

Factorisation - Lesson 2

Common Factors (2 Terms, 3 Variables Max.)

LI

- Factorise expressions of the form $pq \pm pr, pq^2 \pm pr$ and $p^2q \pm p^2r$ (no numbers).

SC

- Finding algebraic factors.

Reminders

$$2 \times x = 2x$$

$$x \times x = x^2$$

$$x \times y = xy$$

etc ...

An **algebraic factor** is a letter that **divides exactly** into another expression
(**no remainder**)

Example 1

$$p q$$

Factors : 1, p, q, pq

Example 2

$$y^2$$

Factors : 1, y, y^2

Example 3

$$x^2 y$$

Factors : 1, x, y, $x y$, x^2 , $x^2 y$

A **common algebraic factor** is an algebraic factor that is the same for two or more expressions

Example 4

$$x y \text{ and } x d$$

Factors of $x y$: 1, x, y, $x y$

Factors of $x d$: 1, x, d, $x d$

Common factors : 1, x

Example 5

$$p q \text{ and } p q^2$$

Factors of $p q$: 1, p, q, $p q$

Factors of $p q^2$: 1, p, q, $p q$, q^2 , $p q^2$

Common factors : 1, p, q, $p q$

Factorising Expressions

(Look for the Highest Common Factor)
 (Biggest common factor in both)

Example 6

Factorise $b x - b y$.

$$b x - b y$$

$$= \boxed{b(x - y)}$$

Example 7

Factorise $p x^2 - p y$.

$$p x^2 - p y$$

$$= \boxed{p(x^2 - y)}$$

Example 8

Factorise $b m^2 + n m$.

$$b m^2 + n m$$

$$= \boxed{m(bm + n)}$$

Example 9

Factorise $w^2 c - k w^2$.

$$w^2 c - k w^2$$

$$= \boxed{w^2(c - k)}$$

Example 10

Factorise $p^2 q + q^2 p$.

$$p^2 q + q^2 p$$

$$= \boxed{pq(p + q)}$$

19. $bu + bv$	20. $cx + cy$	21. $dp + dq$
22. $mu^2 + mv^2$	23. $nr^2 + ns^2$	24. $px^2 + py^2$
25. $qa^2 + qb^2$	26. $mx - my$	27. $nu - nv$
28. $pa - pb$	29. $qc - qd$	30. $ar^2 - as^2$
31. $bp^2 - bq^2$	32. $cx^2 - cy^2$	33. $dm^2 - dn^2$
34. $x^2 + xy$	35. $p^2 + pq$	36. $u^2 + uv$
37. $a^2 + ab$	38. $r^2 + rs$	39. $c^2 - cd$
40. $y^2 - yz$	41. $m^2 - mn$	42. $t^2 - tu$
43. $bc + c^2$	44. $de + e^2$	45. $yz + z^2$
46. $np + p^2$	47. $kl + l^2$	48. $qr - r^2$
49. $ef - f^2$	50. $st - t^2$	51. $lm - m^2$
52. $cd - d^2$	53. $ax^2 + bx^2$	54. $cy^2 + dy^2$
55. $mt^2 + nt^2$	56. $pz^2 + qz^2$	57. $ku^2 - lu^2$
58. $qv^2 - rv^2$	59. $br^2 - cr^2$	60. $ds^2 - es^2$

Answers

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|--------------------------|----------------|--------------------------|----------------|--------------------------|----------------|
| 19. $bu + bv$ | $b(u + v)$ | 20. $cx + cy$ | $c(x + y)$ | 21. $dp + dq$ | $d(p + q)$ |
| 22. $mu^2 + mv^2$ | $m(u^2 + v^2)$ | 23. $nr^2 + ns^2$ | $n(r^2 + s^2)$ | 24. $px^2 + py^2$ | $p(x^2 + y^2)$ |
| 25. $qa^2 + qb^2$ | $q(a^2 + b^2)$ | 26. $mx - my$ | $m(x - y)$ | 27. $nu - nv$ | $n(u - v)$ |
| 28. $pa - pb$ | $p(a - b)$ | 29. $qc - qd$ | $q(c - d)$ | 30. $ar^2 - as^2$ | $a(r^2 - s^2)$ |
| 31. $bp^2 - bq^2$ | $b(p^2 - q^2)$ | 32. $cx^2 - cy^2$ | $c(x^2 - y^2)$ | 33. $dm^2 - dn^2$ | $d(m^2 - n^2)$ |
| 34. $x^2 + xy$ | $x(x + y)$ | 35. $p^2 + pq$ | $p(p + q)$ | 36. $u^2 + uv$ | $u(u + v)$ |
| 37. $a^2 + ab$ | $a(a + b)$ | 38. $r^2 + rs$ | $r(r + s)$ | 39. $c^2 - cd$ | $c(c - d)$ |
| 40. $y^2 - yz$ | $y(y - z)$ | 41. $m^2 - mn$ | $m(m - n)$ | 42. $t^2 - tu$ | $t(t - u)$ |
| 43. $bc + c^2$ | $c(b + c)$ | 44. $de + e^2$ | $e(d + e)$ | 45. $yz + z^2$ | $z(y + z)$ |
| 46. $np + p^2$ | $p(n + p)$ | 47. $kl + l^2$ | $l(k + l)$ | 48. $qr - r^2$ | $r(q - r)$ |
| 49. $ef - f^2$ | $f(e - f)$ | 50. $st - t^2$ | $t(s - t)$ | 51. $lm - m^2$ | $m(l - m)$ |
| 52. $cd - d^2$ | $d(c - d)$ | 53. $ax^2 + bx^2$ | $x^2(a + b)$ | 54. $cy^2 + dy^2$ | $y^2(c + d)$ |
| 55. $mt^2 + nt^2$ | $t^2(m + n)$ | 56. $pz^2 + qz^2$ | $z^2(p + q)$ | 57. $ku^2 - lu^2$ | $u^2(k - l)$ |
| 58. $qv^2 - rv^2$ | $v^2(q - r)$ | 59. $br^2 - cr^2$ | $r^2(b - c)$ | 60. $ds^2 - es^2$ | $s^2(d - e)$ |