

2004 Mathematics

Intermediate 1 – Units 1, 2 and 3

Finalised Marking Instructions

Special Instructions

- 1 The main principle in marking scripts is to give credit for the skills which have been demonstrated. Failure to have the correct method may not preclude a pupil gaining credit for the calculations involved or for the communication of the answer.
 - Where a candidate has scored zero marks for any question attempted, "0" should be shown against the answer in the place in the margin.
 - It is of great importance that the utmost care should be exercised in adding up the marks. Where appropriate, all summations for totals and grand totals must be carefully checked.
- The answer to one part, correct or incorrect must be accepted as a basis for subsequent dependent parts of a question. Full marks in the dependent part is possible if it is of equivalent difficulty.
- Working after a correct answer should only be taken into account if it provides **firm** evidence that the requirements of the question have not been met.
- In certain cases an error will ease subsequent working. **Full** credit cannot be given for this subsequent work but **partial** credit may be given.
- Accept answers arrived at by inspection or mentally, where it is possible for the answer to have been so obtained.
- 6 Do not penalise omission or misuse of units unless marks have been specifically allocated to units.

A wrong answer without working receives no credit unless specifically mentioned in the marking scheme.

The rubric on the outside of the papers emphasises that working must be shown. In general markers will only be able to give credit to partial answers if working is shown. However there may be a few questions where partially correct answers unsupported by working can still be given some credit. **Any such instances will be stated in the marking scheme.**

8 Acceptable alternative methods of solution can only be given the marks specified, ie a more sophisticated method cannot be given more marks.

Note that for some questions a method will be specified.

- 9 In general do not penalise the same error twice in the one question.
- 10 Accept legitimate variations in numerical/algebraic questions.
- Do not penalise bad form eg $\sin x^{\circ} = 0.5 = 30^{\circ}$.
- A transcription error is not normally penalised except where the question has been simplified as a result.
- Do not penalise inadvertent use of radians in trigonometry questions, provided its use is consistent within the question.

Mathematics – Intermediate 1: Paper 1, Units 1, 2 and 3 (non-calc)

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
1. (a)	Ans: £69 •¹ process: calculate 30% of 230	•¹ 69 1 mark
NOTES:		
1. (b)	Ans: 60	
	• process: calculate $\frac{4}{7}$ of 105	•¹ 60 1 mark
NOTES:		
1. (c)	Ans: 200	
	• process: calculate $380 - 20 \times 9$	•¹ 200 1 mark
NOTES:		

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
2.	Ans: £599 •¹ strategy: correct method •² process: carry out calculations correctly	• 1 • 2 599 (award 1 for correct method or $12 \times 45 = 540$)
		2 marks
NOTES:	Correct answer with or without working	award 2/2
3.	Ans: 12m³ •¹ strategy: know how to find volume of cuboid •² process: multiply 4×2·5×1·2 correctly	• $4 \times 2 \cdot 5 \times 1 \cdot 2$ • 2 marks
NOTES: 1. Corr	ect answer with or without working	award 2/2

Question No	Marking Scheme Give 1 mark for each ●	Illustrations of evidence for awarding a mark at each •
4. (a)	Ans: −1·5 •¹ strategy: know to order numbers	-5 -4 -3 -3 -2
	•² process: find median	$-1 \ 0 \ 1 \ 2 \ 3$ $\bullet^2 \ -1.5$
		2 marks
NOTES:		
1. Corr	rect answer with or without working	award 2/2
4. (b)	Ans: 8	
	•¹ strategy: know how to find range	• 3 - (-5)
	• process: find range	• 8
		2 marks
NOTES:		
	rect answer with or without working no working necessary)	award 2/2 award 1/2
4. (c)	Ans: Invergow colder than Abergrange. Temperatures vary more in Invergow	
	• interpret/communicate: interpret calculated statistics	•¹ Invergow colder than Abergrange
	•² interpret/communicate: interpret calculated statistics	• Temperatures vary more in Invergow

1. Do not accept eg

The median is smaller in Invergow
The range is bigger in Invergow

2 marks

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
5.	Ans: $x = 6$	
	• process: collect terms in x	\bullet^1 3x
	• process: collect constants	•2 18
	• 3 process: solve equation for x	\bullet^3 $x=6$ 3 marks

