

2011 Mathematics

Intermediate 2 – Units 1, 2 and 3 Paper 1

Finalised Marking Instructions

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These principles describe the approach to be taken when marking Intermediate 2 Mathematics papers. For more detailed guidance please refer to the notes which are included with the Marking Instructions.

- 1 Marks must be assigned in accordance with the Marking Instructions. The main principle in marking scripts is to give credit for the skills demonstrated and the criteria met. Failure to have the correct method may not preclude a candidate gaining credit for the calculations involved or for the communication of the answer.
- 2 The answer to one part of a question, even if incorrect, must be accepted as a basis for subsequent dependent parts of the question. Full marks in the dependent part(s) may be awarded provided the question is not simplified.
- **3** The following should not be penalised:
 - working subsequent to a correct answer (unless it provides firm evidence that the requirements of the question have not been met)
 - omission or misuse of units (unless marks have been specifically allocated for the purpose in the marking scheme)
 - bad form, eg sin $x^\circ = 0.5 = 30^\circ$
 - legitimate variation in numerical values / algebraic expressions.
- 4 Solutions which seem unlikely to include anything of relevance must nevertheless be followed through. Candidates still have the opportunity of gaining one mark or more provided the solution satisfies the criteria for the mark(s).
- 5 Full credit should only be given where the solution contains appropriate working. Where the correct answer may be obtained by inspection or mentally, credit may be given, but reference to this will be made in the Marking Instructions.
- 6 In general markers will only be able to give credit for answers if working is shown. A wrong answer without working receives no credit unless specifically mentioned in the Marking Instructions. The rubric on the outside of the question papers emphasises that working must be shown.
- 7 Sometimes the method to be used in a particular question is explicitly stated; no credit should be given where a candidate obtains the correct answer by an alternative method.
- 8 Where the method to be used in a particular question is not explicitly stated, full credit must be given for alternative methods which produce the correct answer.
- 9 Do not penalise the same error twice in the same question.
- **10** A transcription error, where a number has been erroneously transcribed from the examination question, is not normally penalised except where the question has been simplified as a result.
- 11 Do not penalise inadvertent use of radians in trigonometry questions, provided their use is consistent within the question.
- 12 When multiple solutions are presented by the candidate and it is not clear which is intended to be the final one, mark all attempts and award the lower mark.

Practical Details

The Marking Instructions should be regarded as a working document and have been developed and expanded on the basis of candidates' responses to a particular paper. While the guiding principles of assessment remain constant, details can change depending on the content of a particular examination paper in a given year.

- 1 Each mark awarded in a question is referenced to one criterion in the marking scheme by means of a bullet point.
- 2 Where a candidate has scored zero marks for any question attempted, "0" should be shown against the answer in the place in the margin.
- 3 Where a marker wishes to indicate how s/he has awarded marks, the following should be used:
 - (a) Correct working should be ticked, \checkmark .
 - (b) Where working subsequent to an error is followed through, if otherwise correct and can be awarded marks, it should be marked with a crossed tick, X.
 - (c) Each error should be underlined at the point in the working where it first occurs.
- 4 Do not write any comments, words or acronyms on the scripts.

Mathematics Intermediate 2: Paper 1, Units 1, 2 and 3 (non-calc)

| Question | Marking Scheme | Illustrations of evidence for awarding |
|----------|---|--|
| No | Give 1 mark for each • | a mark at each • |
| 1 (a) | Ans: (i) $Q_2 = 6.5$ (ii) $Q_1 = 5$ (iii) $Q_3 = 9$ | |
| | \bullet^1 process: calculate the median | • ¹ $Q_2 = 6.5$ |
| | \bullet^2 process: calculate the lower quartile | • ² $Q_1 = 5$ |
| | \bullet^3 process: calculate the upper quartile | • 3 Q ₃ = 9 |
| | | 3 marks |

NOTES:

1. An incorrect answer for the median must be followed through with the possibility of awarding 2/3.

| (b) | Ans: boxplot | |
|-----|---|--|
| | | |
| | | |
| | 0 5 10 15 | |
| | • ¹ communicate: correct endpoints | \bullet^1 endpoints at 0 and 15 |
| | \bullet^2 communicate: correct box | • ² box showing Q_1, Q_2, Q_3 |
| | | 2 marks |

