2009 Mathematics

Intermediate 2 – Units 1, 2 and 3 Paper 1

Finalised Marking Instructions

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General Marking Principles

These principles describe the approach to be taken when marking Intermediate 2 Mathematics papers. For more detailed guidance please refer to the notes which are included with the Marking Instructions.

1 Marks must be assigned in accordance with the Marking Instructions. The main principle in marking scripts is to give credit for the skills demonstrated and the criteria met. Failure to have the correct method may not preclude a candidate gaining credit for the calculations involved or for the communication of the answer.

2 The answer to one part of a question, even if incorrect, must be accepted as a basis for subsequent dependent parts of the question. Full marks in the dependent part(s) may be awarded provided the question is not simplified.

3 The following should not be penalised:
   - working subsequent to a correct answer (unless it provides firm evidence that the requirements of the question have not been met)
   - omission or misuse of units (unless marks have been specifically allocated for the purpose in the marking scheme)
   - bad form, eg \( \sin x^\circ = 0.5 = 30^\circ \)
   - legitimate variation in numerical values / algebraic expressions.

4 Solutions which seem unlikely to include anything of relevance must nevertheless be followed through. Candidates still have the opportunity of gaining one mark or more provided the solution satisfies the criteria for the mark(s).

5 Full credit should only be given where the solution contains appropriate working. Where the correct answer may be obtained by inspection or mentally, credit may be given, but reference to this will be made in the Marking Instructions.

6 In general markers will only be able to give credit for answers if working is shown. A wrong answer without working receives no credit unless specifically mentioned in the Marking Instructions. The rubric on the outside of the question papers emphasises that working must be shown.

7 Sometimes the method to be used in a particular question is explicitly stated; no credit should be given where a candidate obtains the correct answer by an alternative method.

8 Where the method to be used in a particular question is not explicitly stated, full credit must be given for alternative methods which produce the correct answer.

9 Do not penalise the same error twice in the same question.

10 Do not penalise a transcription error unless the question has been simplified as a result.

11 Do not penalise inadvertent use of radians in trigonometry questions, provided their use is consistent within the question.
Practical Details

The Marking Instructions should be regarded as a working document and have been developed and expanded on the basis of candidates’ responses to a particular paper. While the guiding principles of assessment remain constant, details can change depending on the content of a particular examination paper in a given year.

1. Each mark awarded in a question is referenced to one criterion in the marking scheme by means of a bullet point.

2. Where a candidate has scored zero marks for any question attempted, “0” should be shown against the answer in the place in the margin.

3. Where a marker wishes to indicate how s/he has awarded marks, the following should be used:

   (a) Correct working should be ticked, ✓.

   (b) Where working subsequent to an error is followed through, if otherwise correct and can be awarded marks, it should be marked with a crossed tick, ✗.

   (c) Each error should be underlined at the point in the working where it first occurs.

4. Do not write any comments, words or acronyms on the scripts.
### Mathematics Intermediate 2: Paper 1, Units 1, 2 and 3 (non-calc)

<table>
<thead>
<tr>
<th>Question No</th>
<th>Marking Scheme</th>
<th>Illustrations of evidence for awarding a mark at each •</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 (a)</td>
<td>Ans:</td>
<td>•1 process: start to draw dotplot  •1 evidence (see note 1)</td>
</tr>
<tr>
<td></td>
<td>Ans:</td>
<td>•2 process: complete dotplot  •2 complete dotplot</td>
</tr>
</tbody>
</table>

**NOTES:**

1. Minimum acceptable evidence for the award of the first mark

<table>
<thead>
<tr>
<th>0 1 2 3 4 5</th>
</tr>
</thead>
<tbody>
<tr>
<td>•</td>
</tr>
</tbody>
</table>

(b) **Ans:** A

<table>
<thead>
<tr>
<th>0 1 2 3 4 5</th>
</tr>
</thead>
<tbody>
<tr>
<td>•1 communicate: state correct letter</td>
</tr>
</tbody>
</table>

