

**AH Mathematics**

**Methods in Algebra  
and Calculus**

**Practice  
Assessment**

**1**

## Methods in Algebra and Calculus Assessment Standard 1.1

- 1 Express  $\frac{x^2 + 12}{x^3 + 6x}$  in partial fractions. (3)

## Methods in Algebra and Calculus Assessment Standard 1.2

- 2 Differentiate the following function with respect to  $x$  :

$$f(x) = e^{x^2 - 5x}. \quad (2)$$

- 3 Given  $y = \sqrt{\tan 3x}$ , find  $\frac{dy}{dx}$ . (2)

- 4 Differentiate the following functions with respect to  $x$  :

a)  $f(x) = 6x^3 \sin x$  (2)

b)  $g(x) = \frac{4x + 3}{x - 2}, x \neq 2.$  (2)

- 5 Differentiate the following function with respect to  $x$  :

$$f(x) = \sin^{-1}(4x), \quad -\frac{1}{4} \leq x \leq \frac{1}{4}. \quad (2)$$

- 6 If  $x^3 y + x y^4 = 13$ , use implicit differentiation to find  $\frac{dy}{dx}$ . (4)

- 7 The position of a golf ball with respect to a coordinate axis system, at time  $t$  seconds, is given by :

$$x = 7t, \quad y = 16t - 2t^2, \quad 0 \leq t \leq 8.$$

Find the speed of the golf ball when  $t = 3$ . (2)

### Methods in Algebra and Calculus Assessment Standard 1.3

8 Find :

a)  $\int \frac{7}{\sqrt{1 - (4x)^2}} dx$  (2)

b)  $\int \frac{3}{6x - 5} dx$  (2)

c)  $\int_0^{\frac{\pi}{24}} \sec^2 8x \, dx.$  (3)

9 Using the substitution  $u = \cos x$ , find  $\int \frac{\sin x}{\cos^3 x} dx.$  (3)

10 Using integration by parts, evaluate  $\int_1^2 x^5 \ln x \, dx.$  (4)

### Methods in Algebra and Calculus Assessment Standard 1.4

11 Find the general solution of the differential equation  $\frac{dy}{dx} = \frac{4y}{x-1}.$  (4)

12 Find the general solution, in the form  $y = f(x)$ , of the first-order linear differential equation

$$\frac{dy}{dx} + 2y = 4e^{3x}. \quad (5)$$

13 Find the particular solution of the second-order differential equation

$$\frac{d^2y}{dx^2} + 2\frac{dy}{dx} - 15y = 0 \text{ when } x = 0, y = 10 \text{ and } \frac{dy}{dx} = 2. \quad (6)$$