

Dividing by a decimal Find 360 ÷ 0.3 Level 3

 $\frac{360}{0.3} \times \frac{10}{\times 10} = \frac{3600}{3} = 1200$

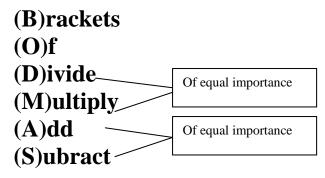
Multiply top and bottom by a multiple 10

ORDER OF OPERATIONS Level 2/3

Would the calculation 7 + 3 \times 5 lead to the answer 50 or 22?

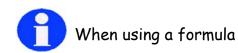
0

When there is more than one operation involved in a calculation we have a specific order to carry them out. The order can be remembered by using the mnemonic **BODMAS**.



Level 2		
Example 1	Find 50 - 10 ÷ 2 = 50 - 5 = 45	divide first then subtract
Example 2	Find 15 - 7 + 6 = 8 + 6 = 14	add and subtract are of equal importance so work left to right
Level 3		
Example 3	Find $(13 - 5) \times 7$ = 8 × 7 = 56	bracket first then multiply

FORMULAE Level 2/3



- Write down the formula
- Replace the variables with the given numbers (this is called SUBSTITUTION)
- Solve the equation

Example 1 Level 2

The formula for calculating the perimeter of a rectangle with length, I and breadth b is P = 2I + 2b.

Find the perimeter of a rectangle with length 20 centimetres and breadth 13 centimetres.

P = 2I + 2b I = 20cm , b = 13 cm P = 2 × 20 + 2 × 13 P = 40 + 26 P = 66

The perimeter is 66 cm.

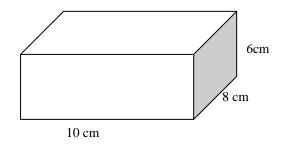
Example 2 Level 3

Find the volume of this cuboid.

 $V = I \times b \times h$

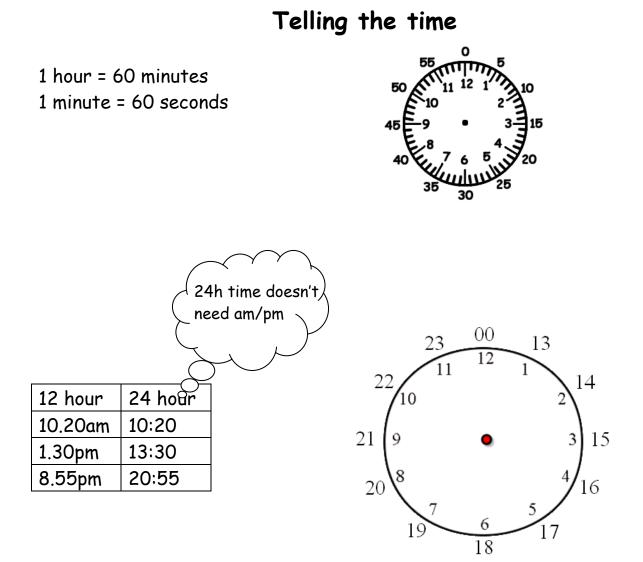
 $V = 10 \times 8 \times 6$

 $V = 480 \text{ cm}^{3}$



Things to remember

- 12 months in a year
- 30 days has September, April, June and November all the rest have 31 except February with 28 days clea and 29 in a leap year.
- 52 weeks in a year
- 365 days in a year
- 366 days in a leap year (the last two digits of a leap year are divisible by 4 or will be 00)





There are not

Finding time intervals Level 2

The length of a time interval can be found by counting on. **Example**

A film starts at 6.50pm and ends at 8.35pm. What is the length of the film.



Length of film = 10minutes + 1 hour + 35 minutes = 1 hour 45 minutes

Converting time

To convert from minutes to hours divide by 60 To convert from hours to minutes multiply by 60

Minutes	Hours
60	1
120	2
180	3

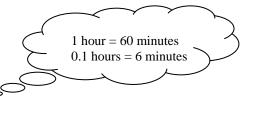
Example 2 Convert 5h 18 minutes to hours

18 minutes : 18 ÷ 60 = 0.3 hours 5 hours 18 minutes = 5.3 hours

Example 1 Convert 3.2 hours to minutes

3.2 × 60 = 192 minutes

time Level 2





Speed, distance and time level 2/3

We can use the following formulae to calculate information about a journey where the speed is constant.

