

2004 Mathematics

Higher

Finalised Marking Instructions

- 1. Marks must be assigned in accordance with these marking instructions. In principle, marks are awarded for what is correct, rather than marks deducted for what is wrong.
- 2. Award one mark for each 'bullet' point. Each error should be underlined in RED at the point in the working where it first occurs, and not at any subsequent stage of the working.
- 3. The working subsequent to an error must be followed through by the marker with possible full marks for the subsequent working, provided that the difficulty involved is approximately similar. Where, subsequent to an error, the working is eased, a deduction(s) of mark(s) should be made. This may happen where a question is divided into parts. In fact, failure to even answer an earlier section does not preclude a candidate from assuming the result of that section and obtaining full marks for a later section.
- 4. Correct working should be ticked (✓). This is essential for later stages of the SQA procedures. Where working subsequent to an error(s) is correct and scores marks, it should be marked with a crossed tick (X). In appropriate cases attention may be directed to work which is not quite correct (e.g. bad form) but which has not been penalised, by underlining with a dotted or wavy line.

Work which is correct but inadequate to score any marks should be corrected with a double cross tick (\mathbf{X}).

- 5. The total mark for each section of a question should be entered in red in the **outer** right hand margin, opposite the end of the working concerned.
 - Only the mark should be written, **not** a fraction of the possible marks.
 - These marks should correspond to those on the question paper and these instructions.
- 6. It is of great importance that the utmost care should be exercised in adding up the marks. Where appropriate, all summations for totals and grand totals must be carefully checked.

Where a candidate has scored zero marks for any question attempted, "0" should be shown against the answer.

7. As indicated on the front of the question paper, full credit should only be given where the solution contains appropriate working. Accept answers arrived at by inspection or mentally where it is possible for the answer so to have been obtained. Situations where you may accept such working will be indicated in the marking instructions.

cont/

Mathematics Higher: Instructions to Markers

- 8. Do not penalise:
 - working subsequent to a correct answer
 - omission of units
 - bad form
 - legitimate variations in numerical answers
 - correct working in the "wrong" part of a question
- 9. No piece of work should be scored through even where a fundamental misunderstanding is apparent early in the answer. Reference should always be made to the marking scheme answers which are widely off-beam are unlikely to include anything of relevance but in the vast majority of cases candidates still have the opportunity of gaining the odd mark or two provided it satisfies the criteria for the mark(s).
- 10. If in doubt between two marks, give an intermediate mark, but without fractions. When in doubt between consecutive numbers, give the higher mark.
- 11. In cases of difficulty covered neither in detail nor in principle in the Instructions, attention may be directed to the assessment of particular answers by making a referal to the P.A. Please see the general instructions for P.A. referrals.
- 12. No marks should be deducted at this stage for careless or badly arranged work. In cases where the writing or arrangement is very bad, a note may be made on the upper left-hand corner of the front cover of the script.
- 13 **Do not write any comments on the scripts**. A summary of acceptable notation is given on page 4.

Summary

Throughout the examination procedures many scripts are remarked. It is essential that markers follow common procedures:

- 1 Tick correct working.
- 2 Put a mark in the right-hand margin to match the marks allocations on the question paper.
- 3 Do not write marks as fractions.
- 4 Put each mark at the end of the candidate's response to the question.
- 5 Follow through errors to see if candidates can score marks subsequent to the error.
- 6 Do not write any comments on the scripts.

Mathematics Higher: Instructions to Markers

Higher Mathematics : A Guide to Standard Signs and Abbreviations

Remember - No comments on the scripts. Please use the following and nothing else.

- The tick. You are not expected to tick every line but of course you must check through the whole of a response.
- X The cross and underline. Underline an error and place a cross at the end of the line.
- ★ The tick-cross. Use this to show correct work where you are following through subsequent to an error.
- The double cross-tick. Use this to show correct work but which is inadequate to score any marks.
- ∧ The roof. Use this to show something is missing such as a crucial step in a proof or a 'condition' etc.
 - The tilde. Use this to indicate a minor transgression which is not being penalised (such as bad form).
- E Eased. Where working is found correct whilst following through subsequent to an error, the working has been eased sufficiently for a mark not to be awarded.
- BOD Benefit of Doubt. Use this where you have to decide between two consecutive marks and award the higher.

line hole	Marks being allo normally be show		ould not	
noie		-	margin	s
	$\frac{dy}{dx} = 4x - 7$		IŬ	
	4x - 7 = 0	x		
and	$x = \frac{7}{4}$	^		
	$y = 3\frac{7}{8}$	× •		
	$y = 5\overline{8}$	ו	2	
¢	C = (1, -1)	X		
nt to	$m = \frac{3 - (-1)}{4 - 1}$	~		
	$m_{rad} = \frac{4}{3}$	∢ • follow	through	
			unougn	
	$m_{tgt} = \frac{-1}{\frac{4}{3}}$			
ect	$m_{igt} = -\frac{3}{4}$	ו		
	$m_{igi} = -\frac{3}{4}$ $y - 3 = -\frac{3}{4}(x - 2)$	ו	3	
ing	$x^2 - 3x = 28$	1.		
n'	x 0x - 20	•		
	x=7 🔨	ж	1	
	$\sin(x) = 0.75 = inv\sin(x)$	(0.75) = 48.6°		
uch	\sim			
		✓•	1	
t e	$\log_3(x-\underline{2}) = 1$	× ו		
:k	$(x-2) = 3^1$	ו		
	x - 2 = 3	N		
	<i>x</i> = 5	Ӿ Е	1	
			1 1	

All of these are to help us be more consistent and accurate.

It goes without saying that however accurate you are in marking, it is to no avail unless you have added the marks up correctly. Please double check totals!!

5

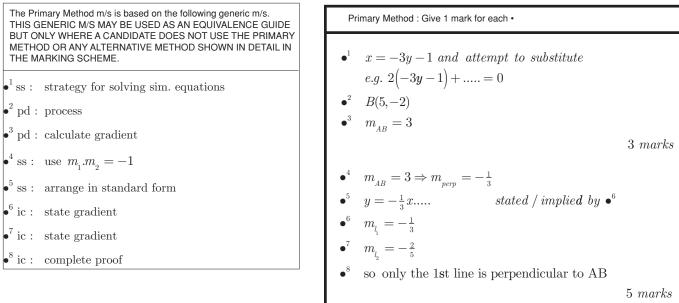
5 marks

1 The point A has coordinates (7, 4). The straight lines with equations x + 3y + 1 = 0 and

2x + 5y = 0 intersect at B.

- (a) Find the gradient of AB.
- (b) Hence show that AB is perpendicular to only one of these two lines.

	Source 04/15	Calculator class CN	Syllabus Code 1.1.1 1.1.9, 1.1.10	Grade C C	marks 3 5	part a b	Qu. 1
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Notes

1 For \bullet^1

Elimination may be used instead of substitution

Evidence of a start to elimination would be the appearance of equal coefficients of x or y.

- 2 For (a) equating the zeros, neither of the first two marks are available.
- 3 (5,-2) may be obtained by inspection or trial and improvement. If it is justified by checking in both equations, •¹ and •² may be awarded. If is not justified in both equations, award neither of the first two marks.
- 4 A general statement about perpendicular lines must have $m_1 \cdot m_2 = -1$ earns no marks
- 5 Candidates who make a mistake in (a) may have to show in (b) that neither line is perpendicular to AB. All five marks are available.

1 Alternative Method for •4 to •8 $\bullet^4 \quad y=-\tfrac{1}{3}x... \qquad \text{may be implied by } \bullet^5$ $\bullet^5 \quad m_l=-\tfrac{1}{3}$

- $\label{eq:ml_l_s} \begin{array}{ll} \bullet^6 & m_{l_2} = -\frac{2}{5} \\ \bullet^7 & l_1: 3 \times -\frac{1}{3} = -1 \ \mbox{so} \ AB \perp l_1 \end{array}$
 - and AB is not $\perp l_2$

2	Alternative Method for •4 to •8	
	$\begin{array}{l} m_{_{AB}}=3 \Rightarrow m_{_{perp}}=-\frac{1}{3}\\ y=-\frac{2}{5}x \qquad \qquad stated \ / \ implied \ by \ \bullet^6\\ m_{_{l_1}}=-\frac{2}{5} \end{array}$	
	$m_{l_1} = 5$ $m_{l_2} = -\frac{1}{3}$ so only the 2nd line is perpendicular to AB	
		5 marks

Continued on page 6

 $\mathbf{5}$

1 The point A has coordinates (7, 4). The straight lines with equations x + 3y + 1 = 0 and

2x + 5y = 0 intersect at B.

- (a) Find the gradient of AB.
- (b) Hence show that AB is perpendicular to only one of these two lines.