1. For answers without valid working

award 0/3

eg (i) x = 6 without working

(ii) $11 + 5 \times 6 = 2 \times 6 + 29 \rightarrow x = 6$

- 2. For the award of the 3rd mark an answer of the form x =is required
- 3. Answers acceptable for partial credit (valid working must be shown)

(i) $3x = 18 \rightarrow 6$

- (ii) $3x = 40 \rightarrow x = 13 \cdot 3 \dots$ award 2/3
- (iii) $7x = 18 \rightarrow x = 2 \cdot 5 \dots$
- (iv) $7x = 40 \rightarrow x = 5.7...$ award 1/3

(Disregard incorrect rounding)

Question No	Marking Scheme Give 1 mark for each ●						Illustrations of evidence for awarding a mark at each •
6.	Ans:						
	Carnation	Daffodil	Lily	Iris	Rose ✓	Total Price £10 · 00 £10 · 50 £10 · 50 £11 · 00 £12 · 00	
	•¹ interpri •² strates	•	ome po	ssibilitie			 one correct combination two more correct combinations final two correct
	Strates	gy. Tilld al	ii possi	omues			combinations 3 marks

1. Allow one addition error or omission in total price column

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
7. (a)	Ans: 3 · 9	
	•¹ communicate: complete table	$ \begin{array}{r} \bullet^{1} & 245 \\ $
	• strategy: know how to find mean	$\bullet^2 780 \div 200$
	• process: correct division of total (Σfx)	• ³ 3.9 3 marks

1.	Final answer	with working	without working
	3.9	3/3	2/3
	$130 (780 \div 6)$	2/3	1/3

- 2. Award of 3rd mark eg $778 \div 6$
 - (a) Accept 129 r 4, $129 \cdot 7$, $129 \cdot 6$
 - (b) Do not accept 129 · 4, 130, 129
- 3. When candidate calculates mean in (b) then award 0/1 in (b) and all 3 marks for (a) are available.

7.	(b)	Ans: 5			
		•¹ interpret:	identify mode	•¹ 5	
					1 mark

Question No	Marking Scheme Give 1 mark for each ●	Illustrations of evidence for awarding a mark at each •
8. (a)	Ans: 5, 1, -4	
	•¹ process: calculate y	\bullet^1 5 or -4
	•² process: complete table	• $5 \text{ or } -4$ • $5, 1, -4$
		2 marks
8. (b)	Ans: straight line graph of $y = 3 - x$	
	•¹ communicate: prepare to draw line	•¹ all three points from the table plotted correctly
	• communicate: draw the line $y = 3 - x$	•² draw straight line through the three points (see note 2)
		2 marks

1. If the line y = 3 - x is drawn

award 2/2

2. Where the three points plotted are consistent with table and are not collinear, the second mark is unavailable

Question No	Marking Scheme Give 1 mark for each ●	Illustrations of evidence for awarding a mark at each •
9.	Ans: 20	
	•¹ process: interpret one billion	•¹ 1 000 000 000
	• process: interpret 2×10^{10}	• ² 20 000 000 000
	• 3 process: express 2×10^{10} in billions	• ³ 20 3 marks

1. Correct answer without working award 0/3

10.	Ans: 15				
	•¹ process:	substitute into expression	•1	$\frac{2\times-5\times6}{-4}$	
	•² process:	correct multiplication involving negative	•2	$2 \times -5 \times 6 = -60$	
	•³ process:	correct division involving negative	•3	15	
					3 marks

NOTES:

1. ± 15 without working award 1/3

2. $\frac{2 \times \pm 5 \times 6}{\pm 4} = \pm 15 \text{ (working must be shown)}$ award a minimum of 1/3

TOTAL MARKS FOR PAPER 1

33

Mathematics – Intermediate 1: Paper 2, Units 1, 2 and 3

Question	Marking Scheme	Illustrations of evidence for awarding
No	Give 1 mark for each ●	a mark at each ●
1.	Ans: $\frac{10}{2000}$ • process: find probability	\bullet^1 $\frac{10}{2000}$ or equivalent
		1 mark