 $D = S \times T$ $T = \frac{D}{S}$ $S = \frac{D}{T}$

Example A car travels for 3 hours at an average speed of 60 miles per hour, how far did it travel?

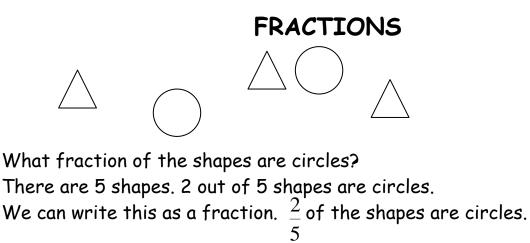
D = S × T D = 60 × 3 D = 180 miles

Example Level 3

A car travels a distance of 180 kilometres at an average speed of 50 kilometres per hour. How long did the journey take?

 $T = \frac{180}{50} = 3.6 \text{ hours} = 3 \text{ hours} 36 \text{ minutes}$ 50Remember to divide by 50
divide by 10 then by 5
Remember 0.1 hours = 6
minutes

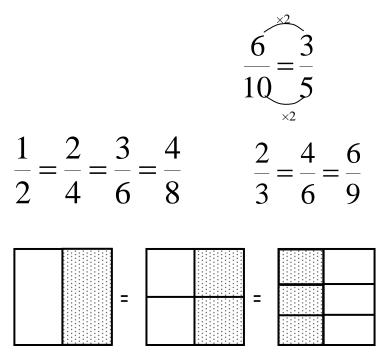


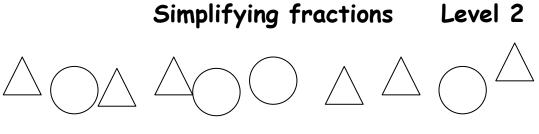


The numerator The denominator 2 5

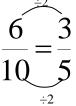
Equivalent fractions Level 2

Fractions of the same value can be written in many different forms.





In the picture above 6/10 of the shapes are triangles. This fraction may be simplified.



To simplify a fraction divide the numerator and denominator by the same number.

Finding a unit fraction Level 2

To find $\frac{1}{2}$ divide by 2, to find $\frac{1}{3}$ divide by 3, to find $\frac{1}{8}$ divide by 8... Divide by the denominator.

Example

 $\frac{1}{6}$ of $84 = 84 \div 6 = 14$

Finding a fraction Level 2

Examplefind $\frac{3}{4}$ of £36First find $\frac{1}{4}$ of £36 $\frac{1}{4}$ of £36 = £36 ÷ 4 = 9then find $\frac{3}{4}$ of £36 $\frac{3}{4}$ of £36 = £9 × 3 = £27by multiplying $\frac{1}{4}$ by 3

PERCENTAGES

Percent means out of 100 $17\% = \frac{17}{100} = 0.17$ $\frac{31}{22} \frac{33}{34} \frac{35}{36} \frac{37}{38} \frac{39}{40} \frac{40}{41} \frac{42}{42} \frac{43}{44} \frac{45}{46} \frac{47}{48} \frac{49}{49} \frac{50}{50} \frac{51}{52} \frac{53}{54} \frac{55}{55} \frac{56}{57} \frac{58}{59} \frac{59}{60} \frac{61}{61} \frac{62}{63} \frac{64}{65} \frac{66}{66} \frac{67}{68} \frac{69}{70} \frac{70}{71} \frac{72}{72} \frac{73}{74} \frac{75}{76} \frac{77}{78} \frac{79}{79} \frac{80}{89} \frac{90}{91} \frac{90}{92} \frac{93}{94} \frac{95}{96} \frac{97}{98} \frac{99}{99} \frac{100}{91} \frac{92}{93} \frac{94}{94} \frac{59}{96} \frac{97}{98} \frac{99}{99} \frac{90}{100} \frac{90}{91} \frac{92}{93} \frac{94}{94} \frac{95}{96} \frac{97}{98} \frac{99}{99} \frac{100}{91} \frac{90}{91} \frac{90}{91}$

Every percentage may be written as an equivalent fraction or decimal.