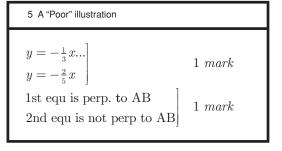
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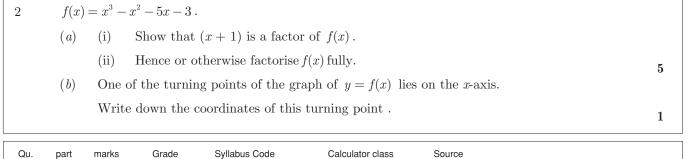
continued from page 5

3 Alternative Method for •4 to •8	
• ⁴ $m_{perp} = -\frac{1}{3}$ • ⁵ strat: find equ. thr' B with gradient $-\frac{1}{3}$ • ⁶ $y - (-2) = -\frac{1}{3}(x-5)$ • ⁷ <i>leading to</i> $3y + x + 1 = 0$ • ⁸ the first line is the ONLY line perp. to AB	5 marks

4 Alternative Method for •4 to •8
•
$$y = -\frac{1}{3}x...$$
 may be implied by •⁵
• $m_{l_1} = -\frac{1}{3}$
• $m_{l_2} = -\frac{2}{5}$
• $l_1: 3 \times -\frac{1}{3} = -1$ so AB is the **ONLY** line $\perp l_1$
• $m_{l_1} = \frac{1}{3} = -1$ so AB is the **ONLY** line $\perp l_1$
• $m_{l_1} = \frac{1}{3} = -1$ so AB is the **ONLY** line $\perp l_1$
• $m_{l_2} = \frac{1}{3} = -1$ so AB is the **ONLY** line $\perp l_1$
• $m_{l_2} = \frac{1}{3} = -1$ so AB is the **ONLY** line $\perp l_1$

6 Further illustrations	
AB is perp. to $x + 3y + 1 = 0$	
because $3 \times -\frac{1}{3} = -1$	$ullet^4$ only
[end!]	
AB is perp. to $x + 3y + 1 = 0$	
as its gradient is $-\frac{1}{3}$	• ⁴ (& • ⁵)
and AB is $3 \Leftrightarrow 3 \times -\frac{1}{3} = -1$	• (&•)
and AD is $5 \Leftrightarrow 5 \land _{3} = 1$ all of the above writing	•7
AB is perp. to the line $y = -\frac{1}{3}$	•5
because $3 \times -\frac{1}{3} = -1$	\bullet^4
all of the above writing	•7





NC

2.1.3 2.1.3

2

a b

5 1

C C

The Primary Method m/s is based on the following generic m/s. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY	Primary Method : Give 1 mark for each •
METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME.	• 1know to find $f(-1)$
• ¹ ss : know to find $f(-1)$	\bullet^2 -1 1 -1 -5 -3
\bullet^2 ss : start eg synthetic division	1
\bullet^3 pd : complete to zero remainder	\bullet^3 -1 1 -1 -5 -3
• ic : extract quadratic	-1 2 3
• ⁵ ic : fully factorise	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
\bullet^6 ic : state coordinates	• $x^{4} - 2x - 3$ • $(x + 1)(x + 1)(x - 3)$
]	5 mar
	-6(-1,0)

•
$$^{1}know to find f(-1)$$

• $^{2} -1$ 1 -1 -5 -3
-1
• $^{3} -1$ 1 -1 -5 -3
-1 2 3
. 1 -2 -3 0
• $^{4}x^{2} - 2x - 3$
• $^{5}(x+1)(x+1)(x-3)$
5 marks
• $^{6}(-1,0)$
1 mark

1 Alternative Method 1 for •1 , •2 and •3

04/58

- \bullet^1 know to find f(-1)
- $f(-1) = (-1)^3 (-1)^2 5(-1) 3 = 0$ \bullet^2
- a strategy for finding the quadratic factor \bullet^3 eg inspection, long division, synthetic division

Notes

1 Treat f(x) = (x+1), (x+1), (x-3) as bad form

2 \bullet^6 is not available for

"(-1,0) or (3, 0)"
"
$$x = -1$$
"
an unsupported "(0,-1)"
Treat $\begin{array}{c} x = -1 \\ y = \dots = 0 \\ \text{so point} = (0,-1) \end{array}$ as bad form

3

3 Find all the values of x in the interval
$$0 \le x \le 2\pi$$
 for which $\tan^2(x) = 3$.

Qu.partmarksGradeSyllabus CodeCalculator classSource34C1.2.9, 1.2.11NC04/85

The Primary Method m/s is based on the following generic m/s. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME.

 \bullet^1 ss : know to get the square root

 \bullet^2 pd : solve trig equation

 \bullet^3 pd : solve trig equation

•⁴ ic : know there is
$$+\sqrt{}$$
 and $-\sqrt{}$

Primary Method : Give 1 mark for each • • $\tan x = \sqrt{3}$ • $x = \frac{\pi}{3}$ • $x = \frac{4\pi}{3}$ • $\tan x = -\sqrt{3}$ stated explicitly and $x = \frac{2\pi}{3}, \frac{5\pi}{3}$ 4 marks

1 Alternative Method for
$$\cdot 1$$
 and $\cdot 2$
•¹ $\tan x = \sqrt{3}$
•² $x = \frac{\pi}{3}$
•³ $\tan x = -\sqrt{3}$ and $x = \frac{2\pi}{3}$
•⁴ $\frac{4\pi}{3}$ and $\frac{5\pi}{3}$
4 marks

Notes

- Candidates must produce final answers in radians.
 If their final answer(s) are in degrees then deduct one mark.
- 2 Cave

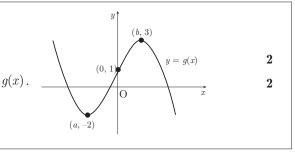
Candidates who produce the four correct answers from $\tan(x) = \sqrt{3}$ can only be awarded \bullet^1 and \bullet^2 .

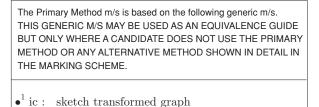
3 Do not penalise "correct" answers outside the range $0 \le x \le 2\pi$

4 Do **NOT** accept
$$\pi + \frac{\pi}{3}$$
 for $\frac{4\pi}{3}$.



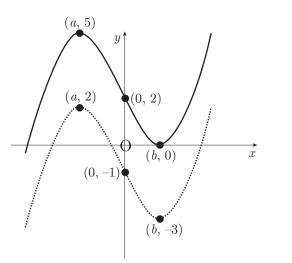
- (a) Sketch the graph of y = -g(x).
- (b) On the same diagram sketch the graph of y = 3 g(x).





- \bullet^2 ic : show new coordinates
- \bullet^3 ic : sketch transformed graph
- •⁴ ic : show new coordinates

solution



1		
\bullet^1	reflection in x -axis and any one from	
	(0,-1),(a,2),(b,-3) clearly annotated	
\bullet^2	the remaining two from the above list	
		2 marks
\bullet^3	translation and any one from	
	(0,2),(a,5),(b,0) clearly annotated	
\bullet^4	the remaining two from the above list	
	-	2 marks

Notes

3

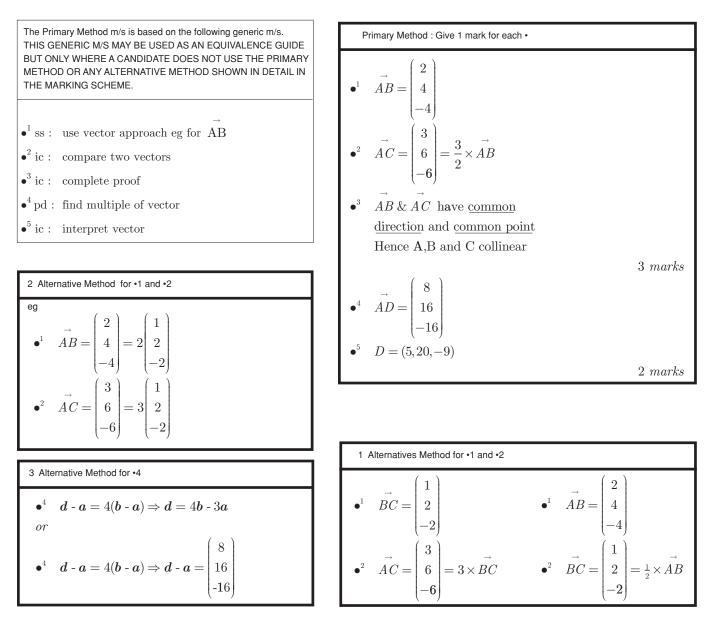
- 1 For (a), reflection in the *y*-axis earns a maximum of 1 out of 2 with all 3 points clearly annotated
- 2 For (b), a translation of $\begin{pmatrix} 0 \\ -3 \end{pmatrix}$ earns a maximum
 - of 1 out of 2 with all 3 points clearly annotated
 - For (b), a translation of $\begin{pmatrix} \pm 3 \\ 0 \end{pmatrix}$ earns no marks.
- 4 For the annotated points in (a) and (b), accept a superimposed grid.
- 5 g(x) needs to retain its cubic shape for \bullet^1 and \bullet^2
- 6 In (b) \bullet^3 and \bullet^4 are only available for applying the translation to the resulting graph from (a).

 $\mathbf{2}$

5 A,B, and C have coordinates (-3, 4, 7), (-1, 8, 3), and (0, 10, 1) respectively.

- (a) Show that A, B, and C are collinear.
- (b) Find the coordinates of D such that AD = 4AB.

5 a 3 C 3.1.7 CN 04/n b 2 B 3.1.6	Qu. 5	part a b	marks 3 2	Grade C B		Calculator class CN	Source 04/n
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1 Treat D=
$$\begin{pmatrix} 5\\20\\-9 \end{pmatrix}$$
 as bad form.

2 For \bullet^3 accept **ONLY** "parallel" in lieu of "common direction"

6 Given that
$$y = 3\sin(x) + \cos(2x)$$
, find $\frac{dy}{dx}$.

Source 04/n		Calculator class CN	Syllabus Code 3.2.1	Grade B	marks 3	part	Qu. 6
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The Primary Method m/s is based on the following generic m/s. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME.

•¹ pd : process simple derivative

 \bullet^2 pd : start to process compound derivative

 \bullet^3 ic : complete compound derivative

Primary Method : Give 1 mark for each • • $3\cos(x)$ • $2 -\sin(2x)$ • 3×2 3 marks

1 Alternative Methods	
e.g.	
$y = 3\sin(x) + 2\cos^{2}(x) - 1$ • ¹ $3\cos(x)$ • ² $4\cos(x)$ • ³ $\times -\sin(x)$ and no further terms	
	3 marks

Notes

- 1 For differentiating incorrectly: For $y' = -3\cos(x) + 2\sin(2x)$, only \bullet^3 may be awarded.
- 2 For $y' = 3\cos(x) 2\sin(2x) + c$, treat the "+c" as bad form.
- 3 For clearly integrating correctly or otherwise: Award no marks.
- 4 If you cannot decide whether a candidate has attempted to differentiate or integrate, assume they have attempted to differentiate.

