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Trigonometric Phenomena - Lesson 1

## Degrees, Radians and Exact Values

### LI

- Convert angles from degrees to Radians (and vice versa).
- Know and work out Exact Values of sin, cos and tan.

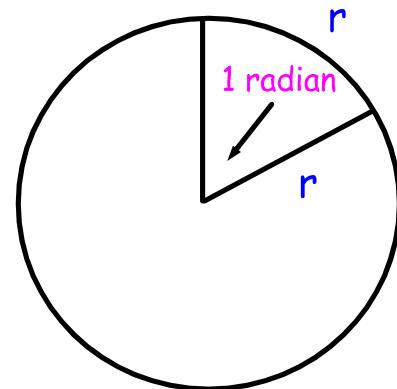
### SC

- Exact Value Table or Triangles.
- Trig. Graphs.

1 radian is the angle made by an arc of length equal to the radius of the circle

$$\pi \text{ radians} = 180^\circ$$

$$1 \text{ radian} \approx 57.3^\circ$$



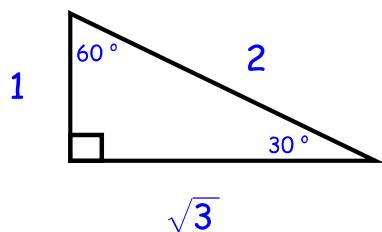
Radians are used to make equations in maths and physics look simpler

Must know these 8 equivalents :

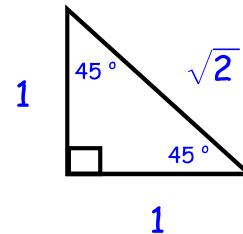
Degrees		Radians
$0^\circ$	↔↔↔↔↔	0
$30^\circ$	↔↔↔↔↔	$\frac{\pi}{6}$
$45^\circ$	↔↔↔↔↔	$\frac{\pi}{4}$
$60^\circ$	↔↔↔↔↔	$\frac{\pi}{3}$
$90^\circ$	↔↔↔↔↔	$\frac{\pi}{2}$
$180^\circ$	↔↔↔↔↔	$\pi$
$270^\circ$	↔↔↔↔↔	$\frac{3\pi}{2}$
$360^\circ$	↔↔↔↔↔	$2\pi$

**Exact Values** are numerical answers that are **not evaluated with a calculator**, but left as surds, fractions, expressions with  $\pi$  etc.

Must know standard sin, cos and tan exact values :



Exact Value Triangles



$$\sin 30^\circ = \sin \frac{\pi}{6} = \frac{1}{2}$$

$$\cos 30^\circ = \cos \frac{\pi}{6} = \frac{\sqrt{3}}{2}$$

$$\tan 30^\circ = \tan \frac{\pi}{6} = \frac{1}{\sqrt{3}}$$

$$\sin 45^\circ = \sin \frac{\pi}{4} = \frac{1}{\sqrt{2}}$$

$$\cos 45^\circ = \cos \frac{\pi}{4} = \frac{1}{\sqrt{2}}$$

$$\tan 45^\circ = \tan \frac{\pi}{4} = 1$$

$$\sin 60^\circ = \sin \frac{\pi}{3} = \frac{\sqrt{3}}{2}$$

$$\cos 60^\circ = \cos \frac{\pi}{3} = \frac{1}{2}$$

$$\tan 60^\circ = \tan \frac{\pi}{3} = \sqrt{3}$$

**Patel's Alternative Memory Aid :**

S	Angle	C	T
	0°		
	30°		
	45°		
	60°		
	90°		

Example 1

Change  $225^\circ$  to radians.

$$\begin{aligned} 225^\circ &= 180^\circ + 45^\circ \\ &= \pi + \frac{\pi}{4} \\ &= \boxed{\frac{5\pi}{4}} \end{aligned}$$

Alternative

$$\begin{aligned} 225^\circ &= 5 \times 45^\circ \\ &= 5 \times \frac{\pi}{4} \\ &= \boxed{\frac{5\pi}{4}} \end{aligned}$$

Example 2

Change  $\frac{4\pi}{3}$  radians into degrees.

$$\frac{4\pi}{3} = \frac{3\pi + \pi}{3}$$

$$= \pi + \frac{\pi}{3}$$

$$= 180^\circ + 60^\circ$$

$$= \boxed{240^\circ}$$

Alternative

$$\frac{4\pi}{3} = 4 \times \frac{\pi}{3}$$

$$= 4 \times 60^\circ$$

$$= \boxed{240^\circ}$$

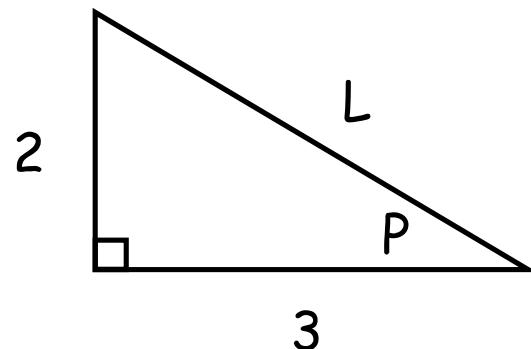
Example 3

If  $P$  is an acute angle with  $\tan P = \frac{2}{3}$ ,

find the exact values of  $\sin P$  and  $\cos P$ .

$$L = \sqrt{2^2 + 3^2}$$

$$L = \sqrt{13}$$



$$\sin P = \frac{O}{H}$$

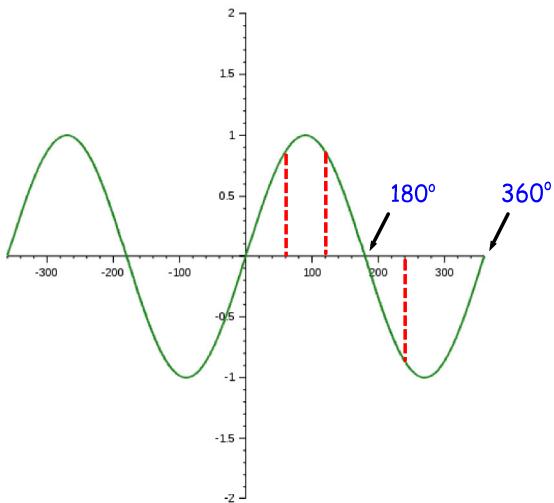
$$\cos P = \frac{A}{H}$$

$$\sin P = \frac{2}{\sqrt{13}}$$

$$\cos P = \frac{3}{\sqrt{13}}$$

Example 4

Find the exact value of  $\sin 240^\circ$ .



$$\begin{aligned}\sin 240^\circ &= -\sin 120^\circ \\&= -\sin 60^\circ \\&= -\frac{\sqrt{3}}{2}\end{aligned}$$

## CfE Higher Maths

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pg. 31 Ex. 2B All Q