Commonly used percentages

percentage	fraction	decimal
50%	$\frac{1}{2}$	0.5
25%	1/4	0.25
75%	3/4	0.75
10%		0.10
20%	1/5	0.20
1%	1/100	0.01
331/3%	1/3	0.33
66⅔%	2/3	0.6Ġ
12 ¹ / ₂ %		0.125





Finding a percentage without a calculator

Convert to equivalent fraction level 2/3

Example 1	Example 2
Find 25% of 60	Find 33 $\frac{1}{3}$ % of 17 100
25% of 60	33 ¼ % of 17 100
= 1 /4 of 60	= 1/3 of 17 100
= 60 ÷ 4	= 17 100 ÷ 3
= 15	= 5 700

Use multiples of 10% and 1%

37% = Example 2 Level 3 Example 1 Level 2/3 30% + 7% Find 70% of 240 Find 37% of £80 10% of 240 = $\frac{1}{10}$ of 240 = 24 $10\% \text{ of } \pounds 80 = \pounds 8$ 70% of $240 = 24 \times 7 = 168$ so 30% of $\pm 80 = 3 \times \pm 8$ = £24 $1\% \text{ of } \pounds 80 = \pounds 0.80$ so 7% of £80 = 7 × £0.80 =£5.60 37% of £80 = £24 + £5.60 = £29.60

Finding a percentage with a calculator Level 3

We do not use the percentage button on a calculator. We convert the percentage to a fraction or decimal.

Example

Find 27% of £108

method 1	method 2
27% of £108	27% of £108
= 0.27 × 108	$=\frac{27}{100}$ of 108
= £29.16	= 27 ÷ 100 × 108
	= £29.16

Expressing an amount as a percentage Level 2/3

To express an amount as a percentage of a total, first write it as a fraction of the total.

Example

There were 14 adults and 6 children in a doctor's waiting room. What percentage were children?

Total number of people = 6 + 14 = 20

Fraction of children $=\frac{6}{20}=\frac{3}{10}$

Percentage of children = 30%



Calculator method

Roy scored 16 /30 in his French test. Calculate this as a percentage to the nearest 1%

 $\frac{16}{30} = 16 \div 30 = 0.53333 = 53\%$

Increasing /decreasing by a percentage Level 3

Example 1

The value of a house was £150 000. Over the next year the value increased by 18%

Method 1 Level 3 18% of £150 000 = £27 000 increase £150 000 + £27 000 = £177 000

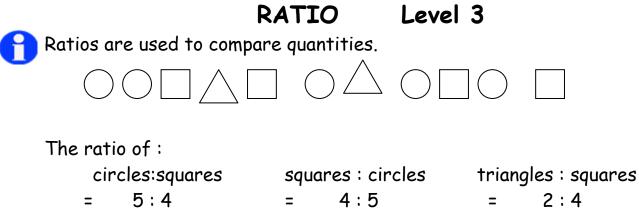
Method 2 Level 3/4 calculator 100% + 18% = 118% 118% of £150 000 =1.18 × £150 000 =£177 000

Example 2

Decrease 315 metres by 7%

Method 1 Level 3 7% of 315 = 22.05 decrease 315 - 22.05 = 292.95 metres

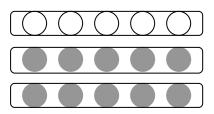
Method 2 Level 3/4 calculator 100% - 7% = 93% 93% of 315 = 0.93× 315 = 292.95 metres



2:4 = This ratio may be simplified

Simplifying a ratio

The ratio of white counters to black counters is 5:10. The counters may be grouped So we have a ratio of 1:2. This is called simplifying a ratio.



2: 6 simplifies to 1:3 (\div 2 on both sides) 6: 15 simplifies to 2:5 (÷ 3 on both sides)

Sharing in a given ratio

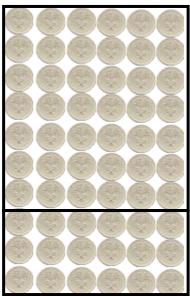
Example

Share £60 in the ratio 7:3.

7: 3 represents 7 parts to 3 parts. Total = 10 parts

 $\pounds 60 \div 10 = \pounds 6$ Find 1 part

7 parts = 7 × £6 = £42 3 parts = $3 \times \pounds 6 = \pounds 18$ $\pounds 60$ is shared into $\pounds 42$ and $\pounds 18$



Using ratio

Example

A rope is cut into two pieces in the ratio 2:5. If the shorter piece is 40 centimetres how long was the original rope?

