

N 5 Practice Paper E - Solutions

(P 1)

$$1) \quad 2 \frac{1}{3} + \frac{5}{6} \text{ of } 1 \frac{2}{5}$$

$$= \frac{7}{3} + \frac{5}{6} \times \frac{7}{5}$$

$$= \frac{7}{3} + \frac{7}{6}$$

$$= \frac{14}{6} + \frac{7}{6}$$

$$= \frac{21}{6}$$

$$= \boxed{\frac{7}{2}}$$

$$2) \quad (4x + 2)(x - 5) + 3x$$

$$= 4x^2 - 20x + 2x - 10 + 3x$$

$$= \boxed{4x^2 - 15x - 10}$$

$$3) \quad m = \frac{4-2}{1-2}$$

(1, 4)

(2, 2)

$$m = \frac{2}{-1} \Rightarrow \boxed{m = -2}$$

$$y = -2x + c$$

$$4 = -2(1) + c \Rightarrow \underline{c = 6} \quad ; \quad \boxed{y = -2x + 6}$$

4)

$$\frac{2}{x} + 9 = 16$$

$$\frac{2}{x} = 7$$

$$2 = 7x$$

$$x = \frac{2}{7}$$

5)

$$2x^2 - 2x - 1 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\begin{pmatrix} a = 2 \\ b = -2 \\ c = -1 \end{pmatrix}$$

$$x = \frac{2 \pm \sqrt{(-2)^2 - 4(2)(-1)}}{2(2)}$$

$$x = \frac{2 \pm \sqrt{4 + 8}}{4}$$

$$x = \frac{2 \pm \sqrt{12}}{4}$$

$$x = \frac{2 \pm \sqrt{4} \sqrt{3}}{4}$$

$$x = \frac{2 \pm 2\sqrt{3}}{4}$$

$$x = \frac{1 \pm \sqrt{3}}{2}$$

6) (a) $(2, 36)$

(b) $x_c = 2$

(c) $y_R = y_S = 20$

$x_{cR} = 2 - 4 = -2$

$\therefore R(-2, 20)$

7) $h^2 = 5^2 - 4^2$

$h^2 = 25 - 16$

$h^2 = 9$

$h = 3$

$d = 7 - 3 \Rightarrow \underline{d = 4}$

$L^2 = 5^2 - 4^2$

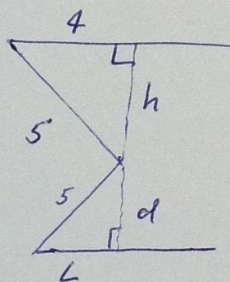
$L^2 = 9$

$L = 3 \text{ cm}$

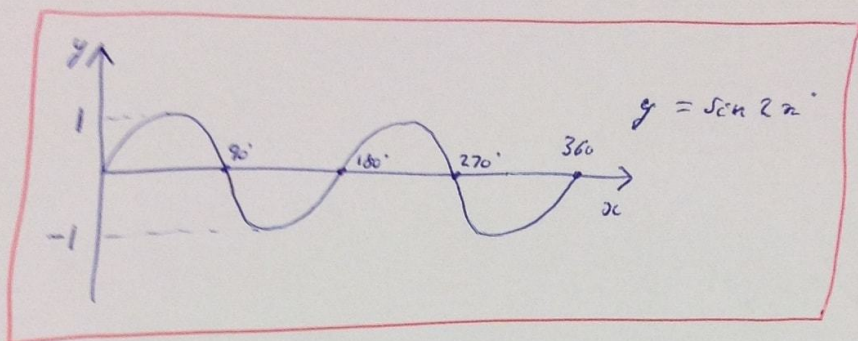
$w = 2 \times L$

$w = 2 \times 3$

$w = 6 \text{ cm}$



8)



9)

$$f(x) = 4\sqrt{x} + \sqrt{2}$$

$$(a) \quad f(72) = 4\sqrt{72} + \sqrt{2}$$

$$f(72) = 4\sqrt{36} \sqrt{2} + \sqrt{2}$$

$$f(72) = 24\sqrt{2} + \sqrt{2}$$

$$f(72) = 25\sqrt{2}$$

$$(b) \quad f(t) = 4\sqrt{t} + \sqrt{2} = 3\sqrt{2}$$

$$4\sqrt{t} = 2\sqrt{2}$$

$$\sqrt{t} = \frac{\sqrt{2}}{2}$$

$$t = \frac{2}{4}$$

$$t = \frac{1}{2}$$

$$10) \quad 7 = \frac{1}{2} \times 2x \times (2x-5)$$

$$x(2x-5) = 7$$

$$2x^2 - 5x = 7$$

$$2x^2 - 5x - 7 = 0$$

$$(2x-7)(x+1) = 0$$

$$2x-7=0, \quad x+1=0$$

$$x = \frac{7}{2}, \quad x = -1$$

If $x = -1$, $2x$ is negative; but lengths cannot be negative. So,

$$x = \frac{7}{2}$$

1) $E = mc^2$

$$E = (3.6 \times 10^{-2}) \times (3 \times 10^8)^2$$

$$E = 3.24 \times 10^{15}$$

2) $\text{Area} = \frac{1}{2} (21)(19) \sin 110^\circ$

$$\text{Area} = 187.468\dots$$

$$\text{Area} = 187.5 \text{ cm}^2 \text{ (1 d.p.)}$$

3) $28 \times (0.896)^3 = 20.14\dots$

$$\therefore 20.1^\circ\text{C (1 d.p.)}$$

4) (a) $C(4, 3, 4), D(6, 2, 2)$

(b) $B(6, 4, 2)$

$$5) \quad V_B = V_S \times k^3 \quad (k = LSF)$$

$$1600 = 200 k^3$$

$$k^3 = 8$$

$$\underline{k = 2}$$

$$h = 2 \times 12$$

$$\boxed{h = 24 \text{ cm}}$$

$$6) \quad \begin{array}{l} 2b + 5p = 5.2 \quad \textcircled{1} \quad \times 3 \\ 3b + 2p = 5.6 \quad \textcircled{2} \quad \times 2 \end{array} \quad \left(\begin{array}{l} b = \text{length of 1 bead} \\ p = \text{length of 1 pearl} \end{array} \right)$$