NOTES:

1. The boxplot must be drawn to a reasonable scale.

| (c) | Ans: The trains are not as late as the buses <u>or</u> the trains are more reliable. | |
|-----|--|---|
| | • ¹ communicate: make a valid comment | • ¹ a valid comment 1 mark |

NOTES:

- For a statement which is factually incorrect, award 0/1. eg The bus took longer than the train (refers to speed not lateness). The train was late less often than the bus (refers to number of times late rather than number of minutes late).
- 2. A valid statement must mention train(s) and/or bus(es).
- 3. Where two contradictory statements are made, award 0/1.

| Question No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|----------------|---|---|
| 2 | Ans: $6x^2 - 12x - 14$ | |
| | • ¹ process: start to multiply out brackets | • 1 evidence of 2 correct terms (eg $6x^2 + 4x$) |
| | • ² process: complete the process of multiplying out brackets | • ² $6x^2 - 21x + 4x - 14$ |
| | • ³ process: collect like terms which must include a term in x^2 | • ³ $6x^2 - 12x - 14$ |
| | | 3 marks |
| NOTES: | | |
| 3 | Ans: 138° | |
| | • ¹ process: calculate size of angle BEP | • ¹ 90° |
| | • ² process: calculate size of angle EPC or angle EPB | • ² 42° or 48° |
| | • ³ process: calculate size of angle EPR | • ³ 138° |
| | | 3 marks |
| NOTES: | | |
| 1. For | r a correct answer without working | award 0/3 |
| 2. For | r marks 1 and 2 angles need not be stated explicitl | y. They may be marked on a diagram. |
| | efore awarding the second mark, markers must be clear that the 42° and 48° refer to angles PC and EPB respectively. | |
| 4. For | r the final mark to be awarded the size of angle EF | PR must be stated explicitly. |

| Question No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|----------------|---|--|
| 4 | Ans: $3\sqrt{8}$ with evidence | |
| | • ¹ process: manipulate one of the four terms | • ¹ evidence (see NOTE 1) |
| | • ² process/communicate: manipulate a different term <u>and</u> state conclusion | • ² $3\sqrt{8}$ with evidence |
| | conclusion | 2 marks |

NOTES:

- 1. The first mark may be awarded for one of the following: $2\sqrt{6} = \sqrt{4} \times \sqrt{6} = \sqrt{24}$ $\sqrt{2} \times \sqrt{12} = \sqrt{24}$ $\sqrt{2} \times \sqrt{12} = \sqrt{2} \times \sqrt{4 \times 3} = 2\sqrt{6}$ $3\sqrt{8} = \sqrt{9} \times \sqrt{8} = \sqrt{72}$ $3\sqrt{8} = 3\sqrt{4 \times 2} = 6\sqrt{2}$ $\sqrt{24} = \sqrt{2} \times \sqrt{12}$ $\sqrt{24} = \sqrt{4 \times 6} = 2\sqrt{6}$
- 2. For an answer of " $3\sqrt{8}$ because the other three are equal", without working, award 0/2

| 5 | Ans: Proof | |
|--|---|---|
| | \bullet^1 strategy: know to use cosine rule | • ¹ evidence |
| | • ² process: substitute correctly into formula | • ² $\cos B = \frac{6^2 + 3^2 - 5^2}{2 \times 6 \times 3}$ |
| | • ³ process: complete proof | • ³ $\cos B = \frac{5}{9}$ |
| | | 3 marks |
| NOTES: 1. The third mark can only be awarded if it has been shown that $\cos B = \frac{20}{36}$. | | |

| Question No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|----------------|---|---|
| 6. | Ans: 27 | |
| | • ¹ process: start to evaluate | \bullet^1 $\sqrt{9^3}$ |
| | \bullet^2 process: complete evaluation | • ² 27 |
| | | 2 marks |
| NOTES: | | |
| 1. For | a correct answer without working, award 2/2. | |
| 7 | Ans: $a = 5, b = 4$ | |
| | • ¹ communicate: state value of a | \bullet^1 $a=5$ |
| | • ² communicate: state value of b | $\bullet^2 b=4$ |
| | | 2 marks |
| NOTES: | | |
| 1. Ac | $\operatorname{cept} y = 5 \cos 4x^{\circ}$ | |
| 2. For | a = 4, b = 5 | award 1/2 |
| 8 | Ans: y 0 x x x x x x x x | • ¹ line with upward slope drawn on |
| | upward sloping line • ² interpret: realise $c < 0$ represents a | graph ² line drawn with v-intercept below |
| | • ² interpret: realise $c < 0$ represents a y-intercept below origin | • ² line drawn with y-intercept below origin |
| | | 2 marks |
| NOTES: | | |