- 1. Accept 10:2000, 10 out of 2000, 10 in 2000, 10-2000, $0\cdot005$ or cancelled down versions of the above
- 2. Do not penalise a correct answer followed by a cancelling error

Question	Marking Scheme	Illustrations of evidence for awarding
No	Give 1 mark for each •	a mark at each •
2. (a)	Ans: V	
	•¹ communicate: plot point	•¹ plot A or C
	•² communicate: plot points	• plot A, B and C 2 marks
2. (b)	Ans:	
	-8 D C C	
	•¹ strategy: plot 4th vertex of kite	•¹ plot (-3,-1)
	• communicate: state co-ordinates of D	• plot $(-3,-1)$ • $(-3,-1)$ 2 marks
NOTES:		
1. 2. 3.	Points need not be labelled If a candidate consistently plots (<i>y</i> , <i>x</i>) instead of (<i>x</i> , (a) Plot A (4, -3), B (4, 2), C (-5, 6) (b) Plot D (-1, -3) and write (-3, -1) Final mark is not available if D is in first quadrant	award 1/2 award 2/2
3. 4.	In (b) if (-3, -1) is written down but not plotted	award 2/2

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awardin a mark at each •		
3.	Ans: 48 mph			
	•¹ strategy: know how to find speed	$\bullet^1 S = \frac{D}{T}$		
	•² process: find time	•² 11h 30m		
	•³ process: find speed	• ³ 48 3 marks		
		3 marks		

- 1. 48 without working award 1/3
- 2. Examples of some common answers (working must be shown)
 - (a) implied time = 11h 30m
 - (i) $\frac{552}{11 \cdot 5} = 48$ award 3/3
 - (ii) $\frac{552}{11 \cdot 3(0)} = 48 \cdot 8...$ award 2/3
 - (b) implied time = 11h 50m
 - (i) $\frac{552}{11 \cdot 83} = 46 \cdot 6...$ award 2/3
 - (ii) $\frac{552}{11 \cdot 50} = 48$ award 1/3
- 3. Divisions which do not give a whole number answer must be rounded or truncated to at least one decimal place
 - eg implied time = 12h 30m
 - (i) $\frac{552}{12.5} = 44.16 \text{ or } 44.2 \text{ or } 44.1 \text{ award } 2/3 \checkmark \checkmark$
 - (ii) $\frac{552}{12 \cdot 5} = 44$ award 1/3
 - (iii) $\frac{552}{12 \cdot 3(0)} = 44 \cdot 8....$ or $44 \cdot 8$ or $44 \cdot 9$ award 1/3
- 4. 3rd mark is not available for division by whole number of hours
- 5. For award of 3rd mark assume answer is in mph unless units are stated

eg
$$\frac{552}{690} = 0.8$$
 miles per minute award 3/3

$$\frac{552}{690} = 0.8$$
 award 2/3

- 6. For S = DT the final 2 marks are available
 - eg $552 \times 11 \cdot 5 = 6348$ award 2/3

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
4.	Ans: $n < 5$	
	•¹ process: collect constants	\bullet^1 8 n < 40
	\bullet^2 process: solve inequality for n	\bullet^2 $n < 5$
		2 marks

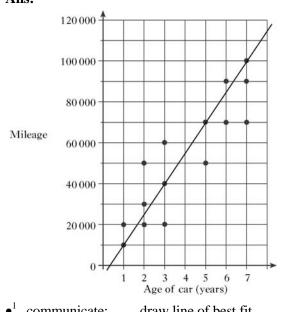
- For answers without valid working award 0/2
 - eg (i) n < 5 without working
 - (ii) $8 \times 5 - 3 < 37 \rightarrow n < 5$
- 2. Answers acceptable for partial credit (valid working must be shown)

award 1/2

(i) $8n < 40 \rightarrow < 5$ (ii) $8n < 40 \rightarrow n = 5 \text{ or } 8n = 40 \rightarrow n = 5$ (iii) $8n < 34 \rightarrow n < 4 \cdot 25 \text{ or } n < \frac{17}{4}$

Question	Marking Scheme	Illustrations of evidence for awarding
No	Give 1 mark for each •	a mark at each •