**NOTES:**

1. Accept “skewed to the right”.

---

**Page 4**
<table>
<thead>
<tr>
<th>Question No</th>
<th>Marking Scheme</th>
<th>Illustrations of evidence for awarding a mark at each •</th>
</tr>
</thead>
</table>
| 2 | Ans: \( y = 3x - 1 \) | • 1 process: find gradient  
• 2 process: state \( y \)-intercept or \( c \) in \( y = mx + c \)  
• 3 communicate: state correct equation of line  
\[
\begin{align*}
\text{• 1} & \quad m = 3 \text{ (or equivalent)} \\
\text{• 2} & \quad c = -1 \\
\text{• 3} & \quad y = 3x - 1
\end{align*}
\] |

3 marks |

**NOTES:**

1. For correct answer without working award 3/3
2. For \( y = 3x \) award 1/3
3. Where \( m \) and/or \( c \) are incorrect the working must be followed through to give the possibility of awarding 1/3 or 2/3
4. If the equation is stated incorrectly and there is no working, 1/3 can be awarded for correct gradient or correct \( y \)-intercept
5. For an incorrect equation (ie both \( m \) and \( c \) incorrect) without working, eg \( y = -x + 3 \) award 0/3

| 3 | Ans: \( (x - 8)(x + 3) \) | • 1 process: start to factorise  
• 2 process: complete factorisation  
\[
\begin{align*}
\text{• 1} & \quad \text{one correct factor} \\
\text{• 2} & \quad (x - 8)(x + 3)
\end{align*}
\] |

2 marks |

**NOTES:**

1. For the following answers award 1/2

\[
\begin{align*}
(x - 24)(x + 1) \\
(x + 24)(x - 1) \\
(x - 12)(x + 2) \\
(x + 12)(x - 2) \\
(x + 8)(x - 3) \\
(x - 6)(x + 4) \\
(x + 6)(x - 4)
\end{align*}
\]
<table>
<thead>
<tr>
<th>Question No</th>
<th>Marking Scheme</th>
<th>Illustrations of evidence for awarding a mark at each •</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>Ans: (2x^3 + 7x^2 - 16x - 5)</td>
<td>• 1 process: start to multiply out brackets&lt;br&gt; • 2 process: complete the process of multiplying out brackets correctly&lt;br&gt; • 3 process: collect like terms which must include (x^3) term</td>
</tr>
</tbody>
</table>

**NOTES:**

1. Where candidates have attempted to ‘simplify’ beyond the correct answer, the 3rd mark is not available.

<table>
<thead>
<tr>
<th>5 (a)</th>
<th>Ans: (i) 58·5 (ii) 11</th>
<th>Illustrations of evidence for awarding a mark at each •</th>
</tr>
</thead>
<tbody>
<tr>
<td>(i)</td>
<td>• 1 process: calculate median</td>
<td>• 1 (58·5)</td>
</tr>
<tr>
<td>(ii)</td>
<td>• 1 process: calculate lower quartile&lt;br&gt; • 2 process: calculate upper quartile&lt;br&gt; • 3 process: calculate SIQR</td>
<td>• 1 (45)&lt;br&gt; • 2 (67)&lt;br&gt; • 3 (11)</td>
</tr>
</tbody>
</table>

**NOTES:**

1. An incorrect answer for the median must be followed through with the possibility of awarding full marks for part (ii).
<table>
<thead>
<tr>
<th>Question No</th>
<th>Marking Scheme</th>
<th>Illustrations of evidence for awarding a mark at each</th>
</tr>
</thead>
<tbody>
<tr>
<td>(b) Ans: In December, the marks (on average) are better and less spread out.</td>
<td>• 1 communicate: make a valid comment</td>
<td>• 1 comment</td>
</tr>
<tr>
<td></td>
<td>• 2 communicate: make a second valid comment</td>
<td>• 2 comment</td>
</tr>
</tbody>
</table>