| Question No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|----------------|---|--|
| 9 (a) | Ans: $(x-7)(x+3)$ | |
| | • ¹ process: factorise trinomial expression | \bullet^1 one correct factor |
| | | |
| | • ² process: complete factorisation | \bullet^2 second correct factor |
| | | 2 marks |
| NOTES: | | |
| 1. For | r the following answers award 1/2: | |
| | (x+7)(x-3) | |
| | (x+21)(x-1) (x-21)(x+1) | |
| | | |
| (b) | Ans: 7, -3 | |
| | \bullet^1 communicate: state roots of equation | • ¹ 7, -3 |
| | | 1 mark |
| NOTES: | 1 | 1 |
| | here a candidate uses the quadratic formula, this n | nark is not available. |
| (c) | Ans: (2, -25) | |
| | • ¹ strategy: find <i>x</i> -coordinate of turning point | • ¹ $x=2$ |
| | • ² process: replace $x = 2$ into $y = x^2 - 4x - 21$ | $\bullet^2 \qquad y = 2^2 - 4 \times 2 - 21$ |
| | • ³ process: complete coordinates of turning point | • ³ (2, -25) |
| | | 3 marks |
| NOTES: | | |
| 1. Inco | orrect roots in part (b) must be followed through t | o give the possibility of awarding full |
| | dit in part (c). | |
| 2. Wh | ere the <i>x</i> coordinate of the turning point has been | calculated incorrectly, the second and |

2. Where the *x* coordinate of the turning point has been calculated incorrectly, the second and third marks are still available only where full working has been shown eg for an answer of (4, -21), without working, award 0/3.

| Question No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|----------------|---|--|
| 10 | Ans: $\frac{4}{5}$ • ¹ communicate: state value of cos a° | • $\frac{4}{5}$ |
| | | 1 mark |
| NOTES: | | |

TOTAL MARKS FOR PAPER 1 30

[END OF MARKING INSTRUCTIONS]



2011 Mathematics

Intermediate 2 – Units 1, 2 and 3 Paper 2

Finalised Marking Instructions

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Question **Marking Scheme** Illustrations of evidence for awarding No Give 1 mark for each • a mark at each • 1. Ans: -9/10 \bullet^1 \bullet^1 -9/10 process: calculate gradient 1 mark **NOTES:** 2. Ans: £147 900 \bullet^1 \bullet^1 strategy: know how to increase by 3.15% $\times 1.0315$ •² \bullet^2 strategy: know how to calculate expected 134750×1.0315^{3} value •3 •3 process: carry out all calculations correctly 147 889.2038 within a valid strategy •⁴ •⁴ process: round answer to 4 significant 147 900 figures 4 marks **NOTES:** For an answer of £147 900, with or without working $(\checkmark \checkmark \checkmark \checkmark)$ award 4/4 1. 2. For an answer of £147 900.00, with or without working, $(\checkmark \checkmark \checkmark \checkmark)$ award 3/4 3. For an answer of £147 889.2, with or without working $(\checkmark \checkmark \checkmark \checkmark)$ award 3/4 Where an incorrect percentage has been used, the working must be followed 4. through to give the possibility of awarding 3/4eg for an answer of £122 400 (134 750 \times 0.9685³), with working For an answer of £417 000 (134 750 \times 1.0315 \times 3), with working $(\checkmark X X \checkmark)$ award 2/4 5. For an answer of £147 500 (134 750 + $3 \times 0.0315 \times 134$ 750), 6. with working $(\checkmark X X \checkmark)$ award 2/4 7. For an answer of £12 730 (134 750 \times 0.0315 \times 3), with working $(X \times X \checkmark)$ award 1/4