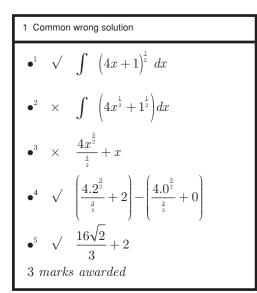
7 Find
$$\int_{0}^{2} \sqrt{4x+1} dx$$
.

Qu. part marks Grade Syllabus Code Calculator class Source 04/52
The Primary Method m/s is based on the following generic m/s.
Primary Method : Give 1 mark for each •

The Primary Method mys is based on the following generic m/s. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME.

 \bullet^1 ic : express in integrable form

- $\bullet^2 \, \mathrm{pd}$: integrate a composite fractional power
- \bullet^3 ic : interpret the '4'
- \bullet^4 ic : substitute limts
- \bullet^5 pd : evaluate



Primary Method : Give 1 mark for each • • $(4x + 1)^{\frac{1}{2}}$ • $\frac{1}{\frac{3}{2}}(4x + 1)^{\frac{3}{2}}$ • $\frac{3}{2} \div 4$ • $\frac{1}{6}(4 \times 2 + 1)^{\frac{3}{2}} - \frac{1}{6}(4 \times 0 + 1)^{\frac{3}{2}}$ • $\frac{5}{13}$ or equivalent fraction or mixed number 5 marks

Notes

eg

 $1 \bullet^4$ is available for substituting the limits correctly into any function except the original one.

$$\int_{0}^{2} (4x+1)^{\frac{1}{2}} dx$$

= $\left[(4x+1)^{\frac{1}{2}} \right]_{0}^{2}$
= $(4 \times 2 + 1)^{\frac{1}{2}} - (4 \times 0 + 1)^{\frac{1}{2}}$
= $3 - 1$
= 2

may be awarded \bullet^1 , not \bullet^2 (no integration) not \bullet^3 (not dealing with f(g(x)))

not • (not detaining with
$$f(g(x))$$
)
not •⁴ (original function)
not •⁵ (working eased)

2 For \bullet^5 , **DO NOT accept** answers like $\frac{\sqrt{729}}{6} - \frac{1}{6}$.

8 (a) Write $x^2 - 10x + 27$ in the form $(x+b)^2 + c$. (b) Hence show that the function $g(x) = \frac{1}{3}x^3 - 5x^2 + 27x - 2$ is always increasing.							2 4		
Qu. 8	part a b	marks 2 4	Grade C B	Syllabus Code 1.2.8 1.3.11	Calci NC	ulator class	Source 04/37		
THIS G BUT ON METHC	ENERIC N	//S MAY BE RE A CANDII Y ALTERNA ⁻	USED AS AN I DATE DOES N	wing generic m/s. EQUIVALENCE GUIDE OT USE THE PRIMARY SHOWN IN DETAIL IN		Primary Method $(x-5)^2 \dots \\ (x-5)^2 +$		k for each •	
\bullet^1 pd :	deal w	ith the 'b'							2 marks
\bullet^2 pd :	deal w	ith the 'c'			• ³	$g'(x) = x^2 - 10x + $		STATED EX	CPLICITLY
\bullet^3 ss :	use dif	ferentiatio	on		\bullet^4	$x^2 - 10x +$	- 27		
\bullet^4 pd :	differen	ntiate			\bullet^5	$(x-5)^2 +$	2		
\bullet^5 ss :	use pre	evious wor	rking		• ⁶	g'(x) > 0 for	or all x		
• ⁶ ic :	comple	ete proof				and so $g(x)$	c) increasi	ing	
									4 marks

1 Alternative	Method for •3 to •6
• ⁶ no roots	STATED EXPLICITLY + 27 = $100 - 108 = -8$, concave up, $g'(x) > 0$; $g(x)$ increasing 4 marks

Notes

- 1 For \bullet^6 , accept g'(x) > 2 in lieu of g'(x) > 0
- 2 Evaluating g(1), g(2) etc or g'(1), g'(2) etc gains no credit.

9 Solve the equation
$$\log_2(x+1)-2\log_2(3)=3$$
 .

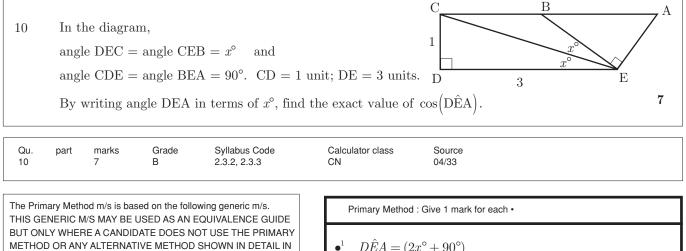
Qu. pa 9	rt marks 4	Grade AB	Syllabus Code 3.3.4	Calculator class NC	Source 04/57
			wing generic m/s.	Primary Metho	d : Give 1 mark for each •
BUT ONLY W	HERE A CANDII ANY ALTERNAT	DATE DOES N	OT USE THE PRIMARY SHOWN IN DETAIL IN	\bullet^1 $-\log_2 3^2$	
• ¹ ic : use	log laws			• ² $\log_2\left(\frac{x+3}{3^2}\right)$	$\left \frac{-1}{2}\right = 3$
	log laws	untial form		• $\frac{x+1}{3^2} =$	2^3

$$\bullet^3$$
 ic : express in exponential form

 \bullet^4 pd : process

 3^2 x = 71•4 4 marks

1 Alternative Method $\log_2(x+1) - 2\log_2 3 = 3\log_2 2$ $\log_2(x+1) = \log_2 2^3 + \log_2 3^2$ $\log_2(x+1) = \log_2(2^3 \times 3^2)$ \bullet^1 \bullet^2 \bullet^3 •4 x = 714 marks



•¹ ic : interpret diagram

THE MARKING SCHEME.

- \bullet^2 pd : expand trig expression
- \bullet^3 pd : simplify
- \bullet^4 ss : use appropriate formula
- •⁵ pd : process
- •⁶ ic : interpret
- \bullet^7 pd : simplify

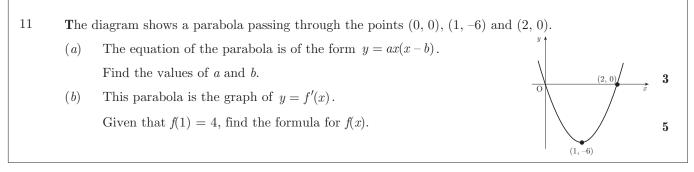
Primary Method : Give 1 mark for each • • $D\hat{E}A = (2x^{\circ} + 90^{\circ})$ • $\cos(2x^{\circ})\cos(90^{\circ}) - \sin(2x^{\circ})\sin(90^{\circ})$ • $-\sin(2x^{\circ})$ • $-2\sin(x^{\circ})\cos(x^{\circ})$ • $CE = \sqrt{1^{2} + 3^{2}} = \sqrt{10}$ stated / implied by •6 • $\sin(x^{\circ}) = (\frac{1}{\sqrt{10}})$ and $\cos(x^{\circ}) = \frac{3}{\sqrt{10}}$ • $\cos D\hat{E}A = -2(\frac{1}{\sqrt{10}})(\frac{3}{\sqrt{10}}) = -\frac{6}{10}$ 7 marks

Note

1 Although unusual, it would be perfectly acceptable for a candidate to go from \bullet^1 to \bullet^3 without expanding (via knowledge of transformations). In this case \bullet^2 would awarded by default.

2 ai	nother common wrong solution	
$\bullet^1 $	$D\hat{E}A = (2x^{\circ} + 90^{\circ})$	
	$\cos(2x^\circ + 90^\circ)$	
$\bullet^2 imes$	$\cos(2x^\circ) + \cos(90^\circ)$	
$\bullet^3 imes$	$\cos(2x^{\circ})$	[working eased]
$\bullet^4 $	$eg \ 2\cos^2 x - 1$	
$\bullet^5 $	$CE = \sqrt{1^2 + 3^2} = \sqrt{10}$	stated / implied by $\bullet 6$
$\bullet^6 $	$\cos(x^{\circ}) = \frac{3}{\sqrt{10}}$	
$\bullet^7 $	$\cos D\hat{E}A = 2\left(\frac{3}{\sqrt{10}}\right)\left(\frac{3}{\sqrt{10}}\right) - 1$	$=\frac{8}{10}$
		5 marks awarded

1 co	mmon wrong solution
$\bullet^1 $	$D\hat{E}A = (2x^\circ + 90^\circ)$
$\bullet^2 $	$\cos(2x^\circ)\cos(90^\circ) - \sin(2x^\circ)\sin(90^\circ)$
	$\cos(2x^{\circ}) \times 1 - \sin(2x^{\circ}) \times 0$
$\bullet^3 \times$	$\cos(2x^{\circ})$
$\bullet^4 $	$eg \ 2\cos^2 x - 1$
$\bullet^5 $	$CE = \sqrt{1^2 + 3^2} = \sqrt{10}$ stated / implied by •
$\bullet^6 $	$\cos(x^{\circ}) = \frac{3}{\sqrt{10}}$
$\bullet^7 $	$\cos D\hat{E}A = 2\left(rac{3}{\sqrt{10}} ight)\left(rac{3}{\sqrt{10}} ight) - 1 = rac{8}{10}$
	6 marks awarded



Qu. part marks Grade Syllabus Code 11 a 3 B 2.1.10 b 5 A 2.2.8	culator class Source 04/57
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The Primary Method m/s is based on the following generic m/s. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME.