**NOTES:**

1. For an answer like “marks are better and less spread out” award 0/2
<table>
<thead>
<tr>
<th>Question No</th>
<th>Marking Scheme</th>
<th>Illustrations of evidence for awarding a mark at each</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>Ans: Any value for $a$ such that $270 &lt; a &lt; 360$.</td>
<td>$\bullet^1$ any size between 270 and 360</td>
</tr>
<tr>
<td></td>
<td>$\bullet^1$ communicate: state possible size of $a$</td>
<td>$\bullet^1$ any size between 270 and 360</td>
</tr>
</tbody>
</table>

NOTES:

7  
Ans: $-1$  
$\bullet^1$ strategy: know how to find gradient  
$\bullet^1$ $y = -x + 5$ or correct graph  
$\bullet^2$ $-1$  

NOTES:  
1. Correct answer without working award 2/2  
2. For an answer of $m = -1, c = 5$, with or without working award 1/2
<table>
<thead>
<tr>
<th>Question No</th>
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</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>Ans: The graph of ( y = 4 \cos 2x^\circ ) drawn from 0° to 360°</td>
<td><img src="image" alt="Graph" /></td>
</tr>
<tr>
<td></td>
<td>• (^1) process: know the max = 4 and min = -4</td>
<td>• (^1) evidence from graph</td>
</tr>
<tr>
<td></td>
<td>• (^2) process: show that there are 2 cycles in 360°</td>
<td>• (^2) evidence from graph</td>
</tr>
<tr>
<td></td>
<td>• (^3) communicate: curve correctly drawn</td>
<td>• (^3) evidence</td>
</tr>
</tbody>
</table>

**NOTES:**

1. For a sketch of the curve \( y = 2 \cos 4x^\circ \), for \( 0 \leq x \leq 360 \) award 2/3

2. Disregard poor draughtsmanship.
<table>
<thead>
<tr>
<th>Question No</th>
<th>Marking Scheme</th>
<th>Illustrations of evidence for awarding a mark at each •</th>
</tr>
</thead>
</table>
| 9 (a) | Ans: \( x = -3 \) | • 1 communicate: state equation
• 1 • \( x = -3 \) | 1 mark |

NOTES:

1. For an answer of \( (\ = \ -3 \) award 0/1

(b) Ans: \( y = (x + 3)^2 - 4 \)
• 1 communicate: state equation in correct form, with \( a \ or \ b \) correct
• 2 communicate: complete equation
• 1 \( y = (x + 3)^2 + b \)
• 2 \( y = (x + 3)^2 - 4 \)
2 marks

NOTES:

1. For \( y = (x + 4)^2 - 3 \) award 0/2

(c) Ans: (0,5)
• 1 strategy: know to substitute \( x = 0 \) in equation
• 1 \( y = (0 + 3)^2 - 4 \)
• 2 communicate: state coordinates of C
• 2 (0,5)
2 marks

NOTES:

1. For a correct answer, without working, award 2/2
<table>
<thead>
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</tr>
</thead>
</table>
| 10          | Ans: \( \cos x \)° | • \( 1 \) strategy: replace \( 1 - \sin^2 x \) with \( \cos^2 x \)  
• \( 2 \) process: cancel \( \cos^2 x \) |
|             | \( \cos^2 x \)  
• \( 1 \) \( \frac{\cos^3 x}{\cos^2 x} \)  
• \( 2 \) \( \cos x \)  |

2 marks

NOTES:

1. For a correct answer, without working, award 0/2

TOTAL MARKS FOR PAPER 1
30

[END OF MARKING INSTRUCTIONS]
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### Mathematics Intermediate 2: Paper 2, Units 1, 2 and 3

<table>
<thead>
<tr>
<th>Question No</th>
<th>Marking Scheme Give 1 mark for each •</th>
<th>Illustrations of evidence for awarding a mark at each •</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Ans: There were 3 sales fewer in 2008 or There were fewer sales in 2008 because 2997 &lt; 3000</td>
<td>• 1 strategy: know how to increase by 11% • 2 strategy: know how to calculate 2008 sales • 3 process: carry out calculations correctly and state conclusion</td>
</tr>
<tr>
<td></td>
<td>• 1 × 1·11 ( = 3330) • 2 3000 × 1·11 × 0·9 ( = 2997) • 3 3 sales less in 2008</td>
<td></td>
</tr>
</tbody>
</table>