Mathematics Intermediate 2: Paper 2, Units 1, 2 and 3

| Question | Marking Scheme | Illustrations of evidence for awarding |
|----------|---|---|
| No | Give 1 mark for each • | a mark at each • |
| 3. | Ans: $r = \sqrt{\frac{A}{4\pi}}$ | |
| | • ¹ process: start to rearrange formula | • ¹ $r^2 = \frac{A}{4\pi}$ |
| | • ² process: make r the subject | • ¹ $r^2 = \frac{A}{4\pi}$ • ² $r = \sqrt{\frac{A}{4\pi}}$ |
| | | 2 marks |
| NOTES: | | |
| 1. For | a correct answer without working | award 2/2 |
| 2. Th | e second mark is available for taking the square ro | bot of an expression for r^2 |
| 3. For | r an answer of $r = \frac{\sqrt{A}}{4\pi}$, with or without working, | award 1/2 |
| | t answers such as $= \sqrt{\frac{A}{\frac{4}{\pi}}}$ | |
| | $=\sqrt{\frac{A \div 4}{\pi}}$ | |
| | $=\sqrt{A\div 4\div\pi}$ | award 1/2 |
| | | |

| Question No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|------------------------------|--|--|
| 4. (a) | Ans: 106 cubic metres ¹ process: substitute correctly into volume formula for cylinder ² process: calculate volume of cylinder | • $\pi \times 1.5^2 \times 15$ • 106 (m ³) 2 marks |
| NOTES: 1. <i>A</i> | Accept variations in volume due to variations in the | value of π |
| (b) | Ans: 17.4 metres ¹ strategy: know how to find expression for volume of cone ² strategy: know to equate volume of cone with 5.7 ³ process: calculate total height of The Pencil | • $\frac{1}{3} \times \pi \times 1 \cdot 5^2 \times h$ • $\frac{1}{3} \times \pi \times 1 \cdot 5^2 \times h = 5 \cdot 7$ • $\frac{1}{3} \times \pi \times 1 \cdot 5^2 \times h = 5 \cdot 7$ • $\frac{1}{3} \times \pi \times 1 \cdot 5^2 \times h = 5 \cdot 7$ • $\frac{1}{3} \times \pi \times 1 \cdot 5^2 \times h = 5 \cdot 7$ • $\frac{1}{3} \times \pi \times 1 \cdot 5^2 \times h = 5 \cdot 7$ |
| NOTES: | l | |

| Question No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|----------------|---|--|
| 5. | Ans: 25.1 square centimetres | |
| | • ¹ strategy: know to express sector as fraction of circle | • ¹ $\frac{54}{360}$ |
| | • ² strategy: know how to find area of sector | $\bullet^2 \frac{54}{360} \times \pi \times 7.3^2$ |
| | • ³ process: correctly calculate area of sector | • ³ 25.1 (sq cm) |
| | | 3 marks |
| NOTES: | I | |
| 1. Ac | cept variations in π , disregard premature or incorre | ect rounding of $\frac{54}{360}$ |
| 2. Foi | $\frac{54}{360} \times \pi \times 2 \times 7.3$ leading to 6.9 | $(\checkmark \checkmark \checkmark)$ award 2/3 |
| 3. Foi | r the award of the final mark, calculations must invo | plve a fraction and π |

| - | estion No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|-----|----------------|---|--|
| 6. | (a) (i) | (i) Ans: $\overline{x} = 41$ (ii) Ans: $s = 2 \cdot 1$ • 1 process: calculate the mean | • ¹ 41 |
| | (ii) | • ¹ process: calculate $(x - \overline{x})^2$ | 1 mark • ¹ 4, 4, 0, 1, 4, 9 |
| | | \bullet^2 process: substitute into formula | $\bullet^2 \sqrt{\frac{22}{5}}$ |
| | | • ³ process: calculate standard deviation | • ³ 2·1 (disregard rounding) 3 marks |
| NOT | TES: | | |
| 1. | For u | use of alternative formula in part (a) (ii), award mar | ks as follows |
| | $ullet^1$ | process: calculate $\sum x$ and $\sum x^2$ | • ¹ 246 and 10 108 |
| | • ² | process: substitute into formula | • ² $\sqrt{\frac{10108 - 246^2/6}{5}}$ |
| | • ³ | process: calculate standard deviation | • ³ 2·1 |
| 2. | For c | orrect answer, without working | award 0/3 |
| 6. | (b) | Ans: Yes, with reasons covering both conditions | |
| | | • ¹ communicate: compare mean with the tolerance | • ¹ Yes, because 41 is between 38 and 42 |
| | | • ² communicate: compare std dev with tolerance | • ² Yes, because 2.1 is less than 3 |
| | | | 2 marks |
| NOT | TES: | | |
| 1 | "Ye "Ye | not accept: s, because the mean is 41 which is in the range 40 s, because the mean is between 38 and 42." s, because the standard deviation is less than 3." | ± 2." |
| 2 | | because of a wrong answer in part (a), the response ress both conditions to access 2 marks | e to part (b) is "No", the candidate must |