5. Ans: (a)



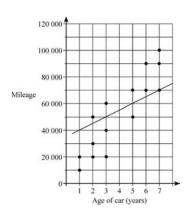
- communicate:
- draw line of best fit
- •¹ see answer

1 mark

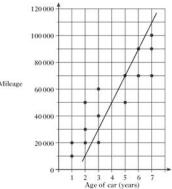
NOTES:

Accept straight lines with $5000 \le \text{gradient} \le 20\ 000\ \text{and}\ | \text{(points above line)} - \text{(points below)}$ 1. $line) | \leq 2$

eg



Mileage



- 5. **Ans: 55 000 miles** (b)
 - •¹ interpret: interpret scattergraph
- 1 55 000 (± 2000)

1 mark

Question	Marking Scheme	Illustrations of evidence for
No	Give 1 mark for each ●	awarding a mark at each •
6. (a)	Ans: $8+3t$	
	•¹ process: multiply out brackets	• $8 - 2t + 5t$ or $8 - 2t$
	•² process: collect like terms	\bullet^2 8+3t
		2 marks
NOTES:		
6. (b)	Ans: 5(2y - 7)	
	•¹ process: identify common factor	• 1 5 or $2y - 7$
	•² process: factorise	• 2 5(2y-7)
		2 marks
NOTES:		
7.	Ans: £36 000	
	•¹ strategy: correct method	•¹ •² 36 000 (award 1 for correct
	•² process: carry out calculations correctly	method or $\frac{90}{2 \cdot 50} = 36$ or
		$\frac{1000}{2 \cdot 5} = 400$)
NOTES:		
1. Corr	rect answer with or without working	award 2/2

2. 36,400 (no working necessary)

award 1/2

Question		Marking Scheme	Illustrations of evidence for
No		Give 1 mark for each •	awarding a mark at each •
8. (a)	Ans: £60 •¹ strategy: •² process:	know to use proportion carry out calculations correctly	• 1 • 2 60 (award 1 for correct method or $\frac{40}{16} = 2.5$ or $\frac{24}{16} = 1.5$)
NOTES:			
1. Corr	1. Correct answer with or without working		award 2/2
2. 2.5	, 1·5 (no working	g necessary)	award 1/2
8. (b)	Ans: 28 · 3 in	ches	
	•¹ strategy:	know to use right-angled triangle	•¹ evidence of use of 20 and 20 in right-angled triangle formula or in diagram
	•² strategy:	correct form of Pythagoras Theorem	\bullet^2 $20^2 + 20^2$
	•³ process:	calculate square root of sum or difference of two squares	•³ 28(·28)
			3 marks

- 1. Disregard incorrect rounding for answers given to one or more decimal places
- (a) 28 without working (possible use of scale drawing)
 (b) 28 · 3 , 28 · 28 without working

award 0/3

award 3/3

Question No		Marking Scheme ve 1 mark for each •	Illustrations of evidence for awarding a mark at each •
9.	Ans: Yes EITHER OR	it costs € 39 · 50 in Scotland it costs £ 25 · 33 (or £ 25 · 32) in Spain	Method 1
	•¹ strategy:	know to convert $\mathfrak{t} \rightarrow \mathfrak{t}$ (or $\mathfrak{t} \rightarrow \mathfrak{t}$)	•¹ 25·99×1·52
	•² process:	convert currency correctly	•² 39·5048
	•³ communicate:	state conclusion and valid reason	•³ Yes. It costs €39 · 50 in Scotland
			Method 2
			$\bullet^1 38 \cdot 50 \div 1 \cdot 52$
			•² 25·328
			• Yes. It costs £25 · 33 (or £25 · 32) in Spain
			3 marks
NOTES	_		
1. Do	o not accept "Yes" with	nout working/valid reason	award 0/3
2. Ac (a)		$4 \times 25 \cdot 33 \text{ (or £ 25 \cdot 32)}$	
(b)		ss € 39 · 50 in Scotland ss £ 25 · 328	award 3/3
(0)		as €39 · 5048 in Scotland	award 2/3 ✓ ✓ X
(c)	Yes. It costs €39	· 50	award 2/3 ✓ ✓ X
(d)	He saves 67p (or 6	66p) OR €1	award 3/3
(e)			award 2/3 ✓ ✓ X
(f)		p) or €1 more in Scotland	award 3/3
(g)	It costs 67p (or 66	p) or €1 more	award 2/3
3. Tr	eat subtraction errors a	as insignificant.	
	$25 \cdot 99 - 25 \cdot 33 \rightarrow H$	_	award 3/3
		available for $17 \cdot 09 \dots (25 \cdot 99 \div 1 \cdot 1)$ conclusion and valid reason	52) or $58 \cdot 52 \ (38 \cdot 50 \times 1 \cdot 52)$