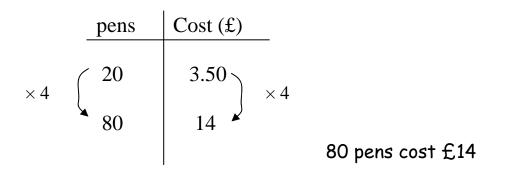
2 parts = 40 cm		Parts	Rope (cm)
1 part = 40 cm ÷ 2 = 20 cm 7 parts = 20 cm × 7 = 140 cm	You could also use a table	2	40
		1	20
The original rope was 140 centime	7	140	

PROPORTION Level 3

When two quantities are in proportion use a table to solve problems.

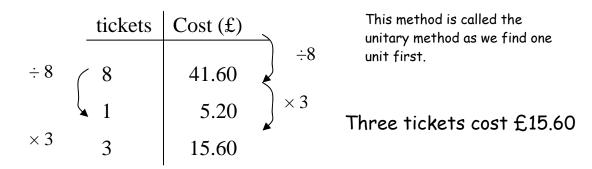
Example 1

A box of 20 pens costs £3.50. How much would 80 pens cost?



Example 2

Eight tickets to the cinema cost £41.60. Find the cost of three tickets.



INFORMATION HANDLING Frequency tables

Data may be organised in a frequency table.

The number of absences in a class is counted each day for three weeks is counted.

4	1	1	1	2
1	0	0	1	1
1	2	0	2	2

The frequency is how often something occurs. Each occurrence is represented by a tally on the frequency table.

absences	tally	frequency
0		3
1	III II	7
2		4
3		0
4		1

LINE GRAPH

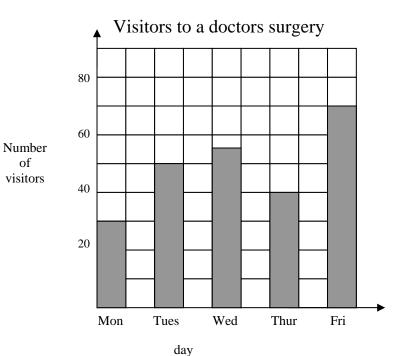
The height of a sunflower.

days	0	5	10	15	20	25	30	35	40
height	0	3	7.5	16	22	26	34	36	45

40 30 Height (cm) 20 10 20 25 30 0 5 10 15 35 40 Number of days

The height of a sunflower

- Top line of table is on the horizontal axis
- Choose a suitable scale
- Draw axes with a ruler
- Align the scales with the vertical lines not the boxes
- Label the axes and give the graph a title
- Plot data neatly and accurately



- Bar graph
 - Choose a suitable scale
 - Draw axes and bars with a ruler
 - Write the vertical scale on the lines
 - Align the labels on the horizontal axis with the bars
 - Make bars the same width
 - You may wish to leave a space between each bar
 - Label the axes and give the graph a title
 - Draw bars neatly and accurately

Mean, mode and median Level 4 (<u>not</u> a numeracy outcome)

There are three measures of average.

Mean	Total of data					
	Number of pieces of data					

Mode The most common piece of data.

Median Arrange data in order and find the middle of the data

The number of millimetres of rain measured over 8 weeks is given below.

	15	5	7	0	5	1	3	4
Mean	15 + 5 + 7 + 0 + 5 + 1 + 3 + 4							
	8							
	$=\frac{4}{8}$	$\frac{0}{8} = 5$	i					
Mode	The mode is 5							
Median	0	1	3	4	5	5	7	15
	Median = 4.5							

NOTE: If the number of pieces of data is odd the median will be a piece of data. If the number is even the median will be half way between two pieces of data.

PROBABILITY

The probability or chance of an event happening can be measured on a scale from 0 to 1

We give probabilities as a fraction or decimal.

The probability of an event happening is given by

$$probability = \frac{number of favourable outcomes}{total number of outcomes}$$

Example

There are 8 red counters and 5 blue counters in a bag. If one is chosen at random what is the probability it is red?

Probability (red) = $\frac{8}{13}$