#### NOTES:

1. For an answer of “There were 3 sales fewer in 2008” without working award 3/3
2. For the third mark candidates must refer to the sales of both 2006 and 2008 or the difference between them.
3. Where a candidate increases 3000 by 11% and then decreases 3000 by 10%, only the first mark is available.
4. Where a candidate calculates 2 increases or 2 decreases, the final mark is not available.
<table>
<thead>
<tr>
<th>Question No</th>
<th>Marking Scheme</th>
<th>Illustrations of evidence for awarding a mark at each •</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 (a)</td>
<td>Ans: 172 cm</td>
<td>• 1 process: calculate the mean</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• 1 172</td>
</tr>
<tr>
<td></td>
<td></td>
<td>1 mark</td>
</tr>
<tr>
<td>2 (b)</td>
<td>Ans: 4.8 cm</td>
<td>• 1 process: calculate $(x - \bar{x})^2$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• 1, 16, 16, 36, 4, 64, 1</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• 2 process: substitute into formula</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• $\sqrt{\frac{138}{6}}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• 3 process: calculate standard deviation</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• 3 4.8</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3 marks</td>
</tr>
</tbody>
</table>

NOTES:

1 For use of alternative formula, award marks as follows:

• 1 process: calculate $\Sigma x$ and $\Sigma x^2$                          • 1 1204, 207226
• 2 process: substitute into formula                                          • $\sqrt{\frac{207226 - 1204^2 / 7}{6}}$
• 3 process: calculate standard deviation                                      • 3 4.8

2 For correct answer, without working award 0/3
<table>
<thead>
<tr>
<th>Question No</th>
<th>Marking Scheme</th>
<th>Illustrations of evidence for awarding a mark at each •</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>Ans: 882 000 mm³</td>
<td>• 1 evidence • 2 $\pi \times 41^2 \times 900$ • 3 $\pi \times 37^2 \times 900$ • 4 882 159 • 5 882 000</td>
</tr>
</tbody>
</table>

**NOTES:**

1. The final mark is for rounding an answer correct to three significant figures. Where the answer requires no rounding, the final mark cannot be awarded.

2. SOME COMMON ANSWERS (working must be shown)

<table>
<thead>
<tr>
<th>Volume (mm³)</th>
<th>Expression</th>
<th>Mark</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 530 000</td>
<td>$(\pi \times 82^2 \times 900 - \pi \times 74^2 \times 900)$</td>
<td>award 4/5</td>
</tr>
<tr>
<td>8 620 000</td>
<td>$(\pi \times 41^2 \times 900 + \pi \times 37^2 \times 900)$</td>
<td>award 4/5</td>
</tr>
<tr>
<td>76 500</td>
<td>$\left(\frac{4}{3} \times \pi \times 41^3 - \frac{4}{3} \times \pi \times 37^3\right)$</td>
<td>award 3/5</td>
</tr>
<tr>
<td>22 600</td>
<td>$(\pi \times 82 \times 900 - \pi \times 74 \times 900)$</td>
<td>award 3/5</td>
</tr>
<tr>
<td>115 000</td>
<td>$(\pi \times 41^2 \times 82 - \pi \times 37^2 \times 74)$</td>
<td>award 3/5</td>
</tr>
<tr>
<td>441 000</td>
<td>$(\pi \times 82 \times 900 + \pi \times 74 \times 900)$</td>
<td>award 2/5</td>
</tr>
<tr>
<td>45 200</td>
<td>$(\pi \times (41 - 37)^2 \times 900)$</td>
<td>award 2/5</td>
</tr>
<tr>
<td>181 000</td>
<td>$(\pi \times 8^2 \times 900)$</td>
<td>award 1/5</td>
</tr>
<tr>
<td>Question No</td>
<td>Marking Scheme</td>
<td>Illustrations of evidence for awarding a mark at each •</td>
</tr>
<tr>
<td>-------------</td>
<td>----------------</td>
<td>-------------------------------------------------------</td>
</tr>
<tr>
<td></td>
<td>Give 1 mark for each •</td>
<td></td>
</tr>
<tr>
<td>4 (a)</td>
<td>Ans: $14x + 60y = 344.30$</td>
<td>• $14x + 60y = 344.30$ 1 mark</td>
</tr>
<tr>
<td></td>
<td>• interpret: interpret the text</td>
<td></td>
</tr>
</tbody>
</table>