| Question No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|---|--|--|
| 7. (a) | Ans: $24x + 6y = 60$ • ¹ interpret: interpret the text | • 1 24 <i>x</i> + 6 <i>y</i> = 60 1 mark |
| (b) | Ans: 20x +10y = 40 •¹ interpret: interpret the text | • $1 20x + 10y = 40$ 1 mark |
| (c) | Ans: 25 points ¹ strategy: know to solve system of equations ² process: follow a valid strategy through to produce a value for <i>x</i> and <i>y</i> ³ process: correct value for <i>x</i> and <i>y</i> ⁴ process: calculate 17<i>x</i> + 13<i>y</i> | • ¹ evidence of scaling • ² a value for x and y • ³ $x = 3, y = -2$ • ⁴ 25 4 marks |
| aw 2. Any 3. Wh 24 <i>x</i> 20 <i>x</i> | orrect equations in parts (a) and/or (b) must be follo arding 4/4. v valid strategy must involve the use of two equatio ere a candidate writes - 6y = 60 for part (a), - 10y = 40 for part (b), leading to $x = 3$, $y = 2a final answer of 25,award 0/1$ for part (a) award 1/1 for part (b) award 4/4 for part (c) | ns. |
| equ equ ie | here the correct values for x and y have been obtained nations, marks are available only if both values have nations $24 \times 3 + 6 \times (-2) = 60$ $20 \times 3 + 10 \times (-2) = 40$ | ÷ |

- ie $24 \times 3 + 6 \times (-2) = 60$ $20 \times 3 + 10 \times (-2) = 40$ leading to x = 3, y = -217x + 13y = 25
- 5. For a correct answer, without working

award 4/4 award 0/4

| Question No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|------------------|---|--|
| 8. | Ans: $\frac{3}{x-5}$ • ¹ process: factorise numerator • ² process: simplify expression correctly | • $3(x-5)$ • $\frac{3}{x-5}$ 2 marks |
| NOTES: 1. For | a correct answer without working, award 2/2 | |
| 9. | Ans: $\frac{3-x}{x(x+1)}$ • ¹ process: state a valid common denominator | • ¹ any valid denominator |
| | • ² process: find correct numerator of equivalent fraction | \bullet^2 both numerators correct |
| | • ³ process: state answer in simplest form | • ³ $\frac{3-x}{x(x+1)}$ 3 marks |
| NOTES: | | |
| | his question working subsequent to a correct answer $\frac{3(x+1)-4x}{x(x+1)} = \frac{3-x}{x^2+1}$ | er should be ignored. award $3/3 (\checkmark \checkmark \checkmark)$ |
| 3. For | $\frac{3(x+1)-4x}{x^2+1} = \frac{3-x}{x^2+1}$ | award 2/3 (X \checkmark) |
| 10. | Ans: $x = 76$ and $x = 256$ • ¹ process: solve equation for $\tan x^{o}$ • ² process: find one value for x • ³ process: find second value for x | • $\tan x^{\circ} = 4$ or equivalent • 76 • 3256 3 marks |
| | ere tan x° is calculated incorrectly, the working mussibility of awarding 2/3 | ust be followed through with the |
| 2. For | a correct answer, without working, | award 0/3 |