Question No		Marking Scheme Give 1 mark for each •		ustrations of evidence for warding a mark at each •
10.	Ans: 53°			
	•¹ strategy:	know to use right-angled triangle	•1	use 1·5 and 0·9 in right- angled triangle diagram or formula
	•² strategy:	know how to use cosine ratio	•2	$\cos x^{\circ} = \frac{0 \cdot 9}{1 \cdot 5}$
	•³ process:	calculate ratio	•3	$\cos x^{\circ} = 0.6$
	• ⁴ process:	carry out trigonometric calculation	•4	53 ·
				4 marks

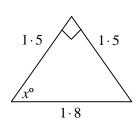
1. Correct answer without working award 3/4

2. Where an incorrect trig ratio is used, working should be followed through with the possibility of awarding 3/4 (working must be shown) eg

(a)
$$\sin x = \frac{0.9}{1.5} \rightarrow x = 36 \cdot$$
 or 37

award 3/4

(b)



$$\cos x = \frac{1 \cdot 5}{1 \cdot 8} \rightarrow x = 33 \cdot \dots \text{ or } 34$$

$$\begin{array}{c}
1.5 \\
\text{OR } \sin x = \frac{1 \cdot 5}{1 \cdot 8} \rightarrow x = 56 \cdot \dots \\
1 \cdot 5 \\
\text{OR } \sin x = \frac{1 \cdot 5}{1 \cdot 8} \rightarrow x = 56 \cdot \dots
\end{array}$$
award 3/4

OR $\tan x = \frac{1 \cdot 5}{1 \cdot 5} \rightarrow x = 45$

right angle need not be marked

Accept variations in answers due to rounding. 3.

4. with working without working 0.92 (radians used) OR 59.03..... (grads used) 4/4 3/4

Question No	Marking Scheme Give 1 mark for each •	Illustrations of evidence for awarding a mark at each •
11. (a)	Ans: 3 · 25 %	
	•¹ interpret: interpret line graph	• $3 \cdot 25 \text{ or } 3\frac{1}{4}$
		1 mark
11. (b)	Ans: It went down	
	•¹ interpret: interpret trend in line graph	•¹ It went down
		1 mark

1. Disregard numerical errors in an otherwise correct answer

	T			
11. (c)	Ans: £8.75			
	•¹ interpret:	interpret line graph	•1	2.5
	$\bullet^2 \bullet^3$ strategy:	know how to calculate interest	•2 •3	$\frac{2 \cdot 5}{100} \times 1400 \times \frac{3}{12}$ (award 1 for an otherwise correct method with one missing or incorrect step)
	• 4 process:	carry out percentage and fraction calculations correctly	•4	8 · 75 4 marks

1.	Final answers	with working	without working
	8 · 75	4/4	3/4
	35 (2.5% of 1400)	2/4	1/4
	$105 (2.5\% \text{ of } 1400 \times 3)$	2/4	1/4

- 2. If <u>amount</u> is found ie $1408 \cdot 75$, a maximum of 3 marks is available unless candidate clearly indicates that <u>interest</u> = $8 \cdot 75$
- 3. Do not penalise premature rounding or truncation eg $2 \cdot 5\%$ of $1400 = 35 \div 12 = 2 \cdot 91 \times 3 = £8 \cdot 73$ award 4/4

Question No	Marking Scheme Give 1 mark for each •		Illustrations of evidence for awarding a mark at each •		
12.	Ans: 9 · 3				
	•¹ process:	substitute into formula	•1	$\sqrt{9\cdot81\times9}$	
	•² process:	start to evaluate	•2	$\sqrt{88\cdot 29}$	
	•³ process:	complete evaluation	•3	9.3	3 marks
NOTES:					
1. Do n	not penalise prema	ture or incorrect rounding			
	Final answers		with wor	king witho	ut working