- •¹ ss : use parabolic form
- \bullet^2 pd : substitute
- \bullet^3 pd : process
- \bullet^4 ss : know to integrate
- •⁵ pd : express in integrable form
- \bullet^6 pd : integrate
- $\bullet^7 \, \mathrm{ss}$: introduce constant and substitute
- \bullet^8 pd : process

Notes

1 In the primary method, •3 must be justified.

A "guess and check" would be acceptable ie guess a = 6 then check that (1, -6) fits the equation.

- 2 In the primary method, •5 is only available if an intention to integrate has been indicated.
- For candidates who fail to complete (a)
 but produce values for a and b ex nihilo, 5
 marks are available in (b). A deduction of
 1 mark may be made if their choice eases
 the working.
- 4 For candidates who retain "a" and "b" in part (b), marks \bullet^4 to \bullet^7 are available.
- 5 **CAVE**

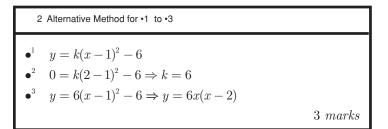
$$\int_{0}^{2} 6x(x-2)dx = \left[2x^{3} - 6x^{2}\right]_{0}^{2} = -8 \text{ may be}$$

awarded •⁴, •⁵ and •⁶.

Primary Method : Give 1 mark for each • • b = 2 or y = ax(x-2)• substitute (1,-6)• a = 6• $f(x) = \int (6x(x-2))dx$ • $\int (6x^2 - 12x)dx$ • $\int (6x^2 - 12x)dx$ • $a = 2 \times 1^3 - 6 \times 1^2 + c$ • a = 85 marks

1 Alternative Method for •1 to •3

two simultaneous equations 2a(2-b) = 0 and a(1-b) = -6
b = 2
a = 6
3 marks



						IQs	of a grou	p of stud	lents	
S1	The	IQs of a	group of s	tudents were mea	sured and the	10	0 2 3	$5 \ 5 \ 6$	8 8	
	scor	es record	ed in the s	tem-and-leaf diag	ram as shown.		9			
	Ider	ntify any	outliers.			11	1 0 0	$2 \ 3 \ 5$	6 7	4
							9			-
ront	acina (ny 5 (in n	osition 1)			12	-			
repu	uciny q	[u.5] ($m p$	05111011 1)			13				
						10	5 2 0			
						n=20 10		means 1	02	
Qu. S1	part	marks 4	Grade C	Syllabus Code 4.1.2, 4.1.3	Calculator class CN	Source 04/61				
				wing generic m/s. EQUIVALENCE GUIDE	Primary Me	hod : Give 1 mark for e	each •			
METHO	D OR AN			OT USE THE PRIMARY SHOWN IN DETAIL IN	$\bullet^1 Q = 10$	$07, Q_0 = 118$				

- \bullet^1 pd : calculate quartiles
- \bullet^2 ss : know how to calculate fences
- \bullet^3 pd : calculate fence/interpret outlier
- ${\ensuremath{\bullet}}^4~{\rm pd}$: calculate fence/interpret outlier

- $\begin{array}{l} Q_1 = 107, Q_3 = 118 \\ eg \ lower \ fence = Q_1 1 \cdot 5(Q_3 Q_1) \\ fence = 90.5 \\ fence = 134.5 \ \& \ 136 \ is \ outlier \end{array}$ \bullet^2
- \bullet^3
- \bullet^4

4 marks

S2 Calculate the mean and variance of the discrete random variable X whose probability distribution is as follows:

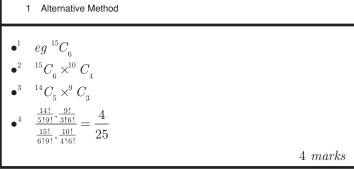
x	0	1	2	3	
$\mathbf{P}(X=x)$	0.4	0.3	0.2	0.1	6

Qu. S2	part	marks 6	Grade C	Syllabus Code 4.2.12	Calculator class NC	Source 04/66

The Primary Method m/s is based on the following generic m/s. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE	Primary Method : Give 1 mark for each •
BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME.	
 ¹ ss : know and state rule for mean ² pd : calculate mean ³ ss : know/state rule for variance ⁴ ss : know how to find E(X²) ⁵ pd : calculate E(X²) ⁶ pd : calculate variance 	• $E(X) = \Sigma x p(x)$ • $\Sigma x p(x) = 1$ • $V(X) = E(X^2) - (E(X))^2$ • $E(X^2) = \Sigma x^2 p(x)$ • $\Sigma x^2 p(x) = 2$ • $V(X) = 1$ 6 marks

S3 The committee of New Tron Golf Club consists of 15 men and 10 women which reflects the proportions of men and women who are members of the club. It is agreed to send a delegation of 10 committee members to a local planning meeting. The members of the delegation are to be chosen at random and will consist of 6 men and 4 women. What is the probability that both committee members Mr Hook and Miss Green will be selected?

Qu. S3	part	marks 4	Grade C	Syllabus Code 4.2.3, 4.2.7	Calcula NC	ator class	Source 04/67	
				owing generic m/s. EQUIVALENCE GUIDE	Pr	rimary Method	: Give 1 mark for each •	
	D OR AN	Y ALTERNAT		OT USE THE PRIMARY SHOWN IN DETAIL IN	•1	P(man) =	<u>- 6</u>	
	-	et probab et probab	e.		\bullet^2	P(lady) = multiply		
\bullet^3 ss :	-	o multiply	e.	endent events		$\frac{6}{15} \times \frac{4}{10} = \frac{4}{20}$	<u>L</u> 5	4 marks



S4 The cumulative distribution function for a random variable X is given by

$$F(x) = \begin{cases} \frac{1}{32} x^2 (6 - x) & 0 \le x \le 4\\ \\ 0 & \text{otherwise} \end{cases}$$

Show that the median is 2.

Qu. S4	part	marks 3	Grade AB	Syllabus Code 4.3.3, 4.3.5, 2.1.3	Calculator class NC	Source 04/70	
THIS GE BUT ON METHOI THE MA	ENERIC M ILY WHEF D OR AN RKING S	I/S MAY BE RE A CANDI Y ALTERNA	USED AS AN E DATE DOES N TIVE METHOD	owing generic m/s. EQUIVALENCE GUIDE OT USE THE PRIMARY SHOWN IN DETAIL IN	• ¹ $F(median)$ • ² $F(2) = \frac{1}{32}$: Give 1 mark for each •) = $\frac{1}{2}$ $\times 2^2 \times (6-2)$ hence median = 2	
• ² pd : • ³ ic :		ute et result					3 marks

- 1. Marks must be assigned in accordance with these marking instructions. In principle, marks are awarded for what is correct, rather than marks deducted for what is wrong.
- 2. Award one mark for each 'bullet' point. Each error should be underlined in RED at the point in the working where it first occurs, and not at any subsequent stage of the working.
- 3. The working subsequent to an error must be followed through by the marker with possible full marks for the subsequent working, provided that the difficulty involved is approximately similar. Where, subsequent to an error, the working is eased, a deduction(s) of mark(s) should be made. This may happen where a question is divided into parts. In fact, failure to even answer an earlier section does not preclude a candidate from assuming the result of that section and obtaining full marks for a later section.
- 4. Correct working should be ticked (✓). This is essential for later stages of the SQA procedures. Where working subsequent to an error(s) is correct and scores marks, it should be marked with a crossed tick (X). In appropriate cases attention may be directed to work which is not quite correct (e.g. bad form) but which has not been penalised, by underlining with a dotted or wavy line.

Work which is correct but inadequate to score any marks should be corrected with a double cross tick (\mathbf{X}).

- 5. The total mark for each section of a question should be entered in red in the **outer** right hand margin, opposite the end of the working concerned.
 - Only the mark should be written, **not** a fraction of the possible marks.
 - These marks should correspond to those on the question paper and these instructions.
- 6. It is of great importance that the utmost care should be exercised in adding up the marks. Where appropriate, all summations for totals and grand totals must be carefully checked.

Where a candidate has scored zero marks for any question attempted, "0" should be shown against the answer.

7. As indicated on the front of the question paper, full credit should only be given where the solution contains appropriate working. Accept answers arrived at by inspection or mentally where it is possible for the answer so to have been obtained. Situations where you may accept such working will be indicated in the marking instructions.

cont/

Mathematics Higher: Instructions to Markers

- 8. Do not penalise:
 - working subsequent to a correct answer
 - omission of units
 - bad form
 - legitimate variations in numerical answers
 - correct working in the "wrong" part of a question
- 9. No piece of work should be scored through even where a fundamental misunderstanding is apparent early in the answer. Reference should always be made to the marking scheme answers which are widely off-beam are unlikely to include anything of relevance but in the vast majority of cases candidates still have the opportunity of gaining the odd mark or two provided it satisfies the criteria for the mark(s).
- 10. If in doubt between two marks, give an intermediate mark, but without fractions. When in doubt between consecutive numbers, give the higher mark.
- 11. In cases of difficulty covered neither in detail nor in principle in the Instructions, attention may be directed to the assessment of particular answers by making a referal to the P.A. Please see the general instructions for P.A. referrals.
- 12. No marks should be deducted at this stage for careless or badly arranged work. In cases where the writing or arrangement is very bad, a note may be made on the upper left-hand corner of the front cover of the script.
- 13 **Do not write any comments on the scripts**. A summary of acceptable notation is given on page 4.