| Question No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|-----------------------|--|---|
| 11. | Ans: 0·2, 1·6 | |
| | • ¹ strategy: know to use quadratic formula | • ¹ evidence |
| | • ² process: correct substitution in formula | $\bullet^2 \qquad \frac{7 \pm \sqrt{(-7)^2 - 4 \times 4 \times 1}}{2 \times 4}$ |
| | • ³ process: calculate $b^2 - 4ac$ correctly | • ³ 33 |
| | • ⁴ process: state both values of x correct to one decimal place | • 4 0.2, 1.6 |
| | | 4 marks |
| NOTES: 1. W | where $b^2 - 4ac$ is calculated incorrectly, the fourth matrix | ark is available only if $b^2 - 4ac > 0$. |
| 1. W | There $b^2 - 4ac$ is calculated incorrectly, the fourth matrix or a correct answer without working Ans: 21 centimetres | ark is available only if $b^2 - 4ac > 0$. award 0/4. |
| 1. W 2. Fo | or a correct answer without working | |
| 1. W 2. Fo | or a correct answer without working Ans: 21 centimetres • ¹ process: state the size of \angle BOD and | award 0/4. |
| 1. W 2. Fo | Ans: 21 centimetres •¹ process: state the size of ∠ BOD and recognise isosceles triangle | \bullet^1 82° plus evidence of isos. triangle |
| 1. W 2. Fo | Ans: 21 centimetres •¹ process: state the size of ∠ BOD and recognise isosceles triangle •² process: state the size of ∠ ADC •³ strategy: know to use the cosine rule in | \bullet^{1} 82° plus evidence of isos. triangle \bullet^{2} 131° |
| 1. W 2. Fo | Ans: 21 centimetres •1 process: state the size of ∠ BOD and recognise isosceles triangle •2 process: state the size of ∠ ADC •3 strategy: know to use the cosine rule in triangle ADC | award 0/4. • 1 82° plus evidence of isos. triangle • 2 131° • 3 evidence • $d^{2} = 9^{2} + 14^{2} - $ |

NOTES:

- 1. Angle BOD may not be explicitly stated, it may be marked in a diagram and, when evidence of the isosceles triangle is also present, can be awarded the first mark.
- 2. Angle ADC may not be explicitly stated. It may be marked in a diagram and can be awarded the second mark.
- 3. Disregard errors due to premature rounding.

| Question No | Marking Scheme Give 1 mark for each • | Illustrations of evidence for awarding a mark at each • |
|----------------|---|--|
| 13. | Ans: 25.1 millimetres | |
| | • ¹ strategy: marshall facts and recognise right-angle | \bullet^1 110 70 |
| | • ² strategy: use Pythagoras Theorem or equivalent | • ² $x^2 = 110^2 - 70^2$ |
| | • ³ process: calculate third side correctly | • ³ 84.9 |
| | • ⁴ process: state height | • ⁴ 25.1 (mm) |
| | | 4 marks |

NOTES:

- 1. The final mark is for subtracting a calculated value from the radius.
- 2. Some common answers (with working):

| $\sqrt{110^2 + 70^2} = 130 \cdot 4$ | award 2/4 |
|---|-----------|
| $110 - \sqrt{140^2 - 110^2} = 23 \cdot 4$ | award 2/4 |

3. Where a candidate assumes an angle of 45° in the right-angled triangle, only the first and fourth marks are available.

| | Give 1 mark for each • Ans: Complete proof • ¹ strategy: know to replace $1 - \sin^2 A$ by | a mark at each • |
|--------|---|--|
| | • strategy: know to replace $1 - \sin^2 A$ by | . 2 . |
| • | stategy into a to replace i shi ii oy | • 2 • |
| | $\cos^2 A$ | $\bullet^1 \frac{\sin^2 A}{\cos^2 A}$ |
| • | • ² strategy: know to use $\frac{\sin A}{\cos A} = \tan A$ to | \bullet^2 complete proof |
| | complete proof | 2 marks |
| NOTES: | | |
| 1. For | $\frac{\sin^2 A}{1-\sin^2 A} = \tan^2 A$ | |
| | $\frac{\sin^2 A}{\cos^2 A} = \tan^2 A$ | |
| | $\tan^2 A = \tan^2 A$ | award 2/2 |
| For | $\frac{\sin^2 A}{1-\sin^2 A} = \tan^2 A$ | |
| | $\frac{\sin^2 A}{\cos^2 A} = \tan^2 A$ | award 1/2 |

TOTAL MARKS FOR PAPER 2 50

[END OF MARKING INSTRUCTIONS]