2.	Final answers		with working	without working	
	(a)	9 · 4 , 9 · 3	3/3	3/3	
	(b)	9	3/3	0/3	
	(c)	$28 \cdot 1 \dots \left(\sqrt{9 \cdot 81} \times 9 \right), \ 29 \cdot 43 \left(9 \cdot 81 \times \sqrt{9} \right)$	2/3	2/3	
	(d)	$4 \cdot 3 \ldots \left(\sqrt{9 \cdot 81} + 9\right)$	2/3	2/3	
	(e)	$3\cdot 1 \ldots \left(\sqrt{9\cdot 819}\right)$	1/3	0/3	
3.	(a)	$\sqrt{9 \cdot 81} \times 9 = 88 \cdot 29 \text{ or } \sqrt{88 \cdot 29}$	award 2/3		
	(b)	$9 \cdot 81 \times 9 = 88 \cdot 29$ or $88 \cdot 29$	award 1/3		

. ,					
13.	Ans: 45%				
	•¹ strategy:	know to express 18 as a fraction of 40	•1	$\frac{18}{40}$	
	•² strategy:	know how to express $\frac{18}{40}$ as a percentage	•2	$\frac{18}{40} \times 100$	
	•³ process:	divide and multiply correctly	•3	45	3 marks

- Correct answer without working Acceptable answers for partial credit (no working necessary) 1. award 3/3
- 2.

(a)
$$\frac{40}{18} \times 100 = 222(\cdot)$$
 award 2/3 **X** \checkmark \checkmark

(b)
$$\frac{40}{100} \times 18 \text{ or } \frac{18}{100} \times 40 = 7 \cdot 2$$
 award 1/3

Question No	Marking Scheme Give 1 mark for each •		Illustrations of evidence for awarding a mark at each ●
14.	Ans: 1 · 46 m ²		
	•¹ strategy:	know to calculate area of semi- circle	$\bullet^1 A = \frac{1}{2}\pi r^2$
	•² strategy:	substitute correct radius into area formula	$\bullet^2 \frac{1}{2} \times \pi \times 0.3^2$
	•³ strategy:	know to subtract area of semi- circle from area of rectangle	$\bullet^3 (2 \times 0 \cdot 8) - \left(\frac{1}{2} \times \pi \times 0 \cdot 3^2\right)$
	• 4 process:	carry out all calculations correctly (must include a circle calculation and either the squaring of a number or a division by 2)	• ⁴ 1·458
	• 5 process:	round to 2 decimal places	• ⁵ 1·46 5 marks

1. First 2 marks not available if $C = \pi d$ is used

2.	Exar	mples of some common answers	with working	without working
	(a)	$1 \cdot 6 - \frac{1}{2} \times \pi \times 0 \cdot 3^2 = 1 \cdot 46$	award 5/5	award 4/5
	(b)	$16000 - \frac{1}{2} \times \pi \times 30^2 = 14586 \cdot 28$	award 4/5	award 3/5
	(c)	$1 \cdot 6 - \pi \times 0 \cdot 3^2 = 1 \cdot 32$	award 4/5	award 0/5
	(d)	$1 \cdot 6 - \frac{1}{2} \times \pi \times 0 \cdot 6^2 = 1 \cdot 03$	award 4/5	award 0/5
	(e)	$1 \cdot 6 - \pi \times 0 \cdot 6^2 = 0 \cdot 47$	award 3/5	award 0/5
	(f)	$1 \cdot 6 - \frac{1}{2} \times \pi \times 0 \cdot 6 = 0 \cdot 66$	award 3/5	award 0/5
		$1 \cdot 6 - \pi \times 0 \cdot 6 = -0 \cdot 28$	award 2/5	award 0/5

- 3. (a) Unrounded or incorrectly rounded versions of the above answers should be awarded 1 mark less than those shown above.
 - (b) $1 \cdot 4$ without working award 0/5.
- 4. 5th mark only available where candidate is required to round circle calculation to 2 decimal places

TOTAL MARKS FOR PAPER 2 47