NOTES:

(b) Ans: $21x + 40y = 368.95$

• interpret: interpret the text

• $21x + 40y = 368.95$ 1 mark

NOTES:
<table>
<thead>
<tr>
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<th>Illustrations of evidence for awarding a mark at each •</th>
</tr>
</thead>
<tbody>
<tr>
<td>(c)</td>
<td>Ans: A car costs £11·95 and a passenger £2·95</td>
<td>1 strategy: know to solve system of equations 2 process: follow a valid strategy through to produce a value for (x) and (y) 3 process: correct value for (x) and (y) 4 communicate: state result</td>
</tr>
<tr>
<td></td>
<td>1 evidence</td>
<td>2 a value for (x) and (y) 3 (x = 11·95, y = 2·95) 4 car costs £11·95, passenger costs £2·95</td>
</tr>
<tr>
<td></td>
<td>4 marks</td>
<td></td>
</tr>
</tbody>
</table>

NOTES:

1 Incorrect answers in (a) and/or (b) must be followed through to give the possibility of awarding 4/4

2 Any valid strategy must involve the use of two equations

3 Where the correct values for \(x\) and \(y\) have been obtained without using simultaneous equations, marks are available only if both values have been substituted correctly into both equations.

\[
\begin{align*}
14 \times 11·95 + 60 \times 2·95 &= 344·30 \\
21 \times 11·95 + 40 \times 2·95 &= 368·95 \\
\text{leading to } x &= 11·95, y = 2·95 \\
a \text{ car costs } &£11·95 \\
a \text{ passenger costs } &£2·95
\end{align*}
\]
award 4/4

4 For an answer of \(x = 11·95, y = 2·95\), award 3/4 (lose communication mark)

5 For wrong answer without working or based on an invalid strategy, the final mark cannot be awarded

6 Where a candidate has calculated \(x\) or \(y\) to be negative, the final mark is not available.

7 For the award of the final mark, the costs must be stated in pounds or pence.

8 For the correct answer without working, award 0/4
<table>
<thead>
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</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>Ans: 313 square inches</td>
<td>• 1 strategy: express sector as fraction of circle • 2 process: know how to calculate shaded area • 3 process: substitute correctly into formula • 4 process: calculate area correctly</td>
</tr>
<tr>
<td></td>
<td>1 ( \frac{160}{360} )</td>
<td>• 2 evidence of difference in area of two sectors • 3 ( \frac{160}{360} \times \pi \times (18^2 - 10^2) ) • 4 313 square inches</td>
</tr>
<tr>
<td></td>
<td>4 marks</td>
<td></td>
</tr>
<tr>
<td>NOTES:</td>
<td>1 Accept variations in ( \pi ); disregard premature or incorrect rounding of 160/360</td>
<td>2 For ( \frac{160}{360} \times 2 \times \pi \times (18 - 10) ) (leading to 22.3) award 2/4</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3 For ( \frac{160}{360} \times \pi \times (18 - 10)^2 ) (leading to 89.4) award 2/4</td>
</tr>
<tr>
<td></td>
<td></td>
<td>4 Where a candidate works out the area of only one sector, eg ( \frac{160}{360} \times \pi \times 18^2 ) award 1/4</td>
</tr>
<tr>
<td>6</td>
<td>Ans: 68.6º</td>
<td>• 1 strategy: know to use cosine rule • 2 process: correct substitution • 3 process: calculate the size of angle BPM</td>
</tr>
<tr>
<td></td>
<td>1 evidence</td>
<td>• 2 ( \frac{1000^2 + 950^2 - 1100^2}{2 \times 1000 \times 950} ) • 3 68.6º</td>
</tr>
<tr>
<td></td>
<td>3 marks</td>
<td></td>
</tr>
<tr>
<td>NOTES:</td>
<td>1 Where an angle other than angle BPM has been calculated (( \angle B = 53.5º ), ( \angle M = 57.8º )), a maximum of 2/3 can be awarded provided that the value of the angle calculated is consistent with the application of the cos rule.</td>
<td>2 1.2 (RAD), 76.2 (GRAD), with working award 3/3</td>
</tr>
<tr>
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</tr>
<tr>
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<td>----------------</td>
<td>-------------------------------------------------------</td>
</tr>
<tr>
<td>7</td>
<td>Ans: ( x = -0.7, x = -4.3 )</td>
<td>• 1 strategy: know to use quadratic formula • 2 process: substitute correctly into quadratic formula • 3 process: calculate ( b^2 - 4ac ) • 4 process: state both values of ( x ) correct to 1 decimal place</td>
</tr>
</tbody>
</table>

