

Arc Length and Sector Area - Lesson 5

Arc Length and Sector Area
(Angle and Radius)

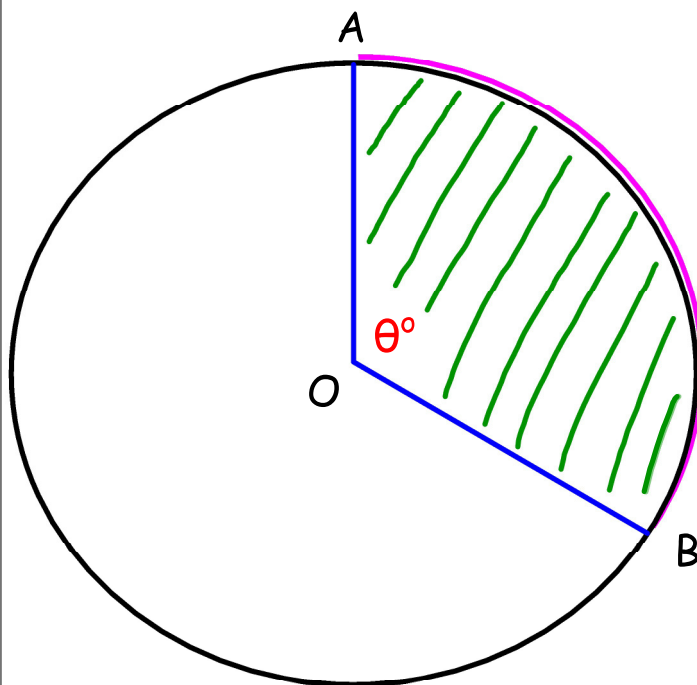
LI

- Calculate radius and angle.

SC

- Arc length and Sector area formulae.

Reminders

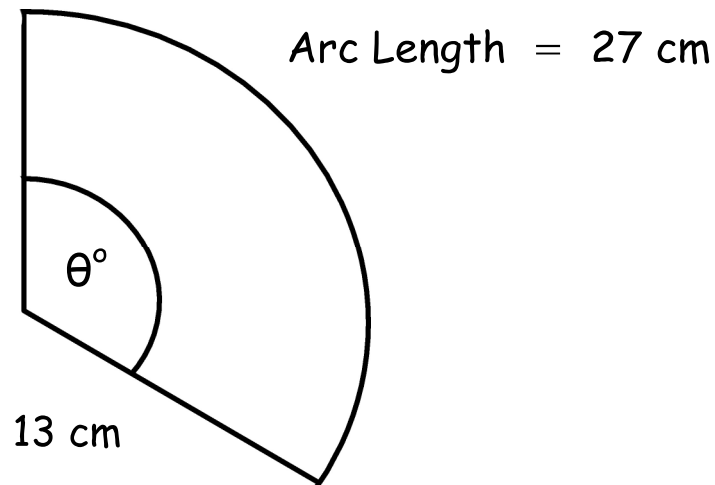


To work out **Arc Length**

$$L = \frac{\theta^\circ}{360^\circ} \times 2\pi r$$

To work out **Sector Area**

$$A = \frac{\theta^\circ}{360^\circ} \times \pi r^2$$

Example 1 (Working out Angle when told Arc Length and Radius)

$$L = 27 \text{ cm}, r = 13 \text{ cm}$$

$$L = \frac{\theta^\circ}{360^\circ} \times 2\pi r$$

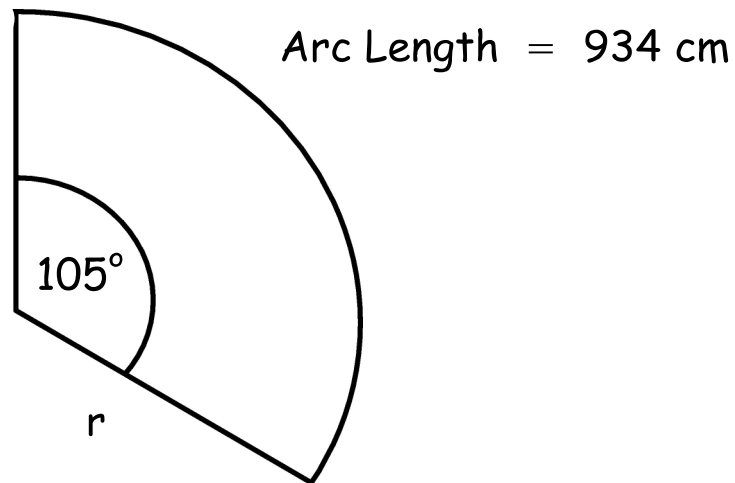
$$\therefore 27 = \frac{\theta^\circ}{360^\circ} \times 2 \times \pi \times 13$$

$$\Rightarrow 27 = \frac{26\pi \theta^\circ}{360^\circ}$$

$$\Rightarrow \theta^\circ = \frac{(27 \times 360^\circ)}{(26 \times \pi)}$$

$$\Rightarrow \theta^\circ = 118.99 \dots^\circ$$

$$\therefore \theta^\circ = 119^\circ \text{ (nearest degree)}$$

Example 2 (Working out Radius when told Arc Length and Angle)