Summary

Throughout the examination procedures many scripts are remarked. It is essential that markers follow common procedures:

- 1 Tick correct working.
- 2 Put a mark in the right-hand margin to match the marks allocations on the question paper.
- 3 Do not write marks as fractions.
- 4 Put each mark at the end of the candidate's response to the question.
- 5 Follow through errors to see if candidates can score marks subsequent to the error.
- 6 Do not write any comments on the scripts.

Mathematics Higher: Instructions to Markers

Higher Mathematics : A Guide to Standard Signs and Abbreviations

Remember - No comments on the scripts. Please use the following and nothing else.

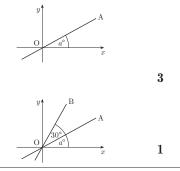
- The tick. You are not expected to tick every line but of course you must check through the whole of a response.
- X The cross and underline. Underline an error and place a cross at the end of the line.
- ★ The tick-cross. Use this to show correct work where you are following through subsequent to an error.
- The double cross-tick. Use this to show correct work but which is inadequate to score any marks.
- ∧ The roof. Use this to show something is missing such as a crucial step in a proof or a 'condition' etc.
 - The tilde. Use this to indicate a minor transgression which is not being penalised (such as bad form).
- E Eased. Where working is found correct whilst following through subsequent to an error, the working has been eased sufficiently for a mark not to be awarded.
- BOD Benefit of Doubt. Use this where you have to decide between two consecutive marks and award the higher.

line hole	Marks being allo normally be show		ould not	
noie		-	margin	s
	$\frac{dy}{dx} = 4x - 7$		IŬ	
	4x - 7 = 0	x		
and	$x = \frac{7}{4}$	^		
	$y = 3\frac{7}{8}$	× •		
	$y = 5\overline{8}$	ו	2	
¢	C = (1, -1)	X		
nt to	$m = \frac{3 - (-1)}{4 - 1}$	~		
	$m_{rad} = \frac{4}{3}$	∢ • follow	through	
			unougn	
	$m_{tgt} = \frac{-1}{\frac{4}{3}}$			
ect	$m_{igt} = -\frac{3}{4}$	ו		
	$m_{igi} = -\frac{3}{4}$ $y - 3 = -\frac{3}{4}(x - 2)$	ו	3	
ing	$x^2 - 3x = 28$	1.		
n'	x 0x - 20	•		
	x=7 🔨	ж	1	
	$\sin(x) = 0.75 = inv\sin(x)$	(0.75) = 48.6°		
uch	\sim			
		✓•	1	
t e	$\log_3(x-\underline{2}) = 1$	× ו		
:k	$(x-2) = 3^1$	ו		
	x - 2 = 3	N		
	<i>x</i> = 5	Ӿ Е	1	
			1 1	

All of these are to help us be more consistent and accurate.

It goes without saying that however accurate you are in marking, it is to no avail unless you have added the marks up correctly. Please double check totals!!

(a) The diagram shows line OA with equation x - 2y = 0. The angle between OA and the x-axis is a°.
(b) The second diagram shows lines OA and OB. The angle between these two lines is 30°. Calculate the gradient of line OB correct to 1 decimal place.



Qu. 1	part a b	marks 3 1	Grade C C	Syllabus Code 1.1.3 1.1.3	Calculator class CR	Source 04/81		
THIS GE	ENÉRIC N	M/S MAY BE	USED AS AN E	wing generic m/s. EQUIVALENCE GUIDE	Primary Metho	od : Give 1 marł	k for each •	
METHO		Y ALTERNA		OT USE THE PRIMARY SHOWN IN DETAIL IN	• ¹ gradien			
	find ou	radient of	a line		• ² $\tan a^\circ =$ • ³ $\tan^{-1}\left(\frac{1}{2}\right)$		stated or implied by \bullet^3	
	0		=tan(angle)	and apply	• tall $\sqrt{2}$) = 20.0		3 marks
	proces		(a. 8 .)		• $m_{l_2} = ta$	an(30+26.)	$6)^{\circ} = 1 \cdot 5$	0
			tan ⁻¹ (angle)		2	X	,	1 mark

1

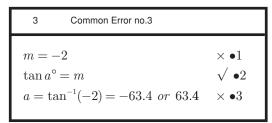
1 Common Error no.1

$$m = -2 \qquad \qquad \times \bullet 1$$

$$\tan a^{\circ} = m \qquad \qquad \sqrt{\bullet 2}$$

$$a = \tan^{-1}(-2) = 116.6 \qquad \qquad \sqrt{\bullet 3}$$

2	Common Error no.2	
m = 1	1	$\times \bullet 1$
$\tan a$	$^{\circ} = m$	$\sqrt{\bullet 2}$
a = t	$an^{-1}(1) = 45$	$\sqrt{\bullet 3}$



Notes

- 1 Accept any answer in (a) rounded correctly, so that e.g. if $a = 27^{\circ}$ (OK) $m_{\rm OB} = \tan(30+27)^{\circ} = 1.5$
- 2 A candiate who states $m = \tan \theta$, and does not go on to use it, cannot be awarded •2.
- 3 Treat $\tan\left(\frac{1}{2}\right) = 26 \cdot 6^{\circ}$ as very bad form.
- 4 In (b) do not penalise "not rounding to 1 d.p." but accept any correct answer which rounds to 1.5

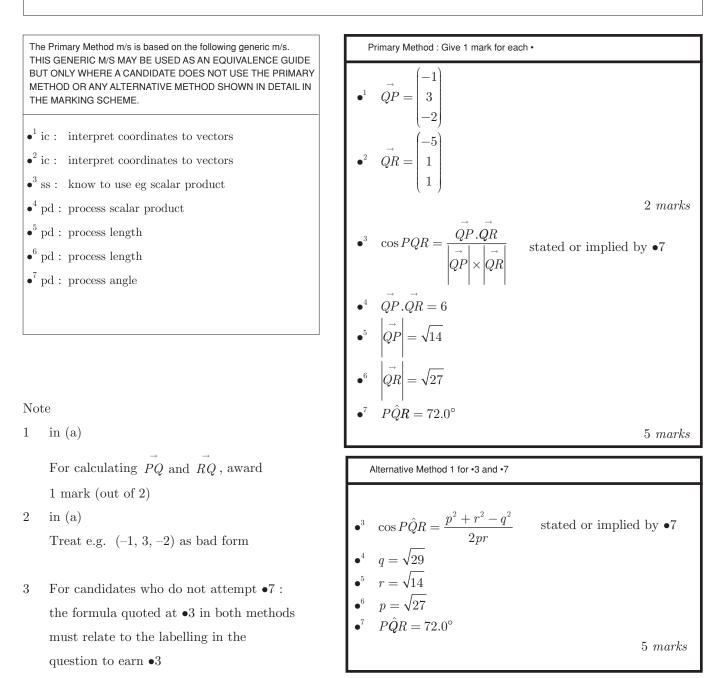
 $\mathbf{2}$

 $\mathbf{5}$

2 P,Q and R have coordinates (1, 3, -1), (2, 0, 1) and (-3, 1, 2) respectively.

- (a) Express the vectors QP and QR in component form.
- $(b)~{\rm Hence}~{\rm or}$ otherwise find the size of angle PQR.

2	part marks	s Grade	Syllabus Code	Calculator class	Source
	a 2	C	3.1.8	CR	04/117
I	b 5	С	3.1.9, 3.1.11		



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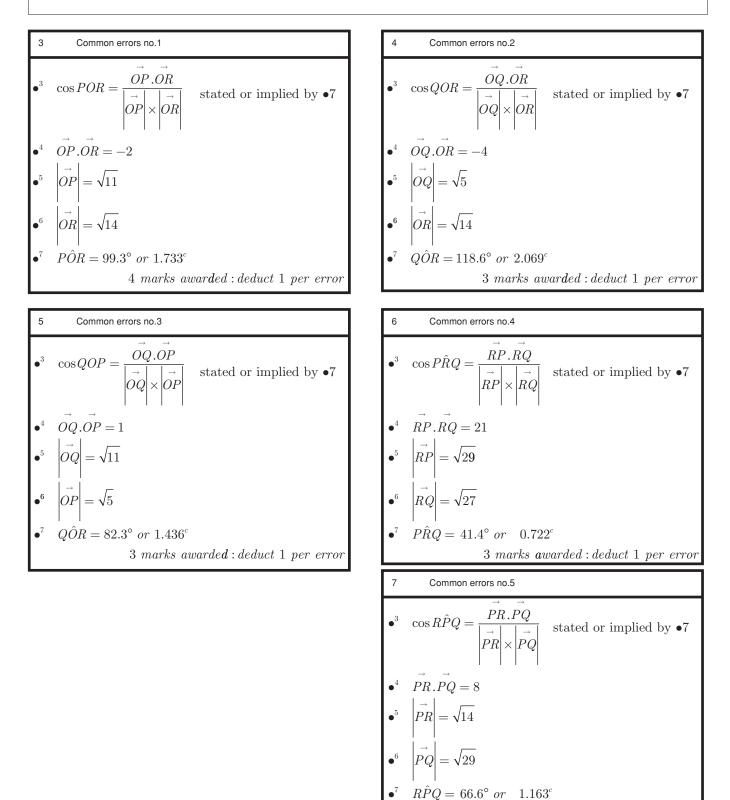
3 marks awarded : deduct 1 per error

 $\mathbf{2}$

 $\mathbf{5}$

- 2 P,Q and R have coordinates (1, 3, -1), (2, 0, 1) and (-3, 1, 2) respectively.
 - (a) Express the vectors QP and QR in component form.
 - (b) Hence or otherwise find the size of angle PQR.