**NOTES:**

1. Where \( b^2 - 4ac \) is calculated incorrectly, the fourth mark is available only if \( b^2 - 4ac > 0 \)
2. Alternative method (graphical solution)
   • 1 strategy: know to graph \( y = x^2 + 5x + 3 \) • 2 communicate: indicate position of roots • 3 communicate: state first root correct to 1 decimal place • 4 communicate: state second root correct to 1 decimal place

3. For a correct answer, without working award 0/4
<table>
<thead>
<tr>
<th>Question No</th>
<th>Marking Scheme</th>
<th>Illustrations of evidence for awarding a mark at each •</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>Ans: $\frac{6x}{(x-1)(x+2)}$</td>
<td>• $^1$ process: state a valid common denominator • $^2$ process: find correct numerator of equivalent fraction • $^3$ process: state answer in simplest form</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• $^1$ any valid denominator • $^2$ both numerators correct • $^3$ $\frac{6x}{(x-1)(x+2)}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3 marks</td>
</tr>
</tbody>
</table>

NOTES:

1. In this question, working subsequent to a correct answer should be ignored

2. For $\frac{2(x+2) + 4(x-1)}{(x-1)(x+2)} = \frac{6x}{x^2-2}$

\[
\frac{2(x+2) + 4(x-1)}{x^2-2} = \frac{6x}{x^2-2}
\]

award 3/3 $\checkmark\checkmark$

\[
\frac{2(x+2) + 4(x-1)}{x^2-2} = \frac{6x}{x^2-2}
\]

award 2/3 $\times\checkmark$
<table>
<thead>
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</tr>
</thead>
</table>
| 9           | Ans: \( h = \frac{2A}{(a+b)} \) | • \(^1\) start to re-arrange the formula
• \(^2\) make \( h \) the subject |
|             | 1 process: \( h(a+b) = 2A \) | \(^1\) \( h(a+b) = 2A \)
\(^2\) \( h = \frac{2A}{(a+b)} \) |

**NOTES:**

1. For \( h(a+b) = 2A \)
   
   or \( \frac{1}{2} h = \frac{A}{a+b} \)
   
   or \( h(a+b) = \frac{A}{\sqrt{2}} \)
   
   the first mark can be awarded

2. For a final answer of
   
   \( h = \frac{2A}{a+b} \)
   
   \( h = \frac{A}{\frac{1}{2}(a+b)} \)
   
   award 2/2

3. For a final answer of
   
   \( h = \frac{\sqrt{2}}{a+b} \)
   
