

Functions - Lesson 3

Functions - Surds, Powers and Missing Inputs

LI

- Work out more complicated functions.
- Work out missing inputs.

SC

- Surds.
- Indices.
- Solve simple equations.

Example 1

If $f(x) = \sqrt{x}$ calculate :

(a) $f(12)$.

(b) $f(72)$.

(a) $f(x) = \sqrt{x}$

$$\therefore f(12) = \sqrt{12}$$

$$\Rightarrow f(12) = \sqrt{4} \sqrt{3}$$

$$\Rightarrow f(12) = 2\sqrt{3}$$

(b) $f(x) = \sqrt{x}$

$$\therefore f(72) = \sqrt{72}$$

$$\Rightarrow f(72) = \sqrt{36} \sqrt{2}$$

$$\Rightarrow f(72) = 6\sqrt{2}$$

Example 2

If $g(x) = 4^x$ calculate :

(a) $g(1/2)$.

(b) $g(-1/2)$.

(c) $g(3/2)$.

(a) $g(x) = 4^x$

$$\therefore g(1/2) = 4^{1/2}$$

$$\Rightarrow g(1/2) = \sqrt{4}$$

$$\Rightarrow g(1/2) = 2$$

(b) $g(x) = 4^x$

$$\therefore g(-1/2) = 4^{-1/2}$$

$$\Rightarrow g(-1/2) = \frac{1}{4^{1/2}}$$

$$\Rightarrow g(-1/2) = \frac{1}{2}$$

(c) $g(x) = 4^x$

$$\therefore g(3/2) = 4^{3/2}$$

$$\Rightarrow g(3/2) = (4^{1/2})^3$$

$$\Rightarrow g(3/2) = 2^3$$

$$\Rightarrow g(3/2) = 8$$

Example 3

If $r(x) = 4x + 7$, find the value of x so that $r(x) = 23$.

$$r(x) = 4x + 7, r(x) = 23$$

$$\therefore 4x + 7 = 23$$

$$\Rightarrow 4x = 16$$

$$\Rightarrow x = 4$$

Example 4

If $p(x) = 3x - 2$, find the value of b so that $p(b) = 12$.

$$p(x) = 3x - 2$$

$$\therefore p(b) = 3b - 2$$

$$\Rightarrow 3b - 2 = 12$$

$$\Rightarrow 3b = 14$$

$$\Rightarrow b = 14/3$$

Questions

- 1) If $f(x) = \sqrt{x}$ calculate : $f(8)$, $f(20)$, $f(27)$, $f(125)$.
- 2) If $g(x) = 9^x$ calculate : $g(1/2)$, $g(-1/2)$, $g(3/2)$.
- 3) If $p(x) = 2x + 9$, find the value of x if $p(x) = 17$.
- 4) If $r(x) = 7x + 30$, find the value of x if $r(x) = 79$.
- 5) If $T(x) = 5x - 9$, find the value of b if $T(b) = 21$.
- 6) If $N(x) = 6x - 15$, find the value of p if $N(p) = 27$.

Answers

1) If $f(x) = \sqrt{x}$ calculate : $f(8)$, $f(20)$, $f(27)$, $f(125)$.

$$2\sqrt{2} \quad 4\sqrt{2} \quad 3\sqrt{3} \quad 5\sqrt{5}$$

2) If $g(x) = 9^x$ calculate : $g(1/2)$, $g(-1/2)$, $g(3/2)$.

$$3 \quad 1/3 \quad 27$$

3) If $p(x) = 2x + 9$, find the value of x if $p(x) = 17$.

$$x = 4$$

4) If $r(x) = 7x + 30$, find the value of x if $r(x) = 79$.

$$x = 7$$

5) If $T(x) = 5x - 9$, find the value of b if $T(b) = 21$.

$$b = 6$$

6) If $N(x) = 6x - 15$, find the value of p if $N(p) = 27$.

$$p = 43/6$$