	Source 04/117	Calculator class CR	Syllabus Code 3.1.8 3.1.9, 3.1.11	Grade C C	marks 2 5	part a b	Qu. 2
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4 marks

3 Prove that the roots of the equation $2x^2 + px - 3 = 0$ are real for all values of p.

Qu. 3	part	marks 4	Grade C,B	Syllabus Code 1.3.4, 1.1.6	Calculator class CN	Source 03/85	

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 \bullet^1 ss : know/use discriminant

 \bullet^2 ic : identify discriminant

 \bullet^3 pd : simplify

 \bullet^4 ic : complete proof

Primary Method : Give 1 mark for each •

• know to show $b^2 - 4ac \ge 0$ • $p^2 - 4 \times 2 \times (-3)$ • $p^2 + 24$ • p^2 is positive so $\Delta \ge 0$ and roots real

Note

- 1 Evidence for \bullet^1 will more than likely appear at the \bullet^4 stage.
- 2 Treat $b^2 4ac > 0$ as bad form

1 Alternative Method 1
•
$$x = \frac{-p \pm \sqrt{(-p)^2 - 4 \times 2 \times (-3)}}{4}$$

• $x = \frac{-p \pm \sqrt{p^2 + 24}}{4}$
• $we \ need \ p^2 + 24 \ge 0$
• $p^2 \ is \ positive \ and \ so \ roots \ real$
4 marks

3

- 4 A sequence is defined by the recurrence relation $u_{n+1} = ku_n + 3$.
 - (a) Write down the condition on k for this sequence to have a limit.
 - (b) The sequence tends to a limit of 5 as $n \to \infty$. Determine the value of k.

The Primary Method m/s is based on the following generic m/s. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE	Primary Method : Give 1 mark for each •				
BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME.	$\bullet^1 -1 < k < 1$	1 mark			
 ¹ ic : state condition for limit ² ss : know how to find limit ³ ic : substitute ⁴ pd : process 	• ² $l = "\frac{b}{1-a}"$ stated or implied by • ³ • ³ $5 = \frac{3}{1-k}$ • ⁴ $k = \frac{2}{5}$				
ra. r	0	3 marks			

 $\begin{array}{ll} 1 & -1 \leq k \leq 1 \ \text{does not gain } \bullet^1 \\ \text{but} \\ \text{accept "between } -1 \ \text{and } 1" \\ \text{accept } \ |k| < 1 \end{array}$

for \bullet^1 for \bullet^1

-1 < a < 1 does not gain •1 unless it has
been replaced by k in subsequent working in
(b)

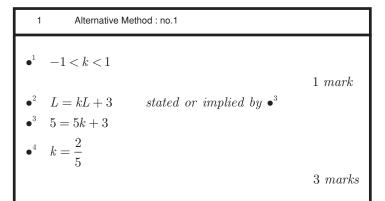
 $2 \quad {\rm Guess \ and \ check}:$

Guessing k = 0.4 and checking algebraically that this does yield a limit of 5 may be awarded 2 marks

3 Guess and check :

Guessing k = 0.4 and checking iteratively that this does yield a limit of 5 may be awarded 1 mark

- 4 No working : Simply stating that k = 0.4 earns no marks
- 5 Wrong formula : Work using an incorrect "formula" leading to a valid value of k may be awarded 1 mark.

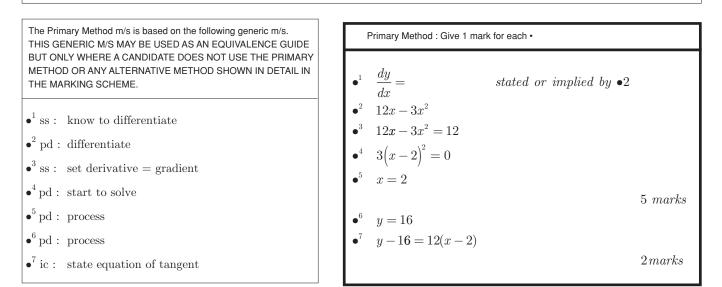


 $\mathbf{5}$

 $\mathbf{2}$

- 5 The point P(x, y) lies on the curve with equation $y = 6x^2 x^3$.
 - (a) Find the value of x for which the gradient of the tangent at P is 12.
 - (b) Hence find the equation of the tangent at P.

Qu.	part	marks	Grade	Syllabus Code	Calculator class	Source	
5	a	5	C	1.3.2, 1.3.9	CN	04/96	
	b	2	С	1.1.6			



1	Common error no.1	
$\bullet^1 $	$\frac{dy}{dx} =$	stated or implied by $\bullet 2$
· ·	$12x - 3x^2$	
$\bullet^3 \times$	$12x - 3x^2 = 0$	
\bullet^4 ×	3x(4-x)	
\bullet^5 $ imes$	x = 0 and $x = 4$	
		2 marks awarded
	$x = 4 \Rightarrow y = 32$	
$\bullet^7 $	y - 32 = 12(x - 4)	
		2 marks awarded

Notes

1 For $\frac{dy}{dx} = 12x - 3x^2$ $12x - 3x^2 = 12$

followed by a guess of x = 2 and no check, only

•1,•2 and •3 can be awarded.

2 For $\frac{dy}{dx} = 12x - 3x^2$

 $12x - 3x^2 = 12$

followed by a guess of x = 2 and a check that does in fact yield 12, $\bullet 1, \bullet 2, \bullet 3$ and $\bullet 4$ can be awarded.

6	(a) Express $3\cos(x^{\circ}) + 5\sin(x^{\circ})$ in the form $k\cos(x^{\circ} - a^{\circ})$ where $k > 0$ and $0 \le a \le 90$.	4
	(b) Hence solve the equation $3\cos(x^{\circ}) + 5\sin(x^{\circ}) = 4$ for $0 \le x \le 90$.	3

part marks Grade Syllabus Code Calculator class a 4 C 3.4.2 CR b 3 B 3.4.2 CR	3.4.2 CR 04
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BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME.	• ¹ $k \cos x \cos a + k \sin x \sin a$ STATED EXPLICITLY • ² $k \cos a = 3, k \sin a = 5$ STATED EXPLICITLY
• 1 ss : expand	• ³ $k = \sqrt{34}$
• ² ic : equate coefficients	• ⁴ $a = 59$ 4 marks
• ³ pd : solve for k	• $\sqrt{34}\cos(x-59)^\circ = 4$
• ⁴ pd : solve for a	• $\sqrt{54}\cos(x-59) = 4$ • $x-59 = \text{any one of}$
\bullet^5 ss : use transformed function	$-46 \cdot 7, 46 \cdot 7, 313.3$
• ⁶ pd : solve trig equation for " $x - a$ "	$\bullet^7 x = 12 \cdot 3$
• ⁷ pd : solve for x	3 marks

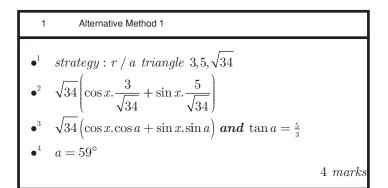
Note

1 Using $k\cos(x^\circ + a^\circ)$ etc:

candidates may use any form of wave equation to start with, as long as their answer is in the form $k \cos(x - a)$.

If it is not, then \bullet^4 is not available.

- 2 $k(\cos x \cos a + \sin x \sin a)$ is OK for \bullet^1
- 3 $\sqrt{34}\cos x\cos a + \sqrt{34}\sin x\sin a$ is OK for \bullet^1
- 4 Treat $k \cos x \cos a + \sin x \sin a$ as bad form provided \bullet^2 is gained
- 5 Accept answers which round to 5.8 for k at \bullet^3
- 6 For \bullet^4 , accept any answer which rounds to 59
- 7 Using $k \cos a = 5$, $k \sin a = 3$, leads to a = 31. Only marks \bullet^1 , \bullet^3 and \bullet^4 are available



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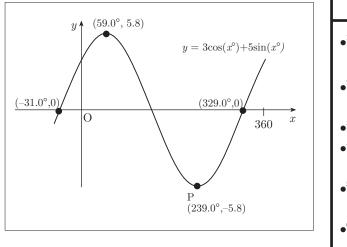
(a) Express
$$3\cos(x^{\circ}) + 5\sin(x^{\circ})$$
 in the form $k\cos(x^{\circ} - a^{\circ})$ where $k > 0$ and $0 \le a \le 90$.
(b) Hence solve the equation $3\cos(x^{\circ}) + 5\sin(x^{\circ}) = 4$ for $0 \le x \le 90$.

(b) Hence solve the equation $3\cos(x^{\circ}) + 5\sin(x^{\circ}) = 4$ for $0 \le x \le 90$.