   \( h = \frac{A}{a+b} \)
   
   award 1/2
<table>
<thead>
<tr>
<th>Question No</th>
<th>Marking Scheme Give 1 mark for each •</th>
<th>Illustrations of evidence for awarding a mark at each •</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>Ans: ( x = 239 \text{ and } x = 301 )</td>
<td>3 marks</td>
</tr>
<tr>
<td></td>
<td>• 1 process: solve equation for ( \sin x^\circ )</td>
<td>• 1 ( \sin x^\circ = -\frac{6}{7} ) or equivalent</td>
</tr>
<tr>
<td></td>
<td>• 2 process: find one value for ( x )</td>
<td>• 2 ( x = 239 )</td>
</tr>
<tr>
<td></td>
<td>• 3 process: find second value for ( x )</td>
<td>• 3 ( x = 301 )</td>
</tr>
</tbody>
</table>

**NOTES:**

1. Where \( \sin x^\circ \) is calculated incorrectly, the second and third marks are available only when \( \sin x^\circ < 0 \). Where \( \sin x^\circ > 0 \), 1/3 can be awarded when two values of \( x \) are calculated consistent with the incorrect value for \( \sin x^\circ \) (working eased).

2. Where a graphical solution has been used, the first mark is available for indicating what graph is drawn and where the values occur.

3. For a correct answer, without working award 0/3

| 11 | Ans: \( 6\sqrt{2} \) | 2 marks |
| | • 1 strategy: know how to rationalise denominator | • 1 \( \frac{12}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} \) |
| | • 2 process: simplify answer | • 2 \( 6\sqrt{2} \) |

**NOTES:**

1. For an answer of \( \frac{6\sqrt{2}}{1} \), with working award 2/2
<table>
<thead>
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<th>Illustrations of evidence for awarding a mark at each</th>
</tr>
</thead>
</table>
| 12 | Ans: \( a^2 \frac{b^4}{a^2} \) | 1\(^{st}\) process: simplify one variable  
2\(^{nd}\) process: simplify fully \textbf{with no subsequent errors} |

NOTES:

| 12 | Ans: \(-2a^2\) or \(4b^4\) | 1\(^{st}\) \(a^2\) or \(b^4\)  
2\(^{nd}\) \(a^2\) \(b^4\) |

2 marks

| 13 | Ans: 8.6 metres | 1\(^{st}\) strategy: know to apply sine rule in \(\Delta BCD\) to find \(BD\) or other valid strategy  
2\(^{nd}\) process: correct application of the sine rule or other valid strategy  
3\(^{rd}\) process: calculate \(BD\)  
4\(^{th}\) strategy: know to use right-angled trig to find height of building  
5\(^{th}\) process: correct calculation of \(AD\) |

NOTES:

1. Disregard any errors due to premature rounding provided there is evidence.
2. Variations in answers for \(BD\) (or \(DC\)) or a wrong value for \(BD\) (or \(DC\)) must be accepted as a basis for calculating the height.
3. Where a candidate assumes that \(B\) is the midpoint of \(AC\), the last two marks are available for a correct trig calculation.
4. Where an incorrect trig ratio is used to find the height, the fifth mark is still available.
5. For a correct answer without working, award 0/5

5 marks
<table>
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</tr>
</thead>
</table>
| 14 | Ans: 3·14 metres | • 1 strategy: marshall facts and recognise right angle  
• 2 strategy: know how to use Pythagoras  
• 3 process: correct calculation of $x$  
• 4 process: find height of tunnel |

4 marks

NOTES:

1 The final mark is for adding 1·7 to a value which has been calculated.

2 SOME COMMON ANSWERS (with working):

\[ \sqrt{1.7^2 + 0.9^2} + 1.7 = 3.62 \]  
award 3/4

\[ \sqrt{1.7^2 + 1.8^2} + 1.7 = 4.18 \]  
award 2/4

\[ \sqrt{1.8^2 - 1.7^2} + 1.7 = 2.29 \]  
award 2/4

\[ \sqrt{3.4^2 - 1.8^2} = 2.88 \]  
award 1/4

3 Where a candidate assumes angle XYO = angle OXY = 45°, only the final mark is available.

4 For an answer of 3·14, without working  
award 0/4

TOTAL MARKS FOR PAPER 2  
50

[END OF MARKING INSTRUCTIONS]