$$6b + 15p = 15.6 \quad \textcircled{3}$$

$$6b + 4p = 11.2 \quad \textcircled{4}$$

$$\underline{\textcircled{3} - \textcircled{4}}: \quad \begin{array}{l} 11p = 4.4 \\ \underline{p = 0.4} \end{array}$$

Substitute $p = 0.4$ into $\textcircled{1}$:

$$2b + 5(0.4) = 5.2$$

$$2b + 2 = 5.2$$

$$2b = 3.2$$

$$\underline{b = 1.6}$$

$$\boxed{\text{Length of 1 bead} = 1.6 \text{ cm}}$$

$$\boxed{\text{Length of 1 pearl} = 0.4 \text{ cm}}$$

$$7) (a) V = \frac{4}{3} \pi r^3, \quad r = 0.5$$

$$V = \frac{4}{3} \pi (0.5)^3$$

$$V = 0.52359\dots$$

$$V = 0.524 \text{ cm}^3 \text{ (3 s.f.)}$$

$$(b) V = \pi r^2 h$$

$$\pi (0.7)^2 h = 0.523\dots$$

$$h = 0.3401\dots$$

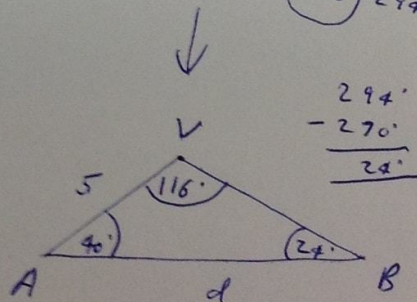
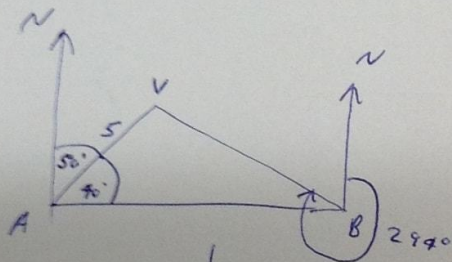
$$h = 0.34 \text{ cm (2 d.p.)}$$

$$8) \frac{d}{\sin 116^\circ} = \frac{5}{\sin 24^\circ}$$

$$d = \frac{5 \times \sin 116^\circ}{\sin 24^\circ}$$

$$d = 11.048\dots$$

$$d = 11.05 \text{ km (2 d.p.)}$$



$$180^\circ - 40^\circ - 24^\circ = 116^\circ$$

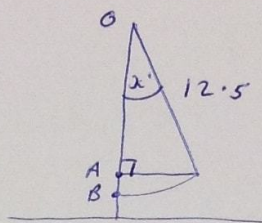
9) (a)

$$\cos \alpha = \frac{11.5}{12.5}$$

$$\alpha = \cos^{-1}\left(\frac{11.5}{12.5}\right)$$

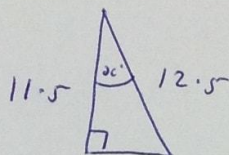
$$\alpha = 23.07\dots$$

$$\alpha = 23^\circ \text{ (nearest degree)}$$



$$AB = 2.5 - 1.5 = 1$$

$$OA = 12.5 - 1 = 11.5$$



$$(b) \quad L = \frac{\theta}{360} \times 2\pi r$$

$$L = \frac{(23.07\dots \times 2)}{360} \times 2 \times \pi \times 12.5$$

$$L = 10.06\dots$$

$$L = 10.1 \text{ m (3 s.f.)}$$

$$10) \quad kx^2 - 4x + 2 = 0$$

$$D = b^2 - 4ac$$

$$D = 16 - 8k$$

$$\begin{pmatrix} a = k \\ b = -4 \\ c = 2 \end{pmatrix}$$

Real roots means $D \geq 0$. So,

$$16 - 8k \geq 0$$

$$8k \leq 16$$

$$k \leq 2$$

11) (a)

$$\sqrt{3} \sin x - 1 = 0, \quad 0 \leq x < 360$$

$$\sin x = \frac{1}{\sqrt{3}}$$

$$RA = \sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$$

$$RA = 35.3^\circ$$

sin is +ve

S	A
✓	✓
$180^\circ - RA$	RA
$180^\circ + RA$	$360^\circ - RA$
T	C

$$x = 180^\circ - RA, RA$$

$$x = 35.3^\circ, 180^\circ - 35.3^\circ$$

$$x = 35.3^\circ, 144.7^\circ$$

(b)

$$\tan x \cos x = \left(\frac{\sin x}{\cos x} \right) \times \left(\frac{\cos x}{1} \right)$$

$$= \frac{\sin x \cos x}{\cos x}$$

$$= \sin x$$