6

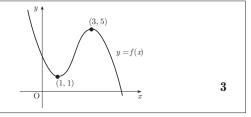
a 4 C 3.4.2 CR 04/122 b 3 B 3.4.2 CR

2	Common wrong solution	3	Early rounding
$ \begin{array}{c} \bullet^{1} \checkmark \\ \bullet^{2} \times \\ \bullet^{3} \checkmark \\ \bullet^{4} \checkmark \end{array} $	$k\cos x \cos a + k\sin x \sin a STATED EXPLICITLY$ $k\cos a = 5, k\sin a = 3 \qquad STATED EXPLICITLY$ $k = \sqrt{34}$ a = 31	$ \begin{array}{c} \bullet^{1} \checkmark \\ \bullet^{2} \checkmark \\ \bullet^{3} \checkmark \\ \bullet^{4} \checkmark \end{array} $	$k\cos x \cos a + k\sin x \sin a STATED EX.$ $k\cos a = 3, k\sin a = 5 \qquad STATED EX.$ k = 5.8 a = 59
$ \begin{array}{c} \bullet^{5} \checkmark \\ \bullet^{6} \checkmark \\ \bullet^{7} \times \end{array} $	$\sqrt{34}\cos(x-31)^\circ = 4$ $x-31 = any \text{ one of } 46 \cdot 7,313.3$ $x = 77.7^\circ \qquad (this mark not awarded as working eased)$ so award 5 marks((5 ticks)	$ \begin{array}{c} \bullet^{5} \checkmark \\ \bullet^{6} \checkmark \\ \bullet^{7} \checkmark \end{array} $	$6\cos(x-59)^\circ = 4$ $x-59 = any one of -48.2, 48 \cdot 2, 311.8$ $x = 10.8^\circ$ so award 7 marks((7 ticks)

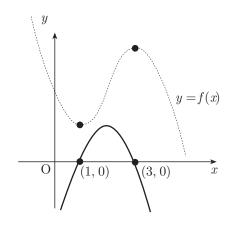


Alternative Method 2 via a Graphics Calcu	ulator
 annotated on diagram max at (59.0,5.8) and min at (239.0,-5.8) annotated on diagram (-31.0,0) or (149.0,0) or (329.0,0) "from the amplitude k = 5.8" 	
 ⁴ "from the shift a = 59.0" ⁵ communication : eg solution will be where y = 4 meets the graph ⁶ annotated on diagram the line with equation y = 4 	4 marks
• intersection gives $x = 12.3$	3 marks

7 The graph of the cubic function y = f(x) is shown in the diagram. There are turning points at (1, 1) and (3, 5). Sketch the graph of y = f'(x).

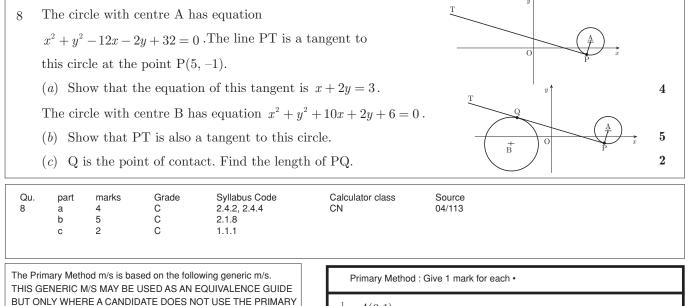


Qu. 7	part	marks 3	Grade B	Syllabus Code 1.3.13	Calculator class CN	Source 04/87	
THIS GE		I/S MAY BE	USED AS AN E	wing generic m/s. EQUIVALENCE GUIDE	Primary Method :	Give 1 mark for each •	
BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME.						the following details $tercepts$ on the x - axis at 1 and 3	
\bullet^2 ic :	interpr	et betwee	ary points n roots = paraboli	ı	 only two intercepts on the x⁻ axis at 1 and 5 function is + ve between the roots and - ve outwite a parabola (symmetrical about midpoint of x - intercepts), stated or implied by the accuracy of the diagram 		
						3 marks	



Note

- 1 The evidence for \bullet^1 may be on a diagram or in a table or in words
- 2 For \bullet^3 , with the intercepts unknown, they must lie on the positive branch of the *x*-axis
- 3 For a parabola passing through (1, 1) and (3, 5) award **ONLY 1 MARK.**



\bullet^1 ic \cdot	interpret	circle	equation
• 10 1	merpret	CITCIE	equation

 \bullet^2 ic : find gradient

THE MARKING SCHEME.

 \bullet^3 ss : know/find perpendicular gradient

METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN

- •⁴ pd : complete proof
- ${\bullet}^5~{\rm pd}$: start solving process
- \bullet^6 ss : know/substitute
- \bullet^7 pd : arrange in standard form
- \bullet^8 ss : know how to justify tangency
- \bullet^9 ic : complete proof
- •¹⁰ ic : interpret solution from (b)
- \bullet^{11} pd : process distance formula

Primary Method : Give 1 mark for each • •¹ A(6,1)•² $m_{AP} = 2$ STA TED EXPLICITLY •³ $m_{PQ} = -\frac{1}{2}$ •⁴ $y + 1 = -\frac{1}{2}(x-5)$ and complete 4 marks •⁵ x = 3 - 2y•⁶ $(3-2y)^2 + y^2 + 10(3-2y) + 2y + 6 = 0$ •⁷ $5y^2 - 30y + 45 = 0$ •⁸ solve and get double root \Rightarrow tangent •⁹ $5(y-3)^2 = 0$ 5 marks •¹⁰ Q = (-3,3)•¹¹ $PQ = \sqrt{80}$ 2 marks

Alternative method for •1 to •4

 $(3-2y)^2 + y^2 - 12(3-2y) - 2y + 32 = 0$

4 marks

Notes

- 1 •³ is **ONLY AVAILABLE** if •² has been awarded.
- ⁴ is only available if an attempt has been made to find a perpendicular gradient

3 completion at \bullet^4 :

the minimum acceptable would be

$$y+1 = -\frac{1}{2}(x-5)$$
$$2y+2 = -x+5$$
$$2y+x = 3$$

1

 $5(y+1)^2 = 0$

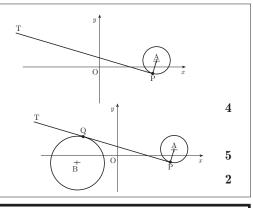
double root \Rightarrow tangent

 $x = 3 - 2y = 3 - 2 \times (-1) = 5$

- 8 The circle with centre A has equation
 - $x^2 + y^2 12x 2y + 32 = 0$. The line PT is a tangent to this circle at the point P(5, -1).
 - (a) Show that the equation of this tangent is x + 2y = 3.

The circle with centre B has equation $x^2 + y^2 + 10x + 2y + 6 = 0$.

- (b) Show that PT is also a tangent to this circle.
- (c) Q is the point of contact. Find the length of PQ.



Alternative for •8 and •9

- $\bullet^{8} \quad use \ discriminant, and \ get \ zero \Rightarrow tangent$
- •⁹ $b^2 4ac = (-30)^2 4.5.45 = 0$

Alternative for (c) (•10 and •11)

2

4

•⁸
$$BP = 10$$
 units, $BQ = radius = \sqrt{20}$ units

•⁹ by Pythagoras $PQ = \sqrt{80}$

4 An "= 0" must appear at either the \bullet^6 or \bullet^7 stage. Failure to appear will forfeit one of these marks.

5 Evidence for (b) may appear in the working for (c)

Notes cont

3 Alternative Method for (b) (*5 to *9) • $y = \frac{1}{2}(3-x)$ • $(x)^2 + (\frac{1}{2}(3-x))^2 + 10(x) + 2(\frac{1}{2}(3-x)) + 6 = 0$ • $5x^2 + 30x + 45 = 0$ • $5(x+3)^2 = 0$ • $double \ root \Rightarrow tangency$ or $b^2 - 4ac = 900 - 4.5.45 \Rightarrow tangency$ 5 marks

Alternative Method for (b) (•5 to •9)

•⁵ centre B = (-5, -1)•⁶ diam : y + 1 = 2(x + 5)•⁷ $2x + 9 = \frac{3 - x}{2}$ •⁸ Q = (-3, 3)•⁹ check : 9 + 9 - 30 + 6 + 6 = 0

5 marks

5 Common error for (b)

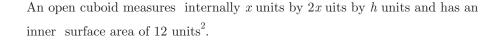
•⁵ × x = 2y - 3•⁶ $\sqrt{(2y - 3)^2 + y^2 + 10(2y - 3) + 2y + 6} = 0$ •⁷ $\sqrt{5y^2 + 10y - 15} = 0$ •⁸ $\sqrt{5(y + 3)(y - 1)} = 0$ •⁹ $\sqrt{$ intersects in two pts (y=1 and y=-3) \Rightarrow not a tgt 4 marks awarded

Higher Maths 2004 Paper 2 Marking Scheme Final

3

 $\mathbf{5}$

9

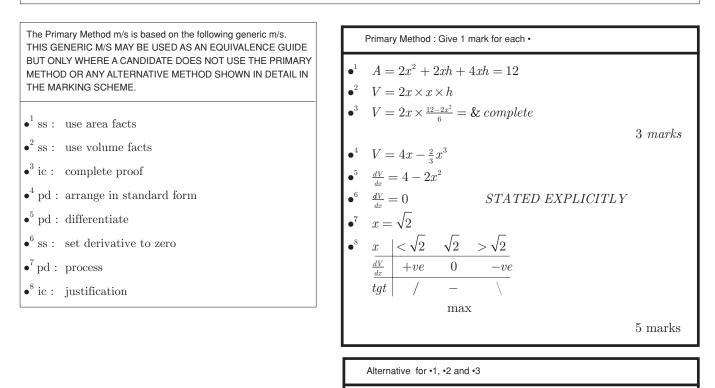


(a) Show that the volume, V units³, of the cuboid is given by

$$V(x) = \frac{2}{3}x\left(6 - x^2\right).$$

(b) Find the exact value of x for which this volume is a maximum.

Qu. 9	part a b	marks 3 5	Grade AB C	Syllabus Code 1.3.15 1.3.15	Calculator class CN	Source 04/n
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•
$$2x^{2} + 2xh + 4xh = 12$$

• $h = \frac{12 - 2x^{2}}{6x}$
• $V = 2x \times x \times \frac{12 - 2x^{2}}{6x} = \& complete$
3 marks

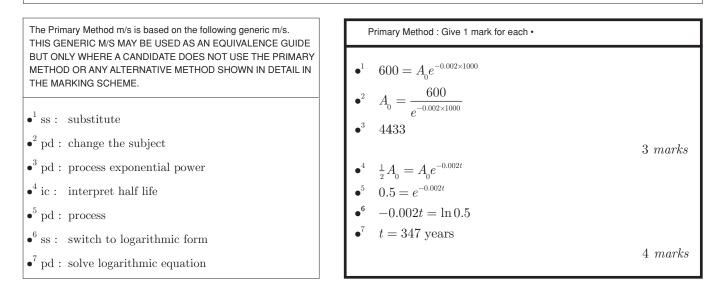
Notes

- 1 Do not penalise the non-appearance of $-\sqrt{2}$ at the \bullet^7 stage.
- 2 $\frac{d^2x}{dx^2} = -4x < 0 \Rightarrow$ maximum may be accepted for \bullet^8 .