$$L = 934 \text{ cm}, \theta^\circ = 105^\circ$$

$$L = \frac{\theta^\circ}{360^\circ} \times 2 \pi r$$

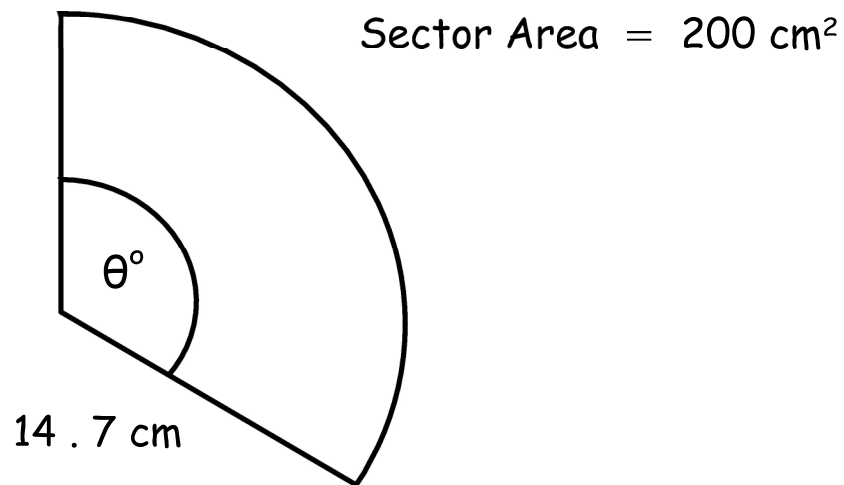
$$\therefore 934 = \frac{105^\circ}{360^\circ} \times 2 \pi r$$

$$\Rightarrow 934 = \frac{210^\circ \pi r}{360^\circ}$$

$$\Rightarrow r = \frac{(934 \times 360^\circ)}{(210^\circ \times \pi)}$$

$$\Rightarrow r = 509.65 \dots$$

$$\therefore r = 509.7 \text{ cm (1 d. p.)}$$

Example 3 (Working out Angle when told Sector Area and Radius)

$$A = 200 \text{ cm}^2, r = 14.7 \text{ cm}$$

$$A = \frac{\theta^\circ}{360^\circ} \times \pi r^2$$

$$\therefore 200 = \frac{\theta^\circ}{360^\circ} \times \pi \times 14.7^2$$

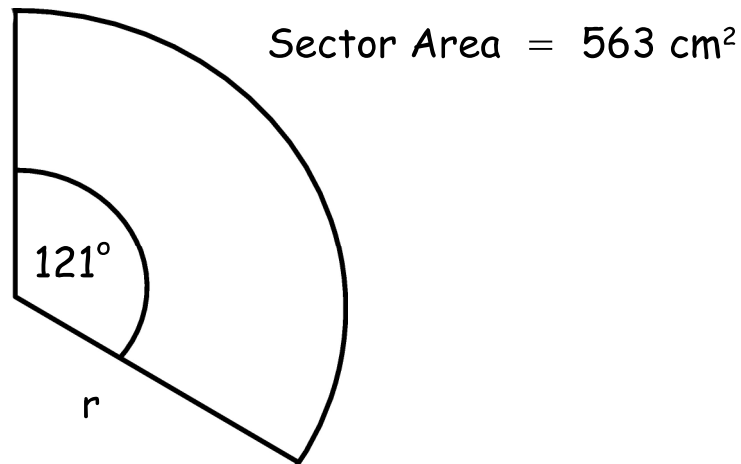
$$\Rightarrow 200 = \frac{216.09 \pi \theta^\circ}{360^\circ}$$

$$\Rightarrow \theta^\circ = \frac{(200 \times 360^\circ)}{(216.09^\circ \times \pi)}$$

$$\Rightarrow \theta^\circ = 106.05 \dots^\circ$$

$$\therefore \theta^\circ = 106.1^\circ \text{ (1 d. p.)}$$

Example 4 (Working out Radius when told Sector Area and Angle)



$$A = 563 \text{ cm}^2, \theta^\circ = 121^\circ$$

$$A = \frac{\theta^\circ}{360^\circ} \times \pi r^2$$

$$\therefore 563 = \frac{121^\circ}{360^\circ} \times \pi r^2$$

$$\Rightarrow 563 = \frac{121^\circ \pi r^2}{360^\circ}$$

$$\Rightarrow r^2 = \frac{(563 \times 360^\circ)}{(121^\circ \times \pi)}$$

$$\Rightarrow r^2 = 533.182 \dots$$

$$\Rightarrow r^2 = \sqrt{533.182 \dots}$$

$$\Rightarrow r = 23.09 \dots$$

$$\therefore r = 23 \text{ cm (nearest cm)}$$

- 1) A sector of a circle has a diameter of 36 cm and a sector area of 275 cm^2 . Find the sector angle (1 d.p.).
- 2) A sector of a circle has a sector angle of 61° and an arc length of 200.43 cm . Find the radius (2 d.p.).
- 3) A sector of a circle has a diameter of 20 cm and an arc length of 50 cm. Find the sector angle (nearest degree).
- 4) A sector of a circle has a sector angle of 231° and a sector area of 1000 cm^2 . Find the radius (3 s.f.).

Answers

- 1) A sector of a circle has a diameter of 36 cm and a sector area of 275 cm^2 . Find the sector angle (1 d.p.). **97.3°**
- 2) A sector of a circle has a sector angle of 61° and an arc length of 200.43 cm. Find the radius (2 d.p.). **188.26 cm**
- 3) A sector of a circle has a diameter of 20 cm and an arc length of 50 cm. Find the sector angle (nearest degree). **286°**
- 4) A sector of a circle has a sector angle of 231° and a sector area of $1\,000 \text{ cm}^2$. Find the radius (3 s.f.). **22.3 cm**