- 10 The amount A_t micrograms of a certain radioactive substance remaining after t years decreases according to the formula $A_t = A_0 e^{-0.002t}$, where A_0 is the amount present initially. (a) If 600 micrograms are left after 1000 years, how many micrograms were present initially? **3**
 - (b) The half-life of a substance is the time taken for the amount to decrease to half of its

initial amount. What is the half-life of this substance?

		Source 04/121	Calculator class CR	Syllabus Code 3.3.4 3.3.4	Grade C AB	marks 3 4	part a b	Qu. 10
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	1 Alternative method for (a)	
	$600 = A_0 e^{-0.002 \times 1000}$ $\ln A_0 = \ln 600 - \ln e^{-0.002 \times 1000}$	
• ³	$A_0 = 4433$	3 marks

Notes

- Accept any correct answer which rounds to 4430.
 For any other answer, rounding must be indicated.
- 2 A trial and improvement approach :

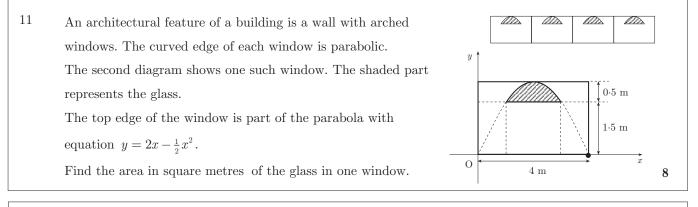
For $600 = A_0 e^{-2}$ award \bullet^1

For eg
$$4000e^{-2} = 541$$

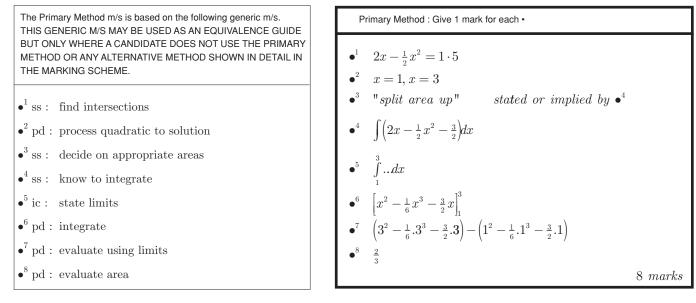
 $4500e^{-2} = 609$

leading to an answer which rounds to 4430, award \bullet^3

- 3 At \bullet^4 , A_0 may be replaced by any real number
- 4 For (b) an answer obtained by trial and improvement which rounds to 346 or 347 may be awarded 1 mark.



	Qu. 11	part	marks 8	Grade A	Syllabus Code 2.1.0, 2.1.9	Calculator class CN	Source 04/110	
L]



Alternative Method

Notes

1 The first two marks may be obtained as follows:

Guess x = 1 and check that y = 1.5, award \bullet^1 Guess x = 3 and check that y = 1.5, award \bullet^2

- 2 In the Primary method, \bullet^3 is clearly not available for subtracting the wrong way round.
 - \bullet^8 will also be lost for statements such as

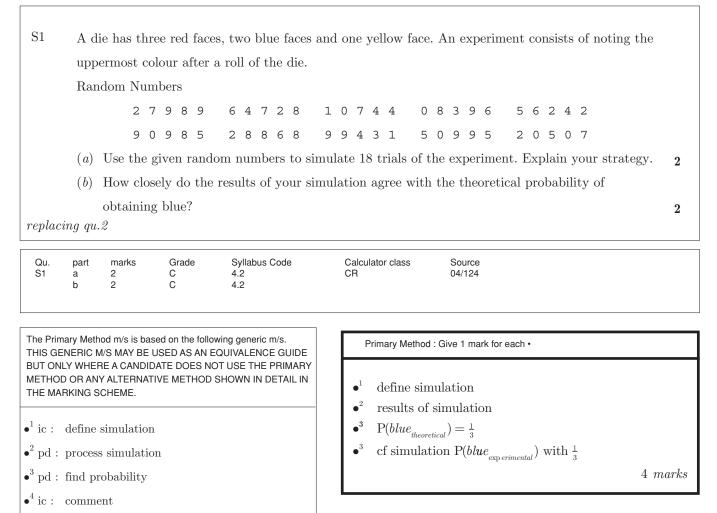
 $-\frac{2}{3}=\frac{2}{3}$

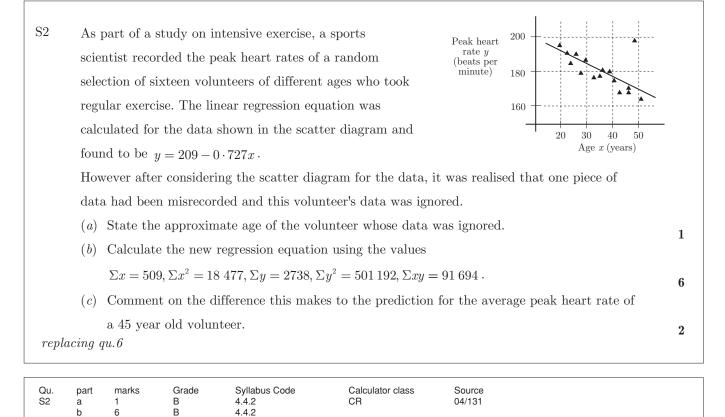
- $-\frac{2}{3}$ so ignore the negative
- $-\frac{2}{3}=\frac{2}{3}$ squ units
- \bullet^8 can still be gained for statements such as

 $\dots -\frac{2}{3}$ and so the area $=\frac{2}{3}$

•
$$2x - \frac{1}{2}x^2 = 1 \cdot 5$$

• $x = 1, x = 3$
• $\int (2x - \frac{1}{2}x^2) dx$
• choose limits, a and $b: 0 \le a \le b \le 4$
• $\left[x^2 - \frac{1}{6}x^3\right]$
• evaluate $\left[x^2 - \frac{1}{6}x^3\right]_a^b$ for chosen values of a and b
• r state areas to be added/subtracted $st / imp \ by \ \bullet^8$
• $\frac{2}{3}$
8 marks





The Primary Method m/s is based on the following generic m/s. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE	Primary Method : Give 1 mark for each •			
BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME.	\bullet^1 48	1 1		
\bullet^1 ic : estimate from graph	\bullet^2 $n=15$	1 mark		
• ² ic : state n	• $S_{xx} = 1204 \cdot 93$			
• ³ pd : process	• $S_{xy} = -1215 \cdot 47$			
• ⁴ pd : process	• ⁵ a = 217			
\bullet^5 pd : determine regression coefficients	$\bullet^6 b = -1 \cdot 01$			
\bullet^6 pd : determine regression coefficients	$\bullet^7 y = 217 - 1 \cdot 01x$	0 1		
• ⁷ ic: state regression equation	-8^{8} cot -176 cot -179	6 marks		
\bullet^8 pd : use regression equation	• ⁸ $est_{old} = 176, est_{new} = 172$ • ⁹ removing outlier improves estimate			
• ⁹ ic : interpret results	• removing outlier improves estimate	2 marks		

А

4.4.2

С

2

 $\mathbf{2}$

3

- S3The selection procedure for a Police force consists of 3 independent tests, Intelligence(I), Fitness (F) and Communication(C). The outcome of each test is an independent event and is either pass or fail. A candidate must pass all three tests to enter training. It has been established that the probability of failing each test is as follows: Test Ι F \mathbf{C} P(failing) 0.20.60.3(a) Calculate the probability that a candidate will be selected for training. (b) Five candidates are being tested for selection. Find the probability that all five candidates will be accepted (i)
 - (ii) all five candidates will be rejected.

S3 a 2 B 4.2.7 CN 04/126 b 32 B 4.2.10

The Primary Method m/s is based on the following generic m/s. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE	Primary Method : Give 1 mark for each •		
BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME.	• ¹ P(selected) = $0 \cdot 8 \times 0 \cdot 4 \times 0 \cdot 7$ • ² $0 \cdot 224 \text{ or } \frac{28}{125}$		
• ¹ ss : use approp. strategy $P(Pass)$ or 1 – $P(fail)$ • ² pd : process	• ³ $0 \cdot 224^5 = 0 \cdot 000564$ • ⁴ P(1 not selected) = 0.776	2 marks	
 ³ pd : process all pass ⁴ pd : process one fail ⁵ pd : process all fail 	• $1(1101 \text{ seccent}) = 0.110$ • $0.776^5 = 0.281$	3 marks	

yS4Show that the diagram represents a probability density $\frac{1}{5}$ function for a continuous random variable X. 3 0 4 replacing qu.10 Qu. part marks Grade Syllabus Code Calculator class Source S4 4.3.4 CN 04/129 3 А The Primary Method m/s is based on the following generic m/s. Primary Method : Give 1 mark for each • THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN \bullet^1 function above x - axisTHE MARKING SCHEME. •2 total area must be 1 $\frac{1}{2} \times 1 \times \frac{1}{5} + 3 \times \frac{1}{5} + \frac{1}{2} \times 3 \times \frac{1}{5}$ \bullet^3 $\bullet^1 \ {\rm ic}: \ \ {\rm state \ requirement \ for \ pdf}$ $=\frac{1}{10}+\frac{6}{10}+\frac{3}{10}=1$ \bullet^2 ic : state requirement for pdf 3 marks \bullet^3 pd : complete proof